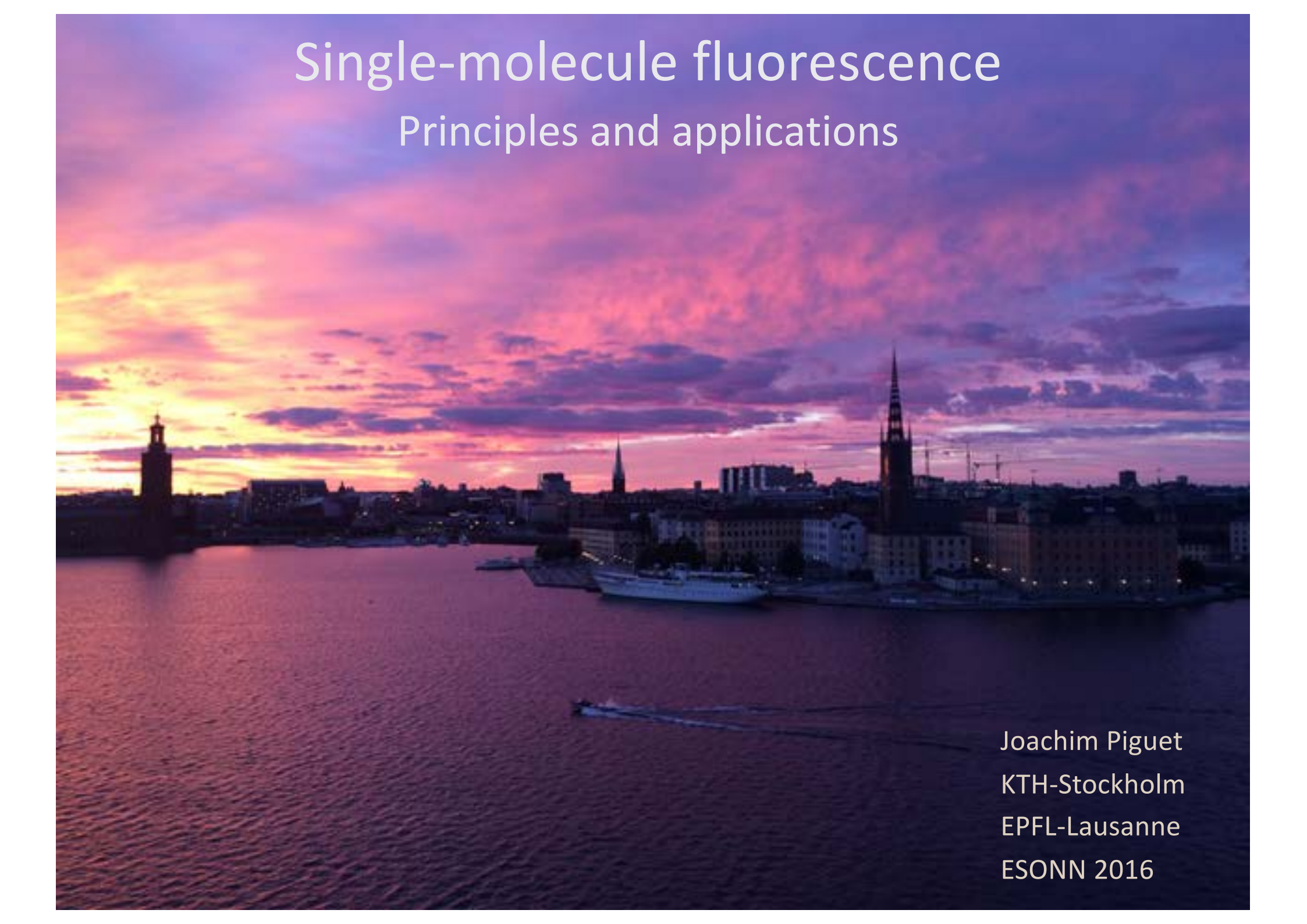


# Single-molecule fluorescence

## Principles and applications



Joachim Piguet  
KTH-Stockholm  
EPFL-Lausanne  
ESONN 2016

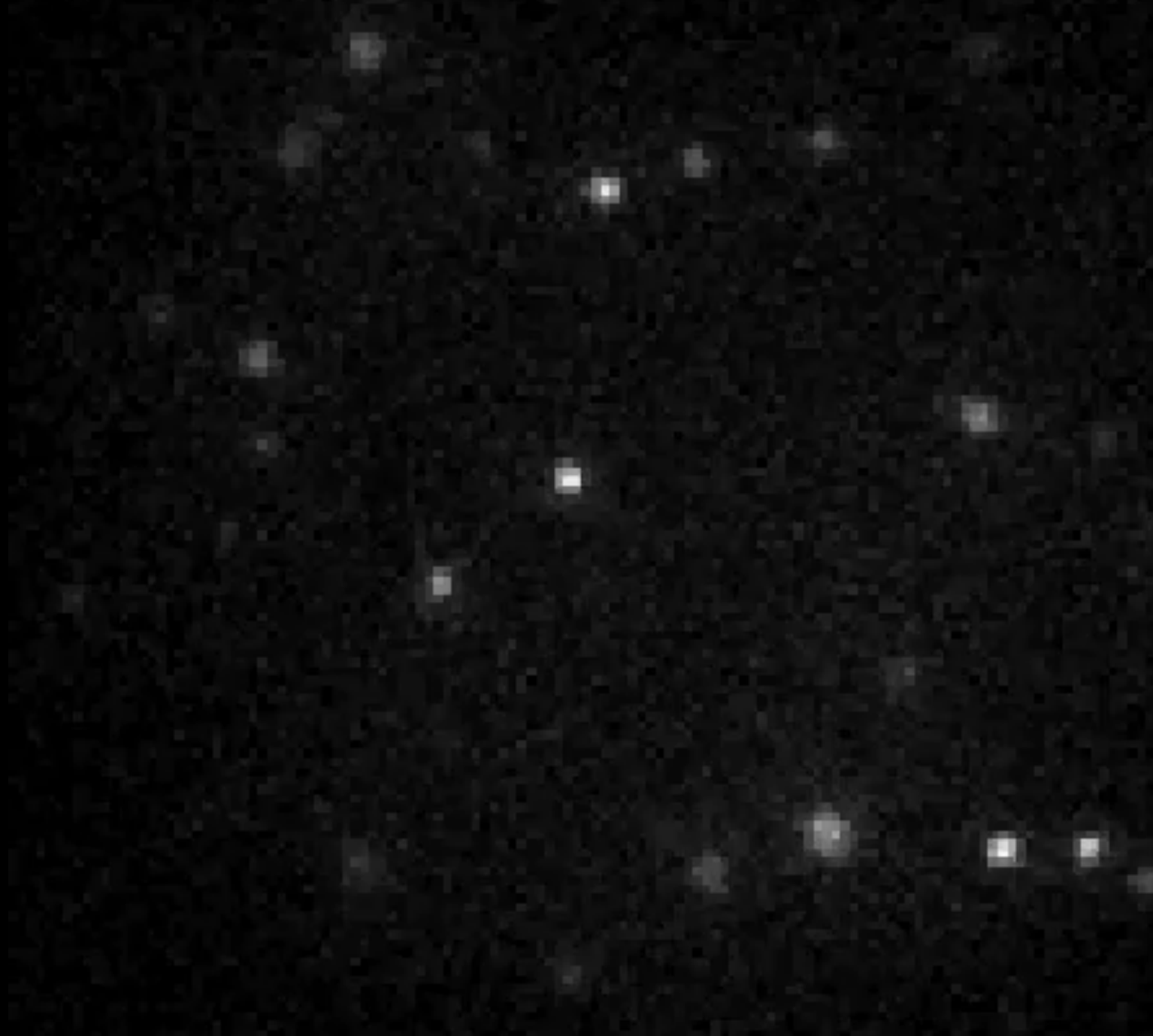
# Course structure

- A. Fundamentals
- B. Microscopy and fluorescence imaging setup
- C. Single-molecules
- D. Fluorescence nanoscopy
- E. Single-molecule detection and fluorescence signal correlation
- F. Functional devices based on single-molecule
- G. Nanopores

## Observing a nanomachine at work: Single-molecule imaging or spectroscopy (SMI or SMS)

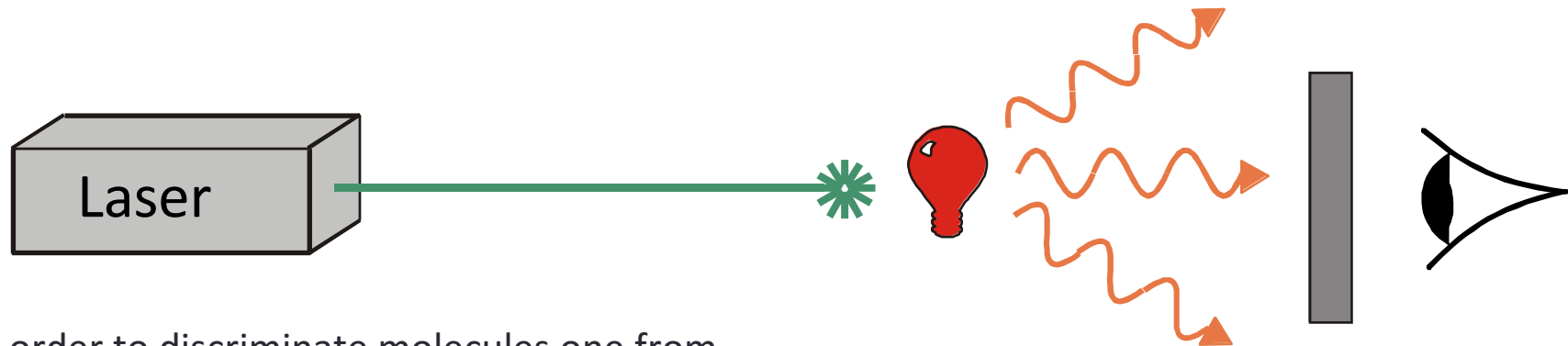
- Observation of the function and the motion of nano-objects in real-time in living systems
- Measurements on single molecule and not on ensemble of molecules
- Statistical analysis based on individual events
- Non-invasive and highly specific measurements
- Large choice of fluorophores and labels
- Controlled apparent dilution of the probe:
  - Controlled labeling,
  - Photobleaching,
  - Photoactivation,
  - Photoswitching,
  - Blinking,
  - Volume reduction,
  - Ground state depletion
  - Interference patterns

# Single-molecules detection



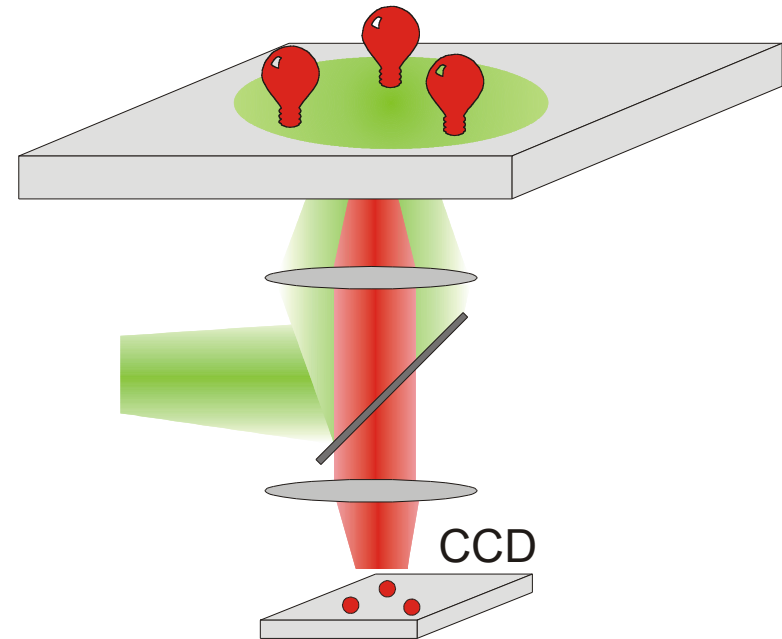


# Measurement principle: Fluorescence microscopy

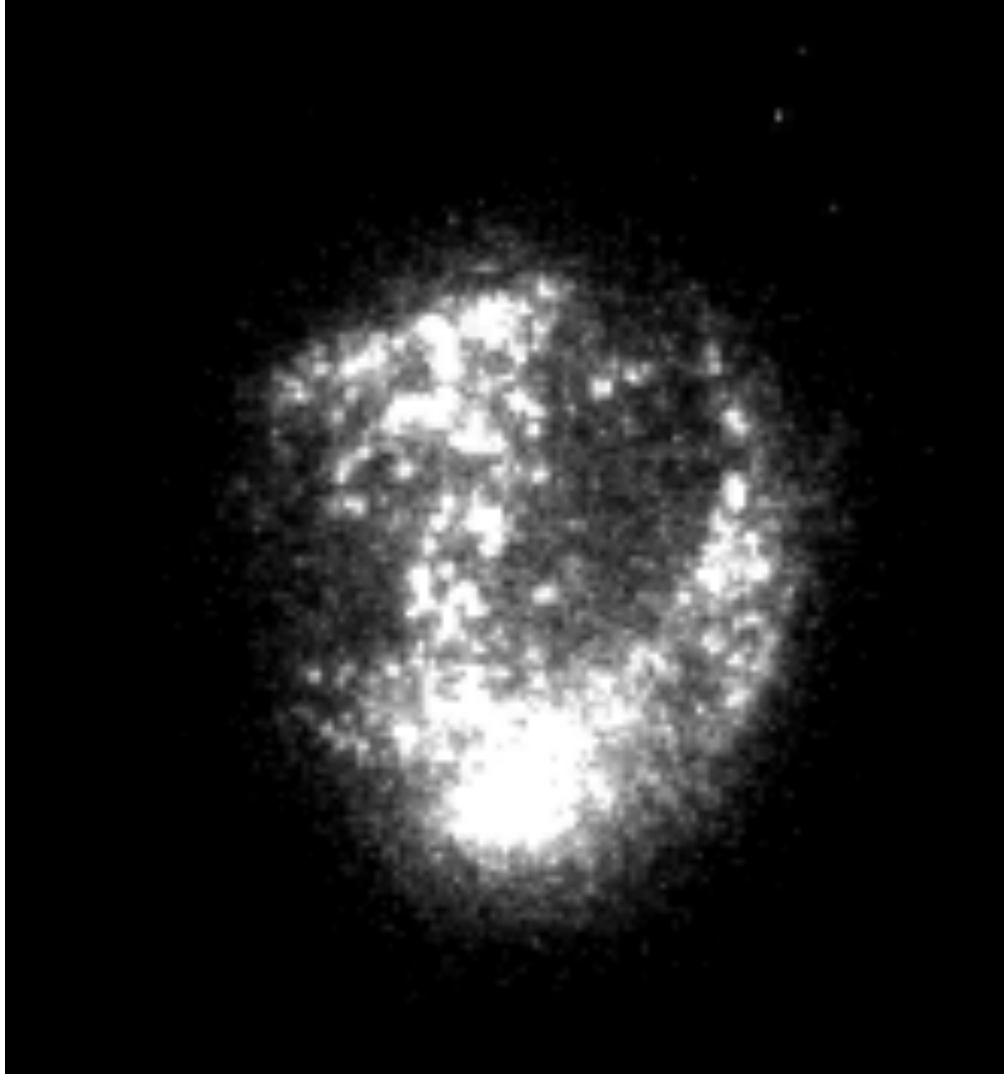


In order to discriminate molecules one from each others, it is necessary to dilute the concentration of fluorophores to such an extent that the average distance between two fluorophores is larger than the resolution of the microscope (confocal or wide-field). Depending on the experiment, the dilution will occur:

- ❖ in a cell membrane
- ❖ in an artificial membrane
- ❖ on a biomodified surface
- ❖ in a thin polymer sheet spin coated on a glass surface
- ❖ in a microfluidics device

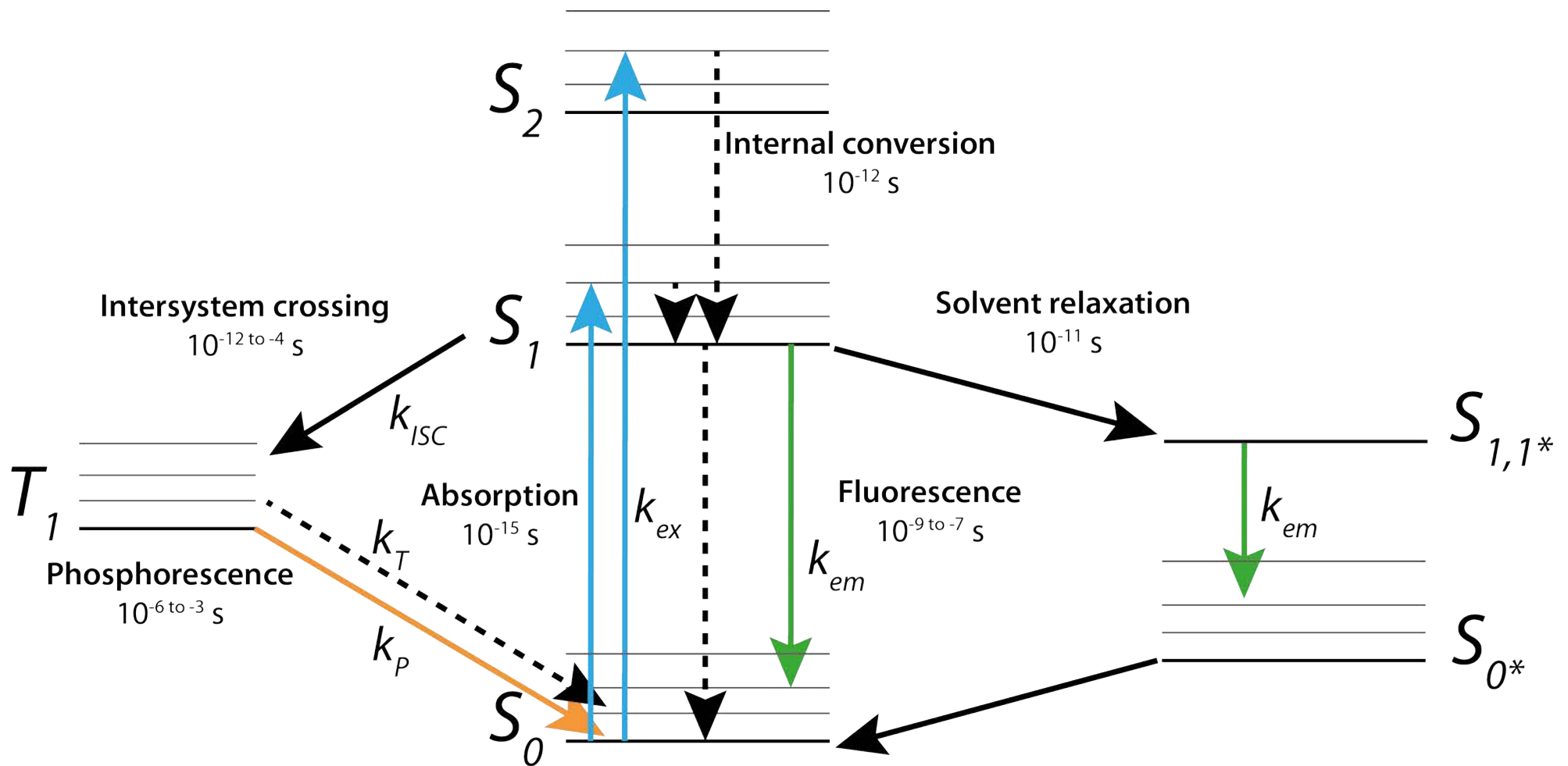


# Benefits of single-molecule experiments



- No ensemble averaging
- No temporal averaging (no need to synchronize).
- Give access to novel experimental parameters (in particular to a higher position accuracy).
- Can increase the resolution of microscopy beyond Abbe limit (superresolution microscopy)

# Fundamentals: Jablonski's diagram



- Fluorescence lifetime:  $1/k_f = t_f = 1/(k_{em} + S k_i)$ , radiative lifetime  $t_r = 1/k_{em}$
- Fluorescence quantum yield  $q_f = t_f/t_r = \# \text{ emitted photons} / \# \text{ absorbed photons}$

# Fundamentals: Signal emitted by a single molecule

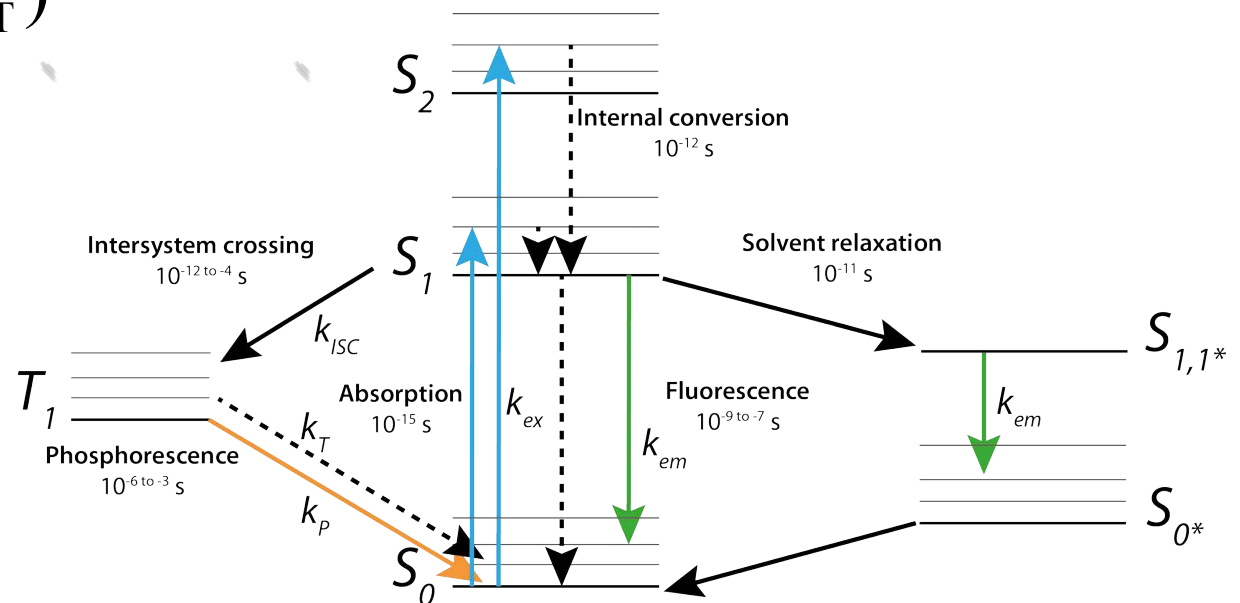
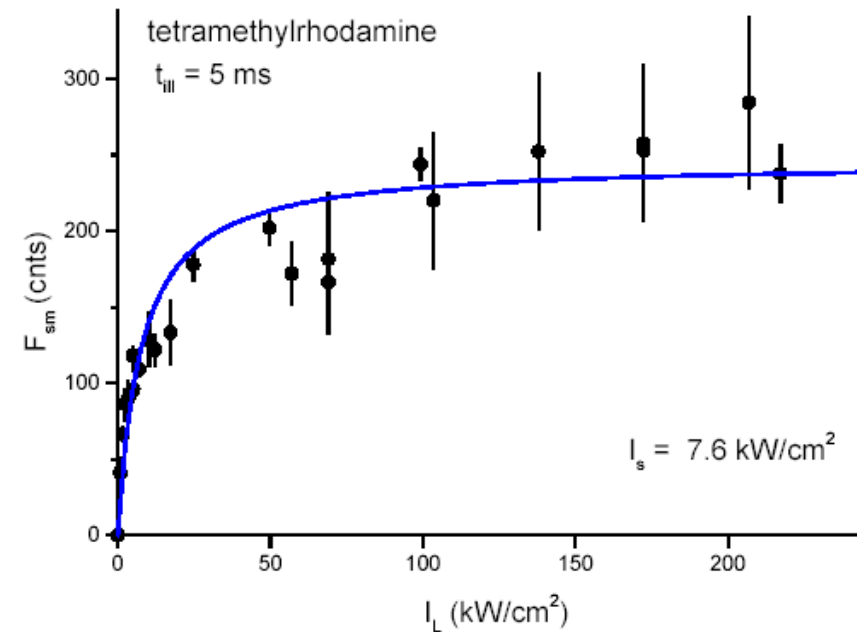
$$R(I_{\text{ex}}) = R_{\text{max}} \frac{I_{\text{ex}} / I_{\text{sat}}}{1 + I_{\text{ex}} / I_{\text{sat}}}$$

$$R_{\text{max}} = \frac{k_f q_f}{(1 + k_{\text{ISC}} / k_T)}$$

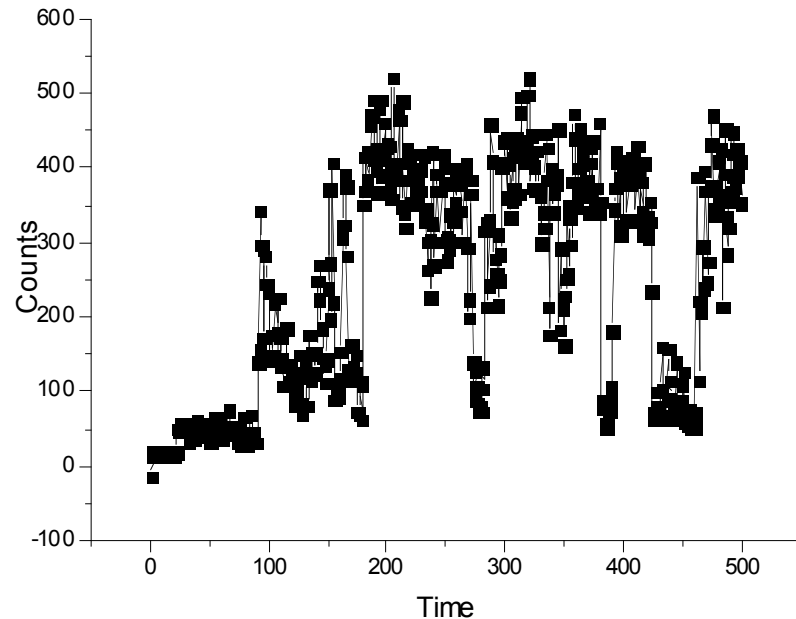
$$I_{\text{sat}} = \frac{(k_f)}{\sigma \cdot (1 + k_{\text{ISC}} / k_T)}$$

$$\sigma = 3\sigma_{\text{av}} \cos^2 \theta$$

$R$  = fluorescence emission rate,  
 $I_{\text{ex}}$  = laser excitation intensity,  
 $I_{\text{sat}}$  = saturation intensity,  
 $k_T$  = triplet decay rate,  
 $k_{\text{ISC}}$  = inter-system crossing rate,  
 $s$  = absorption cross-section



# Fundamentals: Fluorescence timetrace



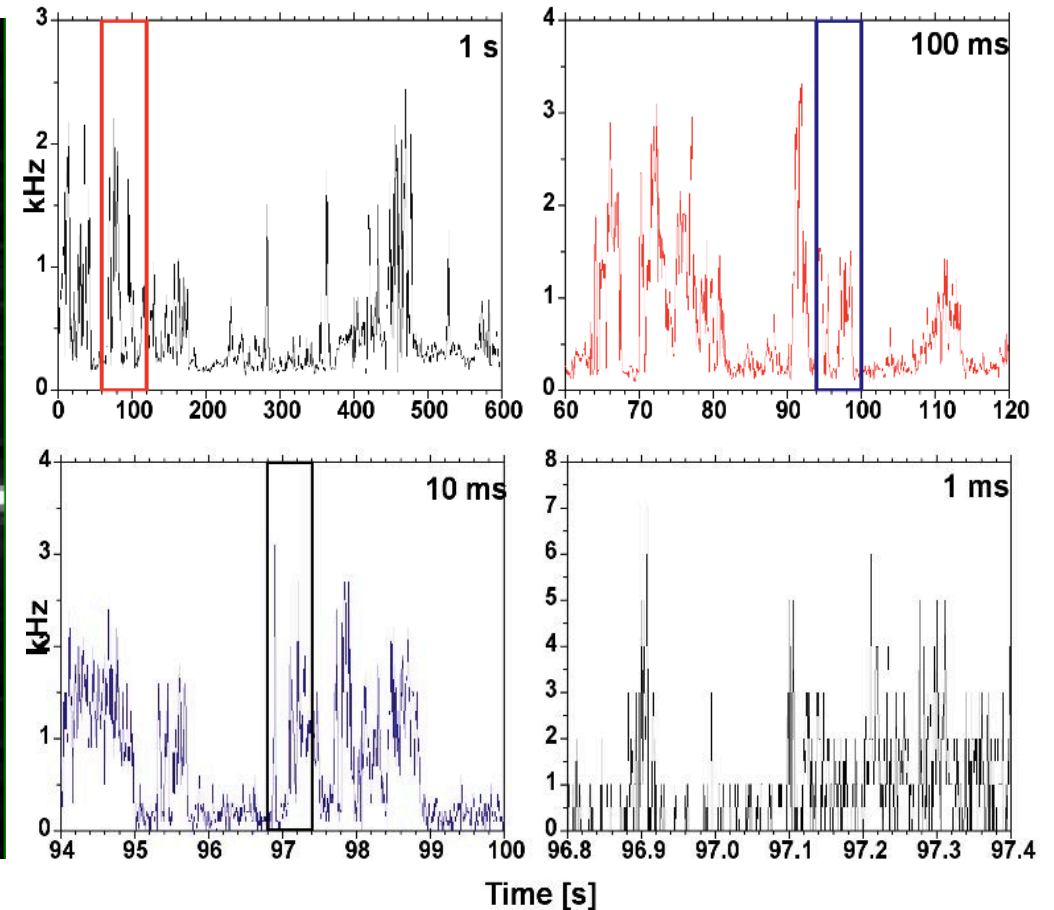
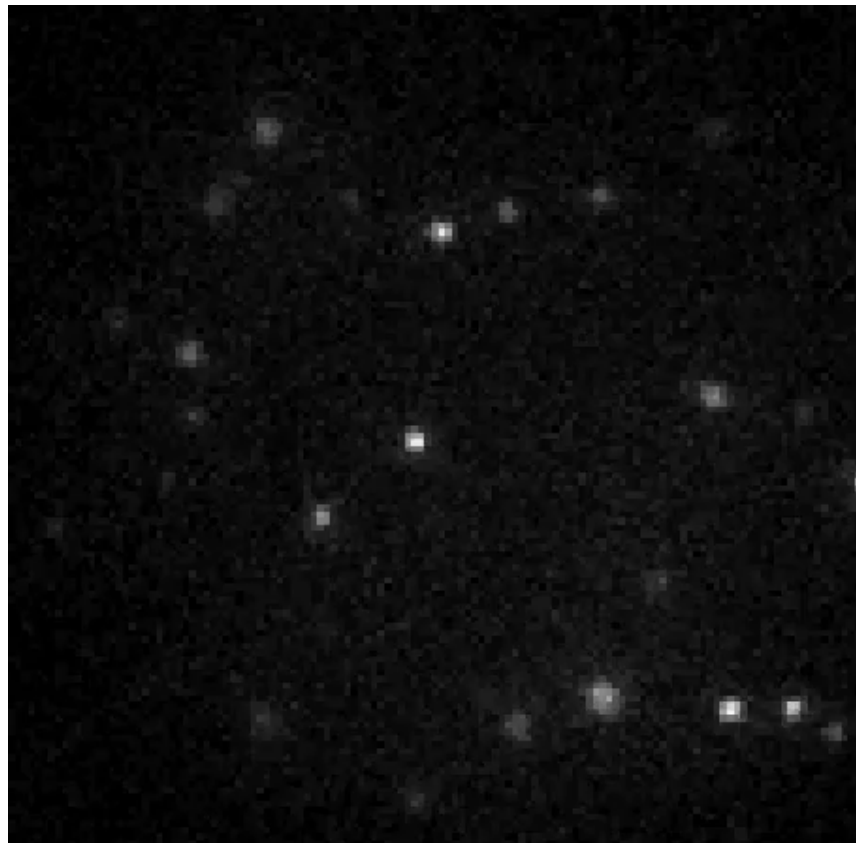
Blinking can have several origins:

- Triplet and other dark states.
- Modifications in the environment: Changes of the spectrum or of the fluorescence quantum yield.
- Chemical reactions (e.g. protonation) or complex formations (with  $O_2$ ).
- photo-ionisation.
- etc...



# Fundamentals: Blinking of quantum dots

Blinking of semi-conductor nanoparticles (quantum dots) is very pronounced due to photo-ionisation

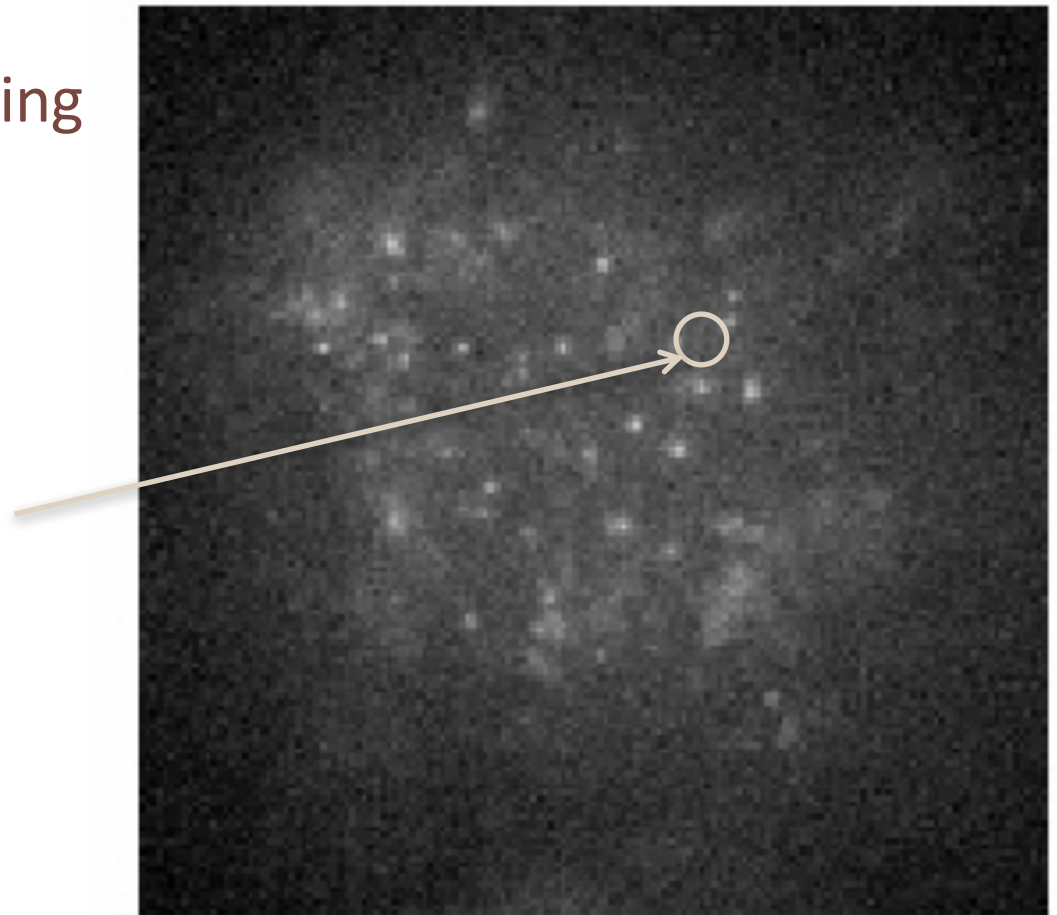
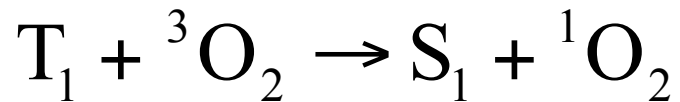
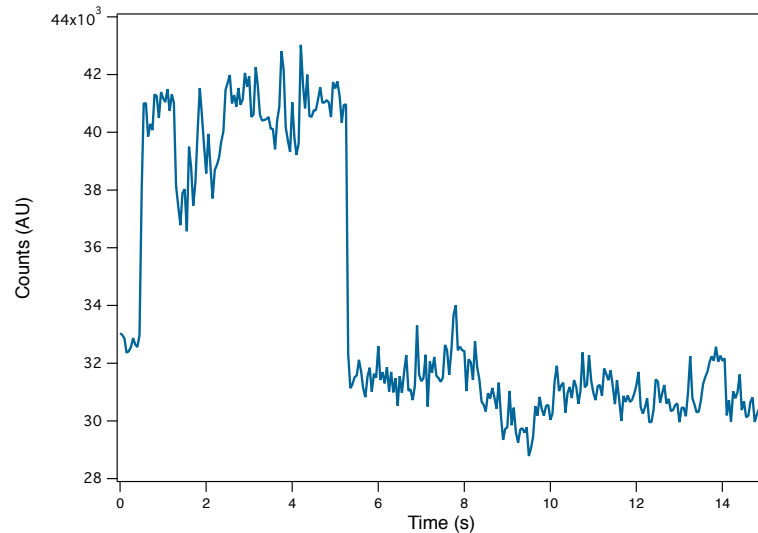


NK1 receptor (GPCR) labelled with Qdot 655  
(Life technologies) on 293T cells

Blinking occurs at every timescale



# Fundamentals: Photobleaching



Serotonin receptor labelled with a tris-NTA-Atto647N probe in 293T cells.

- A considerable amount of energy is flowing through single molecules. After a limited amount of time, they will undergo photodestruction.
- Most common mechanism: The molecule goes into the triplet state ( $S_1 \rightarrow T_1$ ) and then decays producing highly reactive singlet oxygen that will oxidize the fluorophore.
- Photobleaching quantum yields are typically in the order of  $10^{-5}$ - $10^{-6}$ .
- Photobleaching drastically reduces the measurement time.

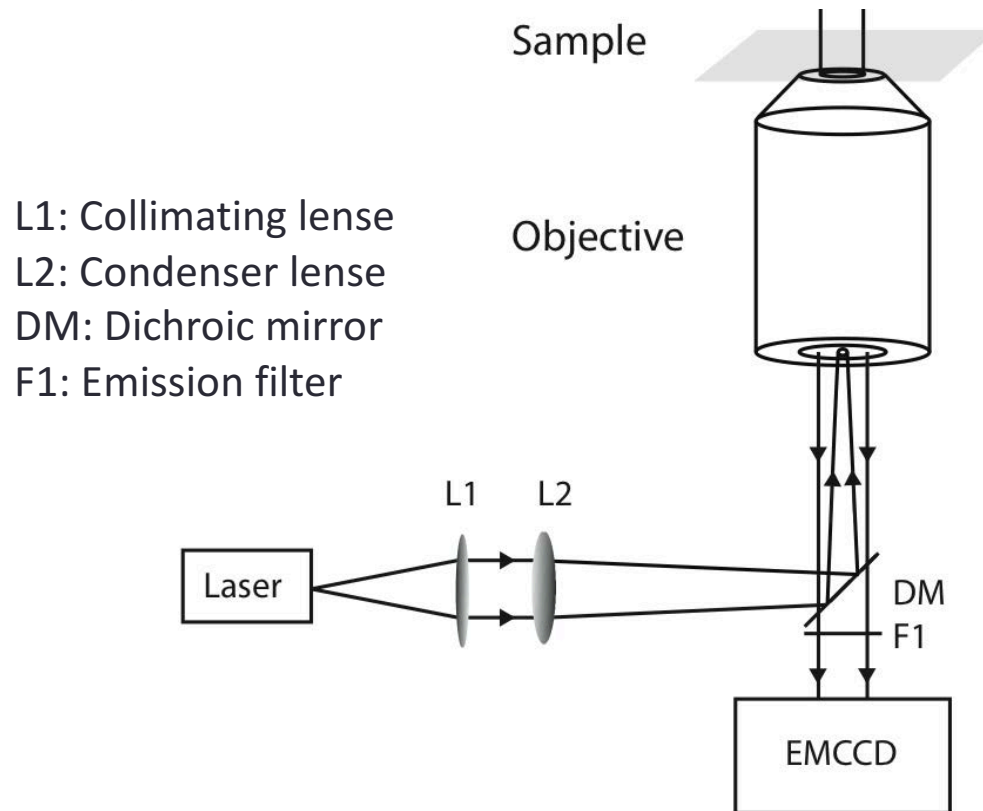
# Typical fluorophores

Fluorophore	$\lambda_{\text{exc}}$	$\lambda_{\text{em}}^{\text{max}}$	QE	$\tau_f$	$I_s$	$k_{\infty}$	$\tau_{\text{bl}}^{\infty}$	$N_{\text{max}}$	$\varepsilon$	Brightness
	(nm)	(nm)	(in H <sub>2</sub> O)	(ns)	(kW/cm <sup>2</sup> )	(kcnts/ms)	(ms)	(10 <sup>6</sup> photons)	(M <sup>-1</sup> cm <sup>-1</sup> )	Rel to EGFP
fluorescein	488	520	0.71	-	-	-	-	< 0.1	68000	146
TMR	514	580	0.28	2.1	5.6±1.6	4.0±1.	11.5±2.5	0.6±0.2	95000	81
Cy3	532	568	0.14	~1	-	-	-	-	150000	64
Cy5	630	670	0.18	~1	2.2±1.0	2.3±0.3	14.8±0.3	0.67±0.11	250000	136
Atto488	501	523	0.80	4	-	-	-	-	90000	218
Atto565	563	592	0.90	4	-	-	-	-	120000	327
STAR635	634	654	0.51	2.8	-	-	-	-	63000	97
QF640R	630	670	-	-	-	-	-	-	105000	295
Atto647N	644	669	0.65	3.5	-	-	-	-	150000	295
Alexa647	650	665	0.33	1	-	-	-	-	237000	237
ECFP	439	476	0.40	-	-	-	-	-	32500	39
mTurquoise	434	474	0.84	3.7	-	-	-	-	30000	76
EGFP	488	512	0.60	3.2	13±3	2.9±0.2	2.8±0.2	0.14±0.05	55000	100
EYFP	514	527	0.61	3.7	9±2	3.1±0.3	2.6±0.1	0.14±0.05	83400	154
mCitrine	516	529	0.76	-	-	-	-	-	77000	177
mCherry	587	610	0.22	1.46	-	-	-	-	72000	48
mPlum	590	649	0.10	~1	-	-	-	-	41000	12
PA-GFP d	400	515	0.13	-	-	-	-	-	20700	8
PA-GFP a	504	517	0.79	-	-	-	-	-	17400	42
PA-mCherry a	564	595	0.46	-	-	-	-	-	18000	25
Dronpa (G)	503	517	0.85	-	-	-	-	-	95000	245
mEOS2 (G)	506	519	0.74	-	-	-	-	-	56000	126
mEOS2 (R )	573	584	0.66	-	-	-	-	-	46000	92

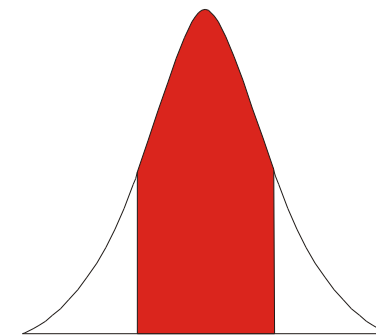
# Far-field microscopy imaging setups

# Set-up: Wide-field laser microscopy

- Illumination of a wide region using a laser (clean gaussian illumination).
- The polarization, the excitation intensity and the excitation wavelength are controlled.
- Detection using highly-sensitive CCD cameras.



Laser illumination:  
Truncated gaussian profile



Resolution:

$$r = 0.61 \frac{\lambda}{NA}$$

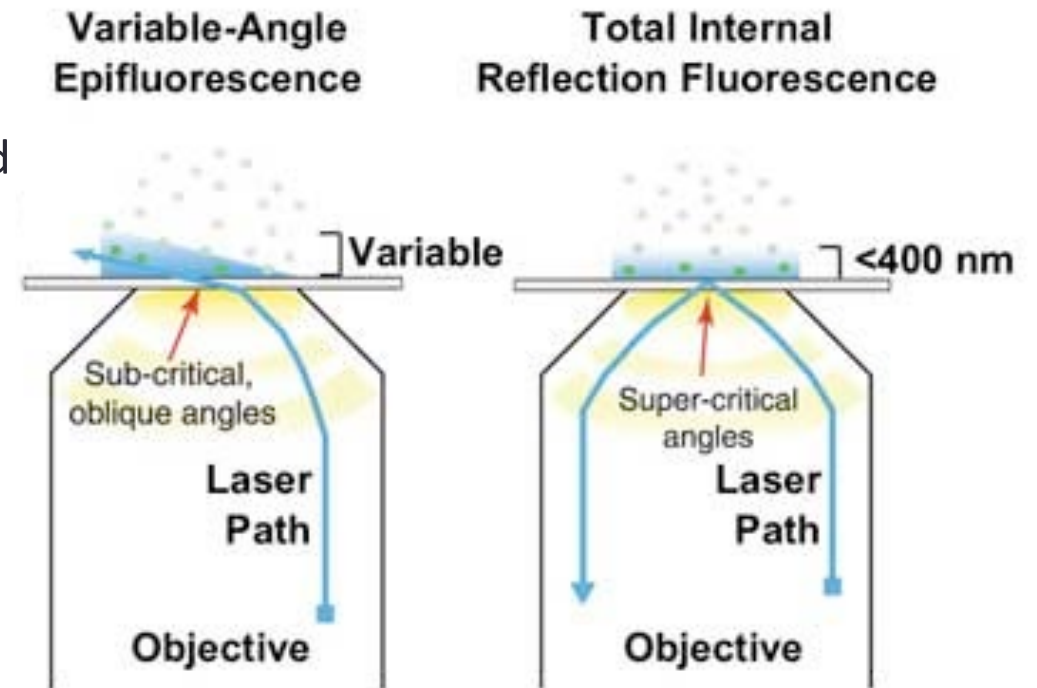
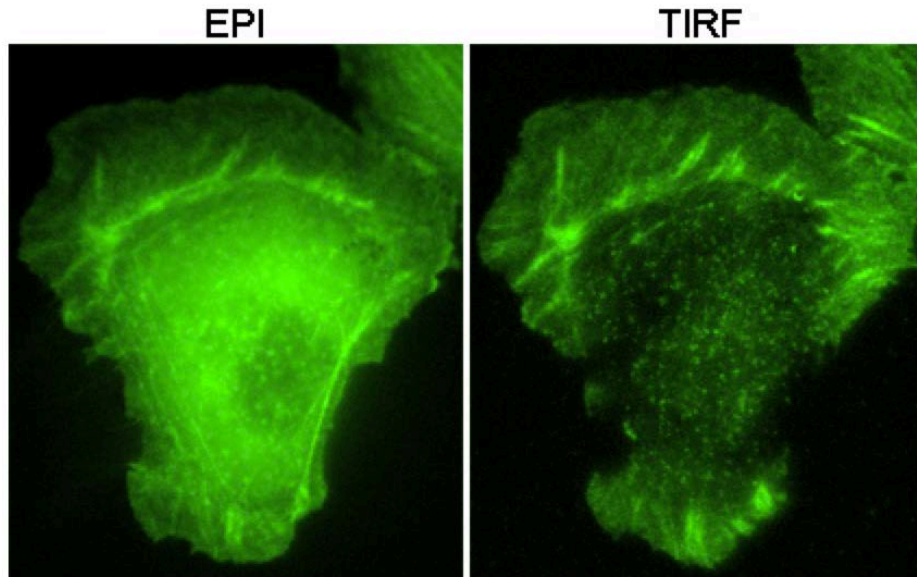
$$NA = n \cdot \sin \vartheta$$

$$\varnothing_{\text{illumination}} = \frac{f_{\text{objective}}}{f_{\text{condenser}}} \varnothing_{\text{aperture}}$$

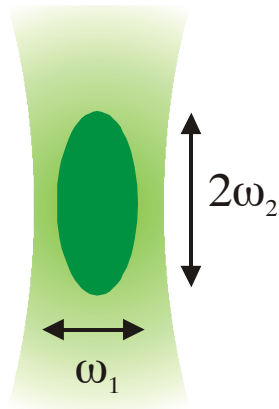
Resolution = capability to discriminate the light emitted by two different sources

# Set-up: Total-Internal Reflection Fluorescence (TIRF) Microscopy

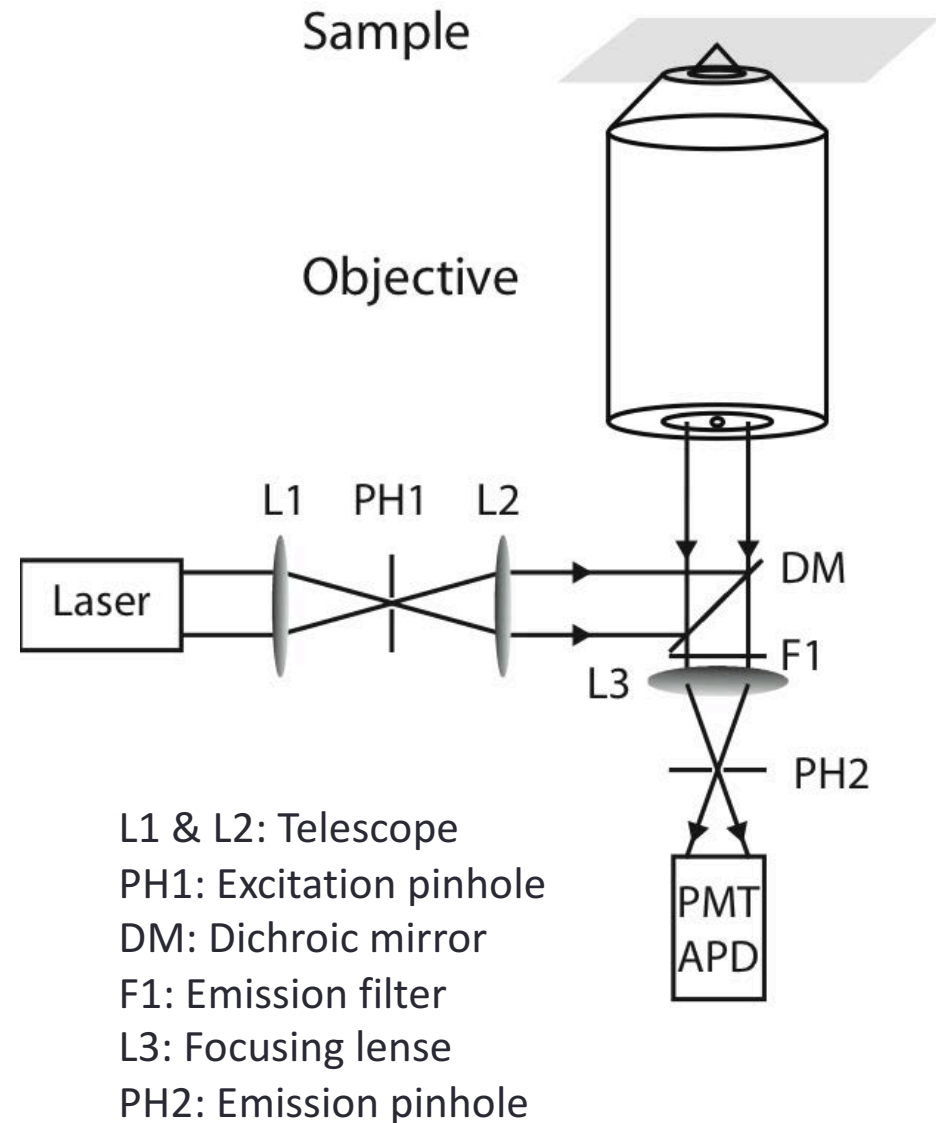
The illumination incident light is totally reflected  
-> An evanescent wave illuminate only a few  
hundreds on nanometer



# Set-up: Confocal laser scanning microscopy

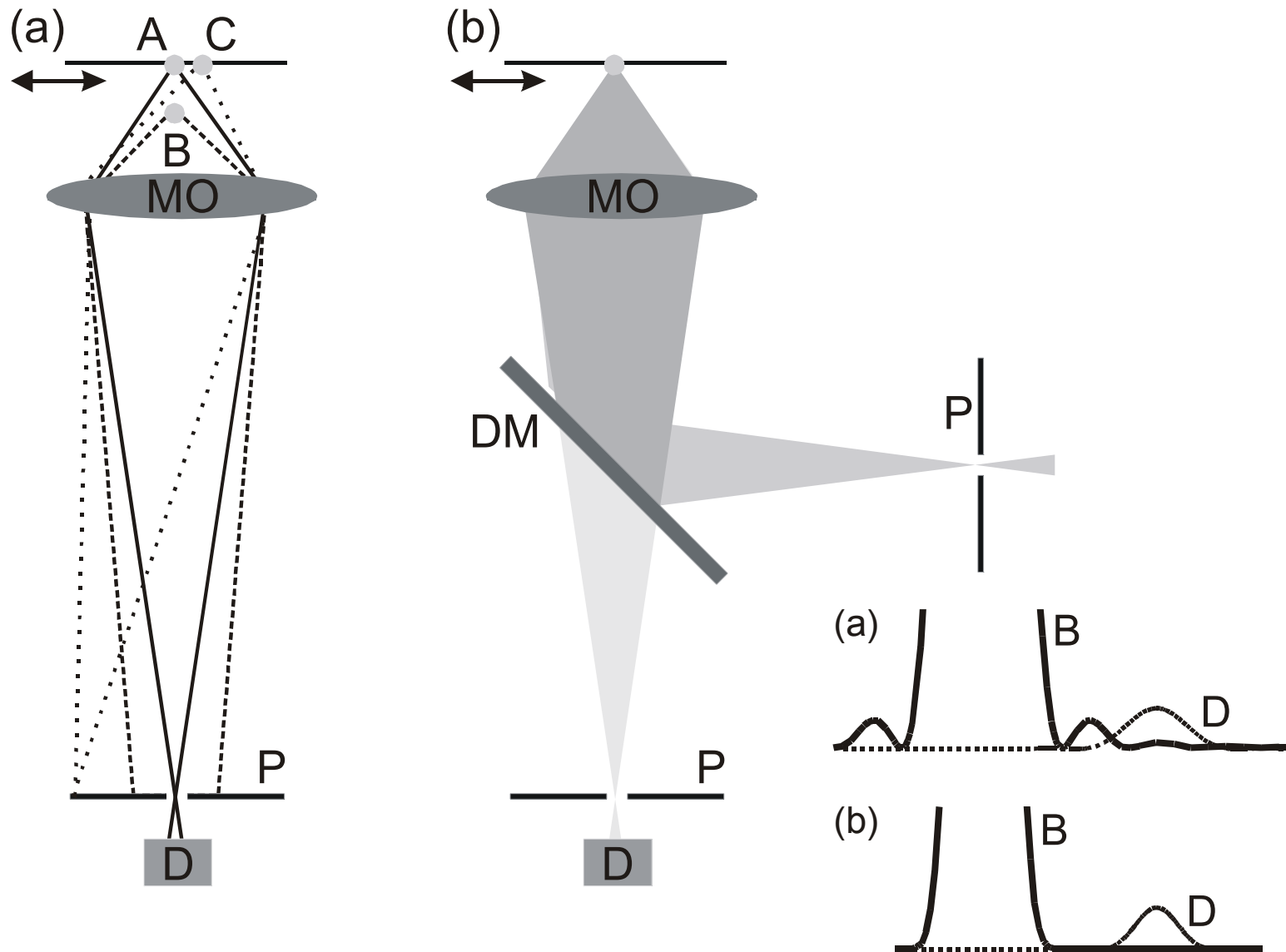


- Confocal illumination: Only a **small volume** (the confocal volume) is efficiently detected and illuminated.
- An image is obtained by **scanning** the sample and recording the fluorescence intensity as a function of the position.
- Slow measurement, high contrast
- Detection using highly-sensitive single-photon avalanche photo-diodes (APD).
- The fluorescence can be split into multiple components using cube polarizer or dichroic mirror.





## Set-up: Confocal laser scanning microscopy: principle

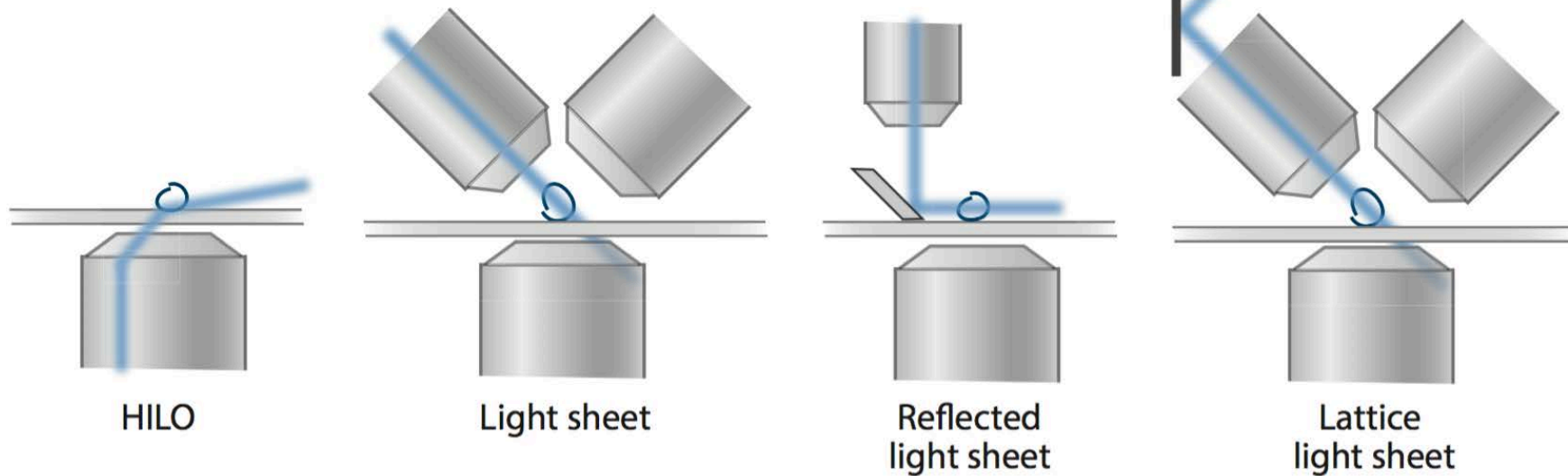


## Set-up: Light-sheet illumination

The sample is illuminated with a sheet of light.

-> Higher axial resolution

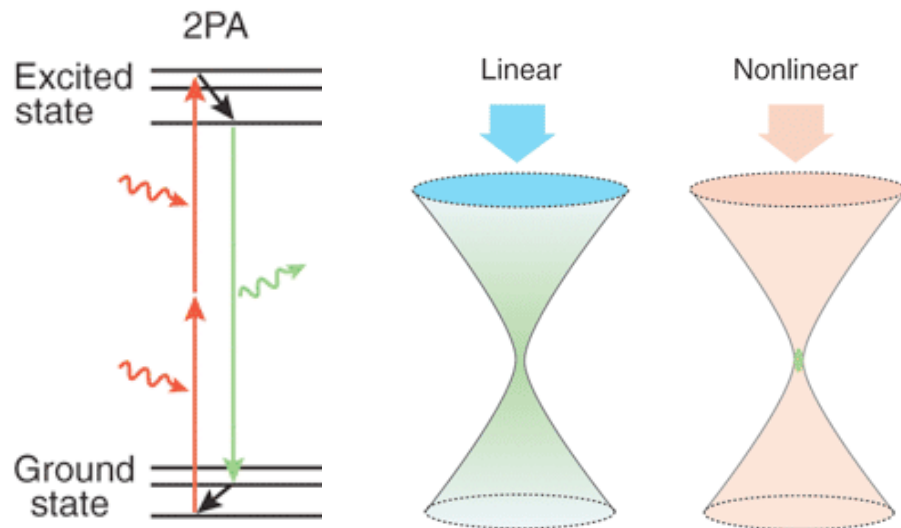
-> 3D imaging possible



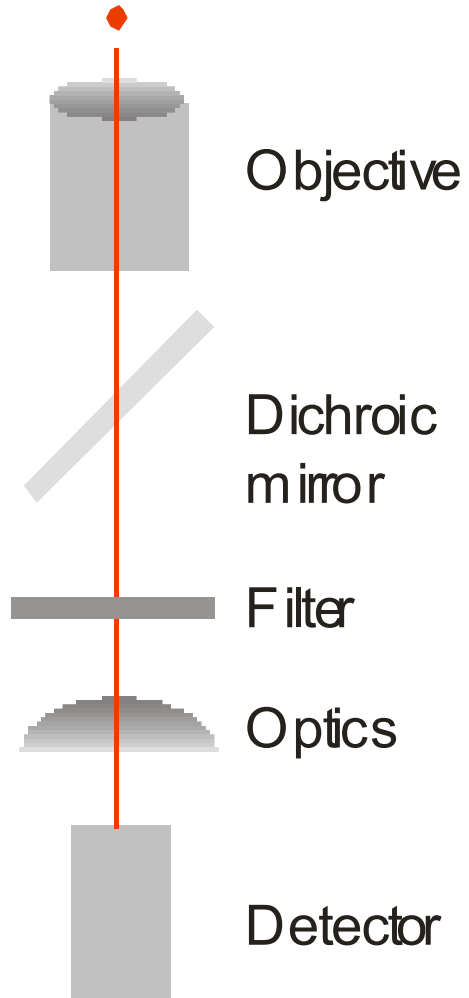
# Set-up: Two-photons microscopy

The fluorophore is excited by two consecutive photons of half of the electronic transition energy

- The photon density is sufficient only close to the focus
- Confocal-like excitation volume
- The scattering of the surrounding is lower at higher wavelength. The signal to noise is increased
- It is possible to measure deeper in tissues.



## Set-up: Detection efficiency



$$\eta_{\text{obj}} = 0.5 \cdot [1 - \sqrt{1 - (NA/n)^2}]$$

For NA=1.2 and n=1.33,  $\eta_{\text{obj}}$ =28%

But it depends on the orientation of the fluorophore

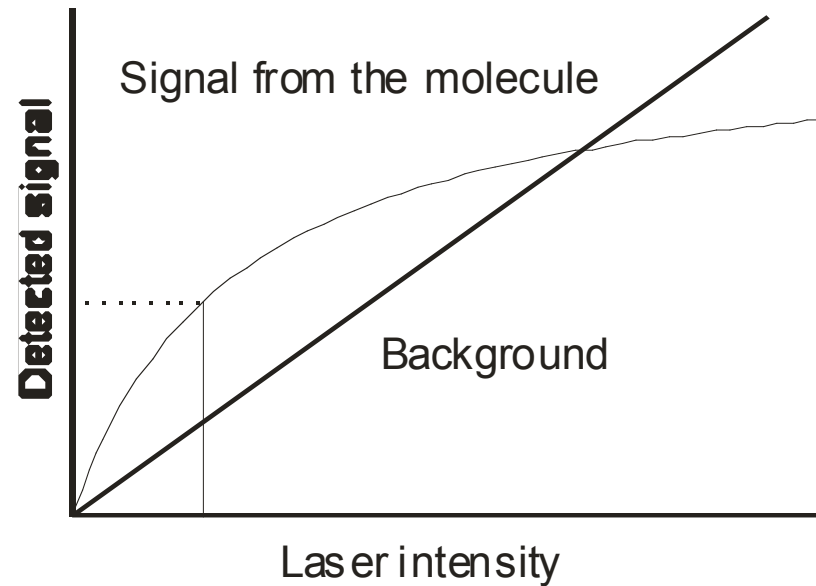
Filters and dichroics:  $\eta_{\text{fil}}$ =40%

Optics:  $\eta_{\text{opt}}$ =90%

Detector:  $\eta_{\text{det}}$ =50%

**In total:  $\eta_{\text{tot}}$ =5%**

## Set-up: Signal/noise ratio



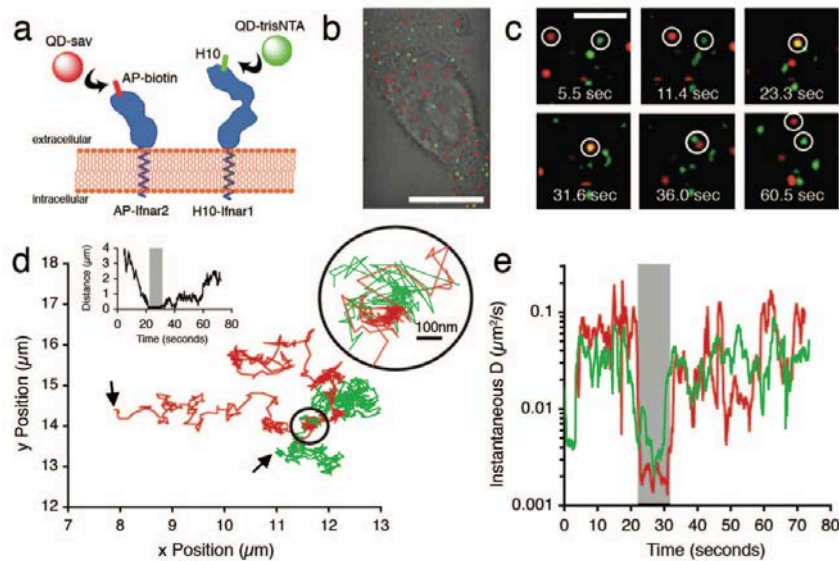
$$SNR = \frac{\eta_{\text{det}} RT_{\text{int}}}{\sqrt{\eta_{\text{det}} RT_{\text{int}} + C_b P T_{\text{int}} + N_d T_{\text{int}}}}$$

$T_{\text{int}}$ =integration time

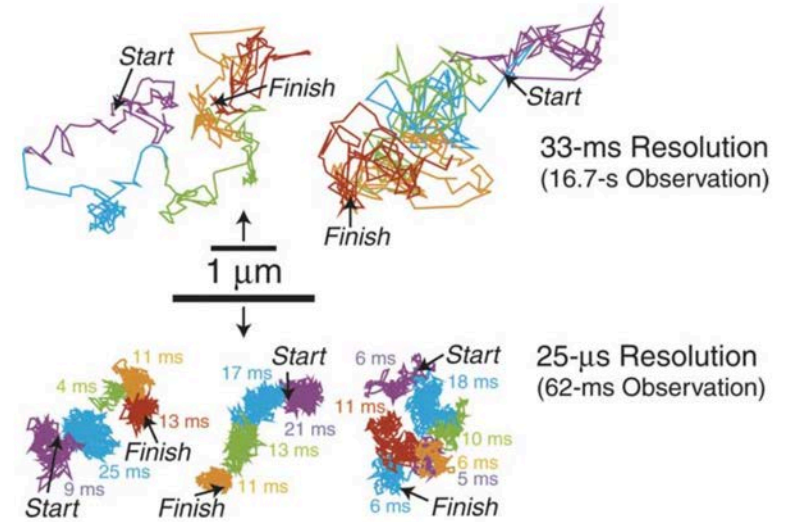
$C_b P$ =background

$N_d$ =noise from the detector

- The noise consists of the statistical noise of the signal, of the noise induced by the background and of the noise from the detector.
- The background has multiple origins: stray photons; autofluorescence from the filters and optics; impurities in the sample (cell autofluorescence).
- The minimal background is due to the Raman signal from the solvent.
- Practically: It is best to work slightly below  $I_{\text{sat}}$ . Reduce as much as possible the autofluorescence. Often 100-200 detected counts from the molecule are sufficient to get an SNR of 8-10. This typically represents 5-10 ms measurement time. The effective number of images that can be recorded depends on the photo-bleaching.

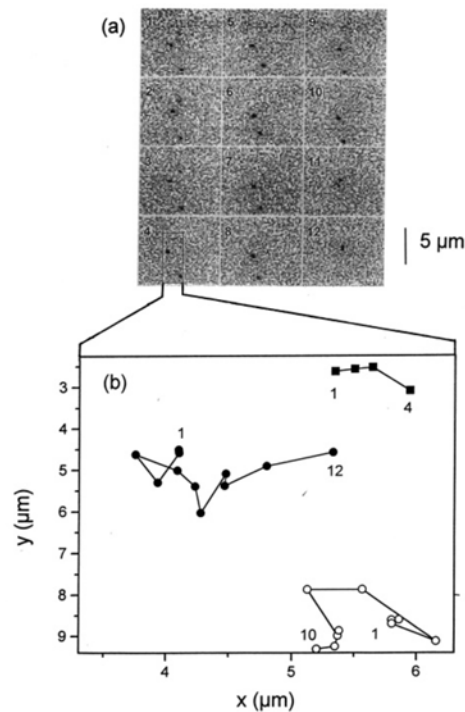


Roullier V et al. (2009) *Nano Lett*



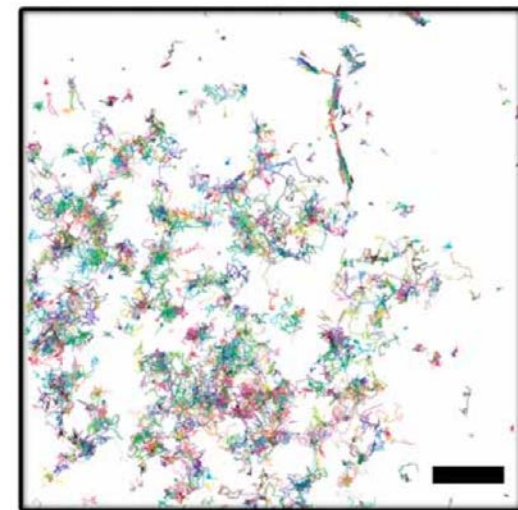
Kusumi A et al. (2005) *Semin Immunol* 17:3–21

## Single-molecule imaging and tracking



Schmidt T et al.(1995) *Journal of Physical Chemistry* 99:17662–17668

Manley S et al. (2008). *Nat Methods* 5:155–157

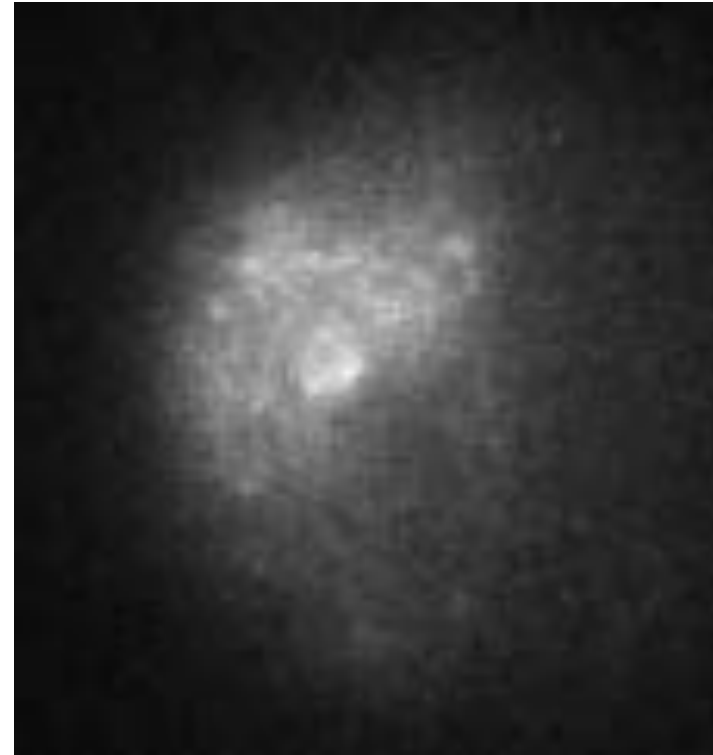




# How to be sure that these are single molecules?

## 1: Well characterize the system without single molecules

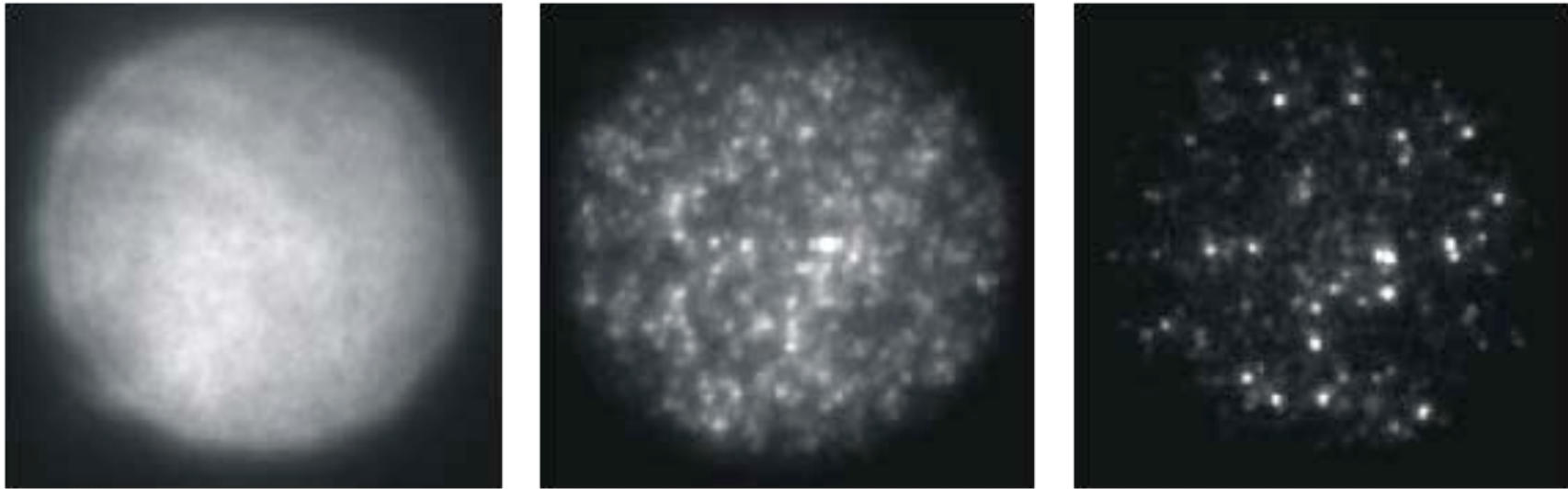
Cell autofluorescence



- Many biomolecules are fluorescent: flavines, NADH, FAD, chlorophyll.
- Cell autofluorescence is localized. Sometimes there is autofluorescence in the membrane. Most of all, the Golgi apparatus is usually very brilliant showing small vesicles. In general stressed cells are more autofluorescent.

=> **Only a detailed analysis of the autofluorescence allows unambiguous statements about single-molecule measurements.**

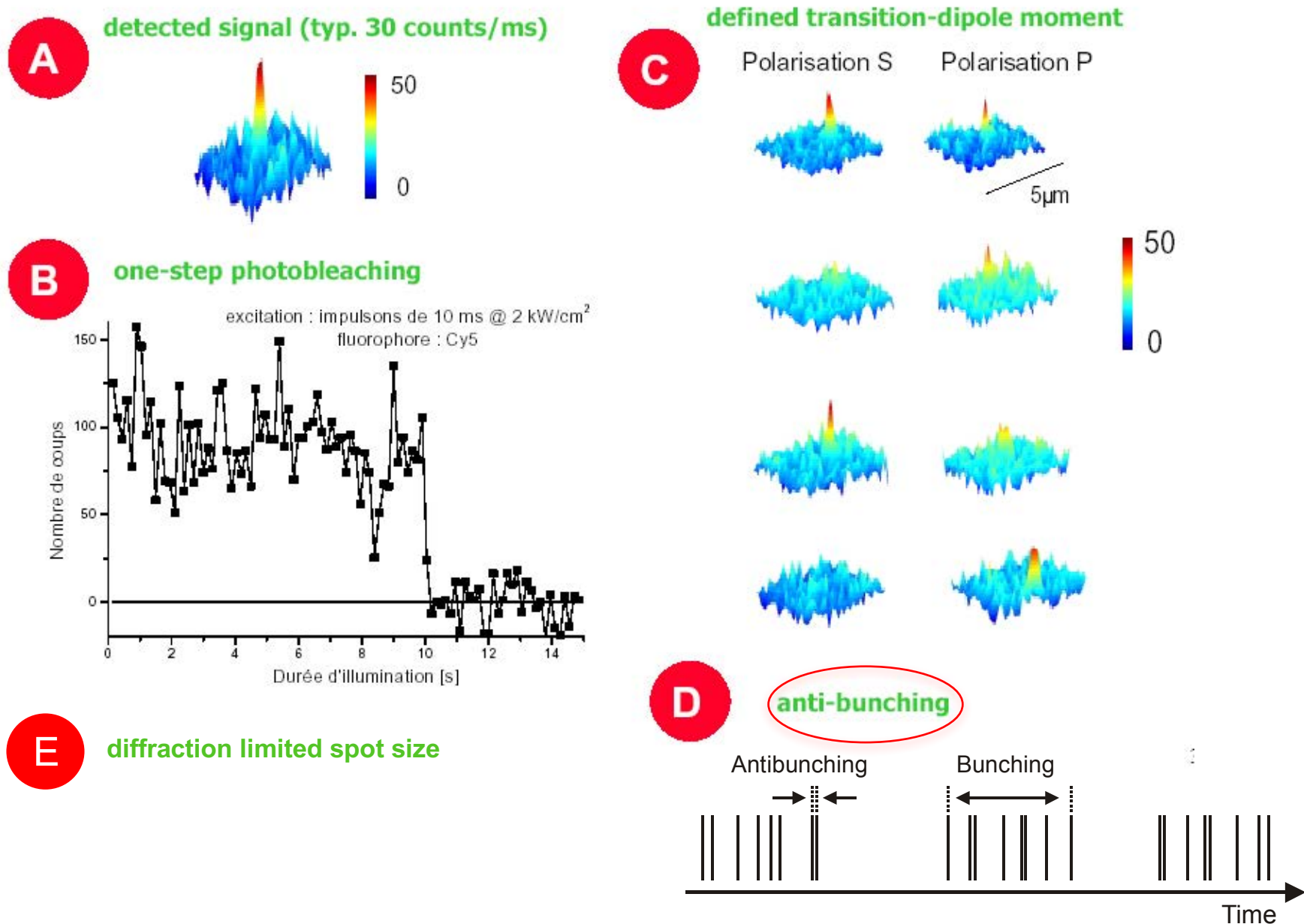
## 2: Careful control of the concentration



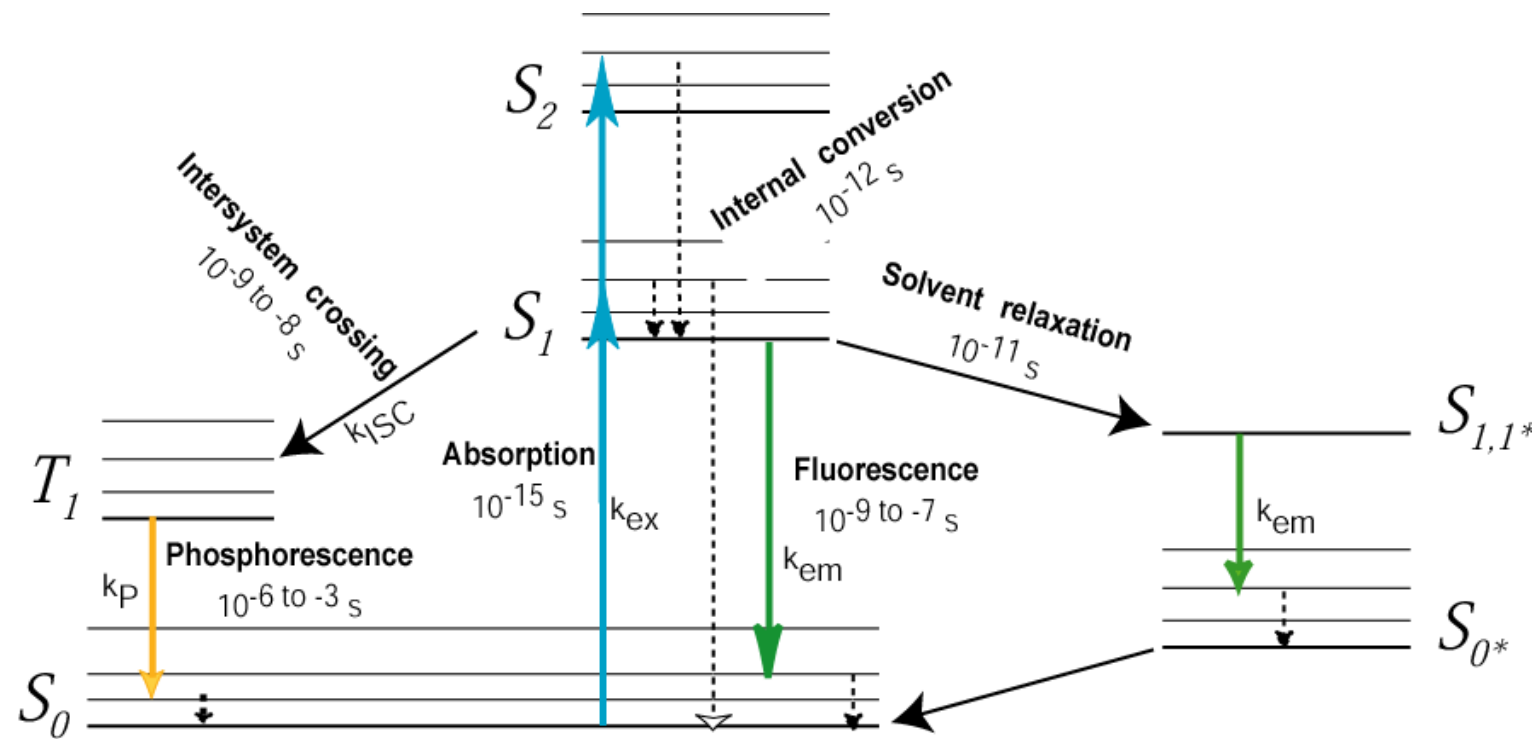
Concentration

- Molecules of a dye (Rhodamine 6G) diluted in a polymer (PVA).
- It is important to have full control on the concentration of the fluophores.

### 3: Detected molecules must exhibit several characteristic features of single molecules



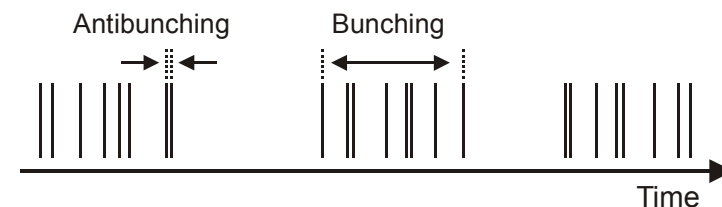
### 3: Detected molecules must exhibit several characteristic features of single molecules



**D**

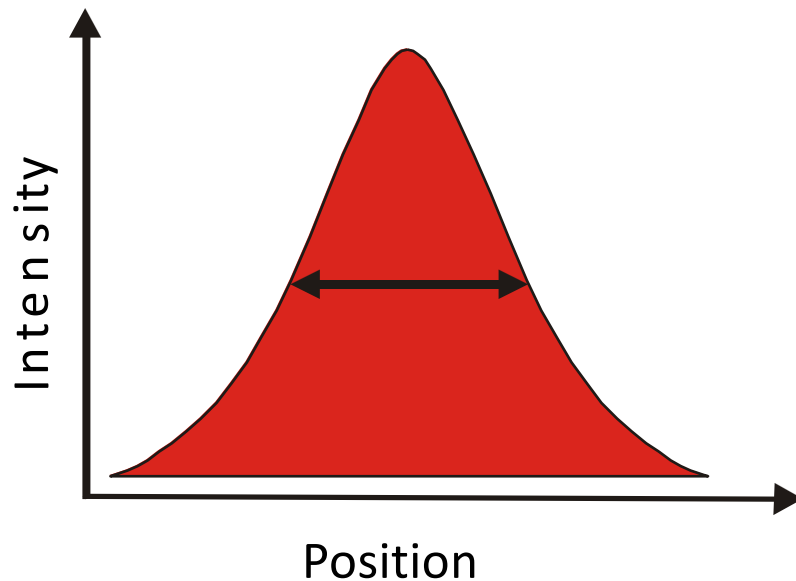
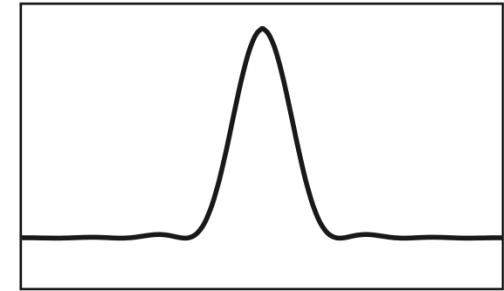
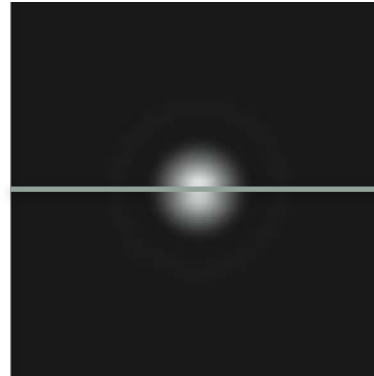
anti-bunching

Anti-bunching is the “absolute” proof of the presence of single-molecule



# Determination of the position of a single molecule

The size of the image of a single point photon emitter is limited by the diffraction

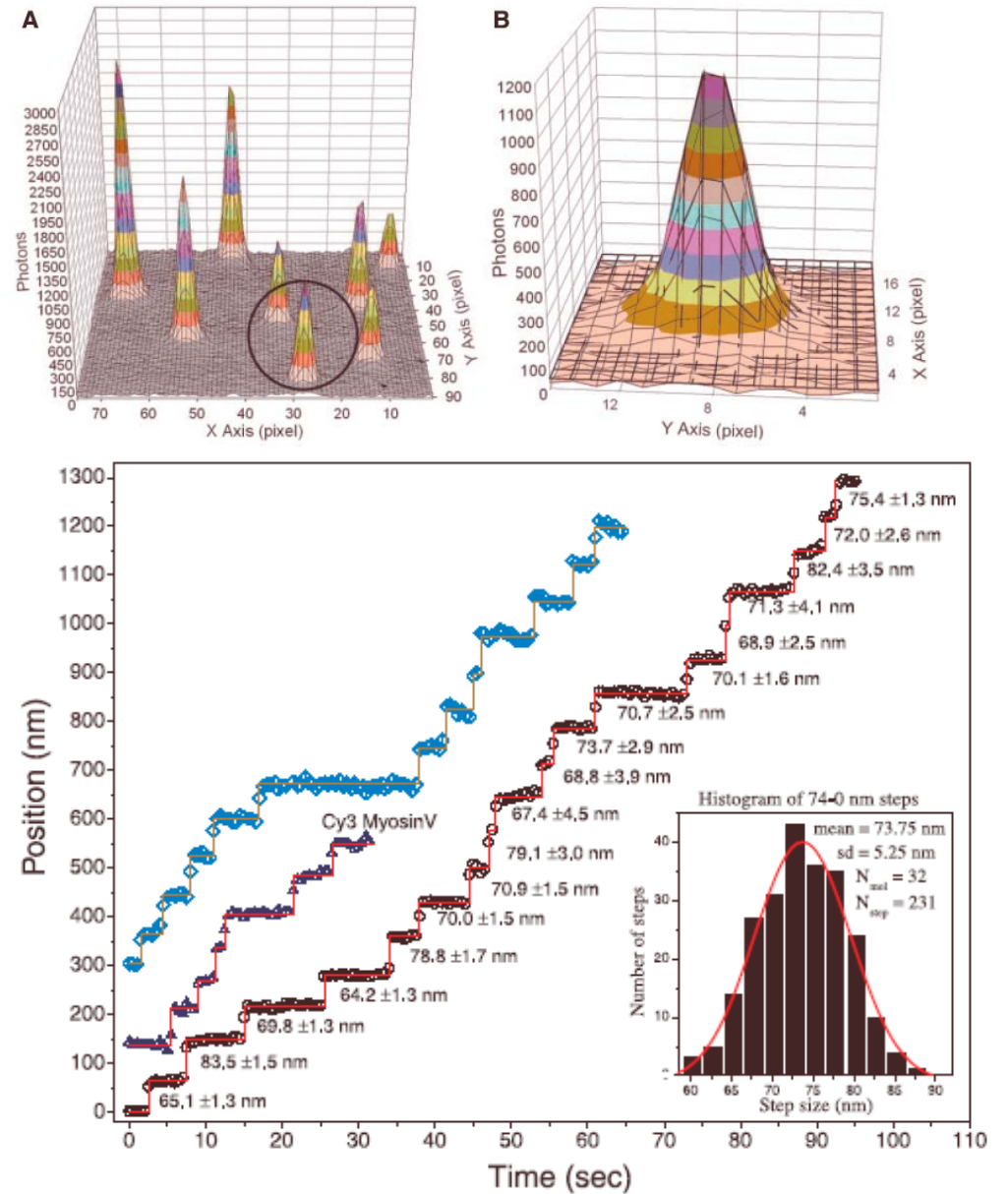
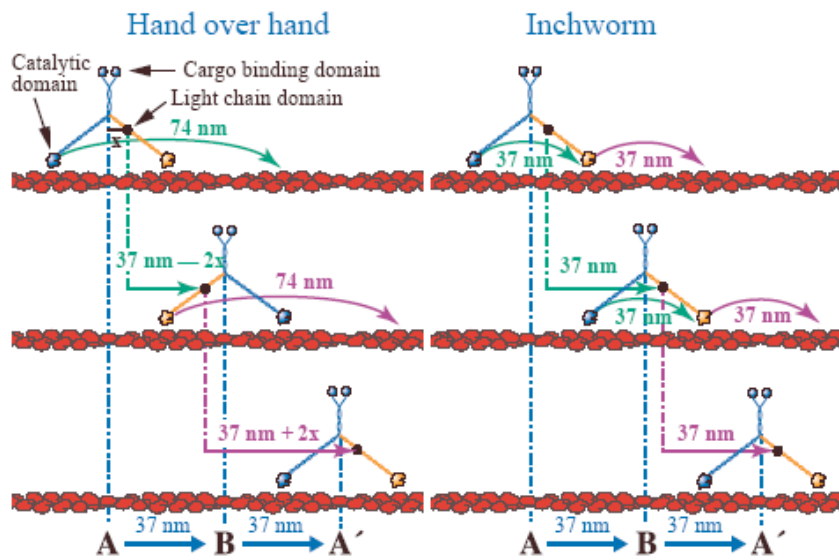
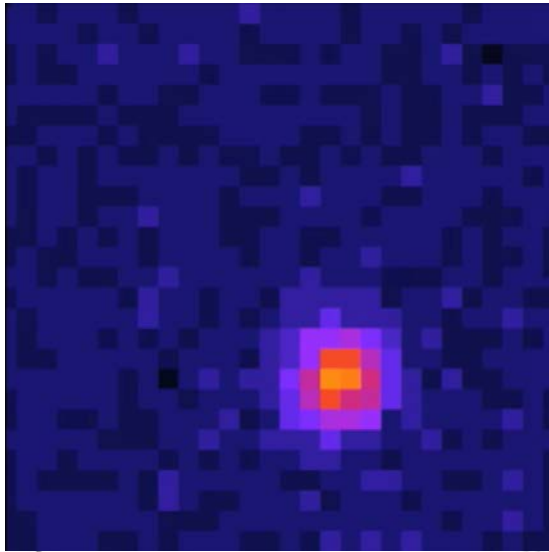


- The image of a single molecule on the camera can be very well approximated by a gaussian.
- The width of the gaussian is given by the resolution ( $\sim 0.5 \cdot \lambda$ )
- The precision depends on multiple factors:

$$\sigma \approx \sqrt{\frac{s^2 + (a^2/12)}{N} + \frac{4\sqrt{\pi s^3 b^2}}{aN^2}},$$

The experimental precision is a few tens of nanometer :  
50 nm (fluorophore), 30 nm (organic dyes) and 5 nm (quantum dots)

## Example: The motion of the molecular motor myosin V

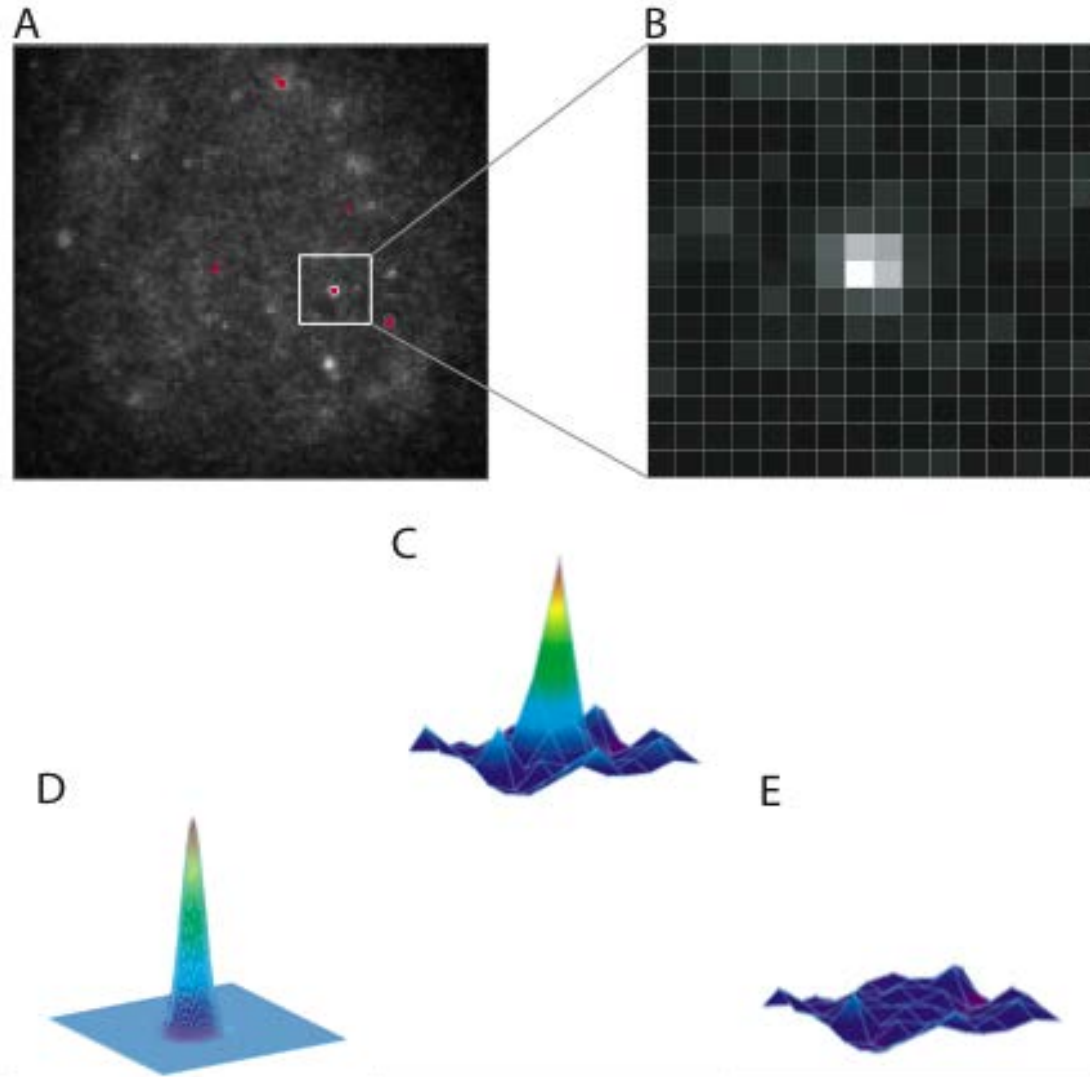


A. Yildiz, J.N. Forkey, S.A. McKinney, T. Ha, Y.E. Goldman, P.R. Selvin, *Science* **300**, 2061 (2003)

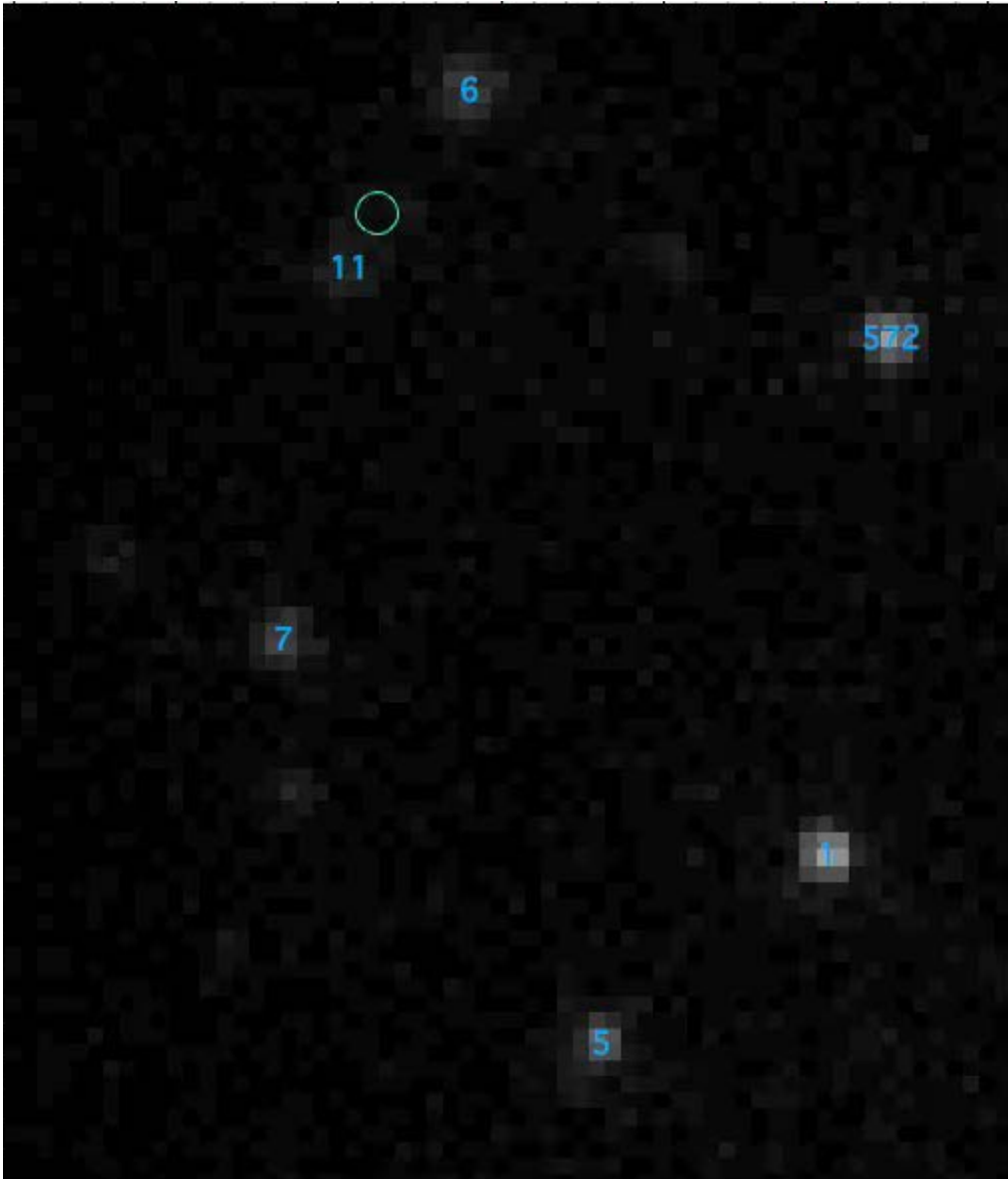


# Single-molecule tracking fluorescent peaks

- In a second step, single-molecule images are fitted using a two-dimensional gaussian.



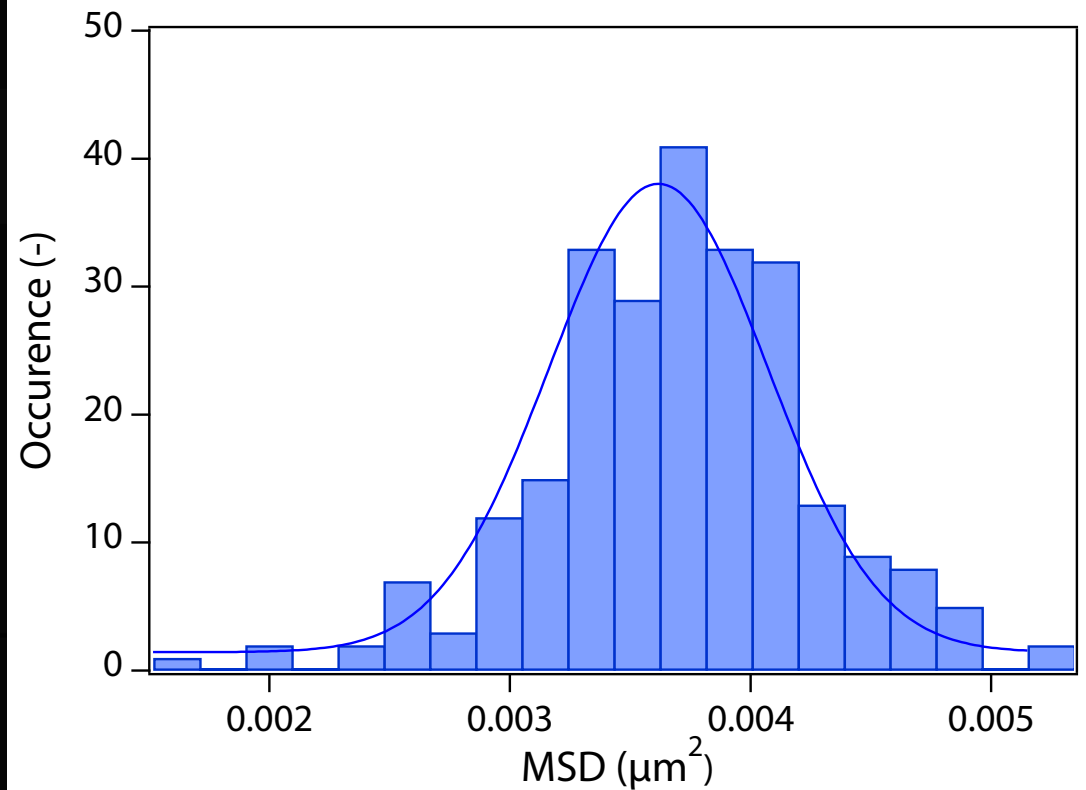
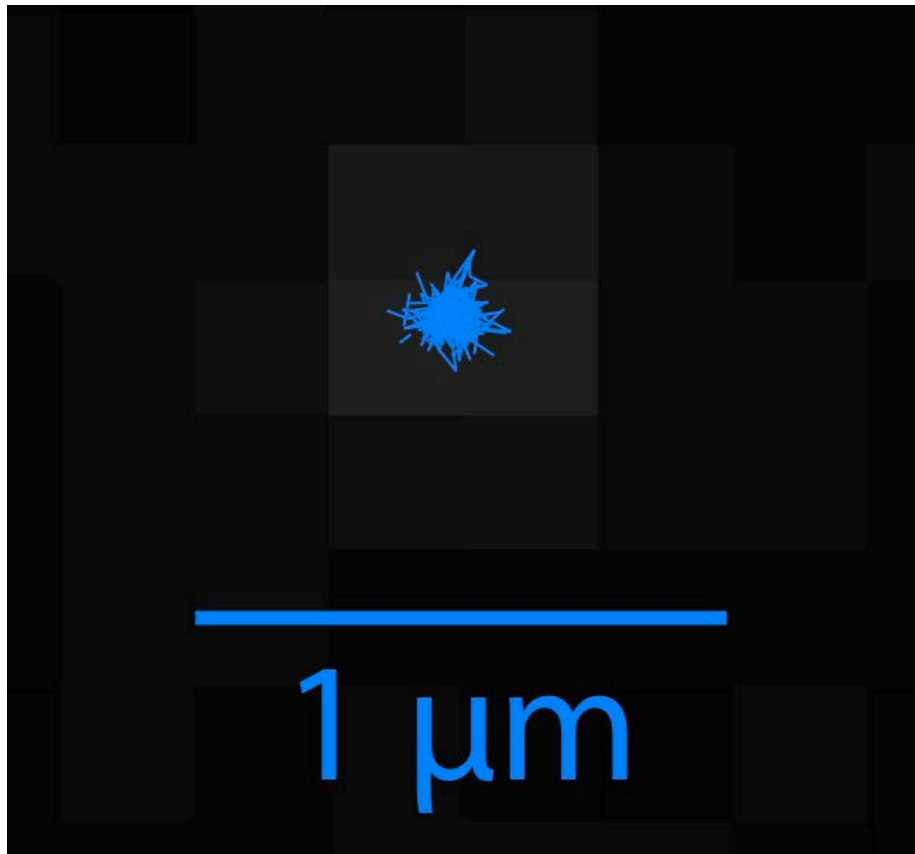
# Single-molecule tracking movie



1. Localization of every single molecule in a movie
2. Test of single molecule properties
3. Tracking peaks along the movie: trajectories extraction
4. Trajectories control
5. Diffusion parameter computation

# Single-molecule tracking noise

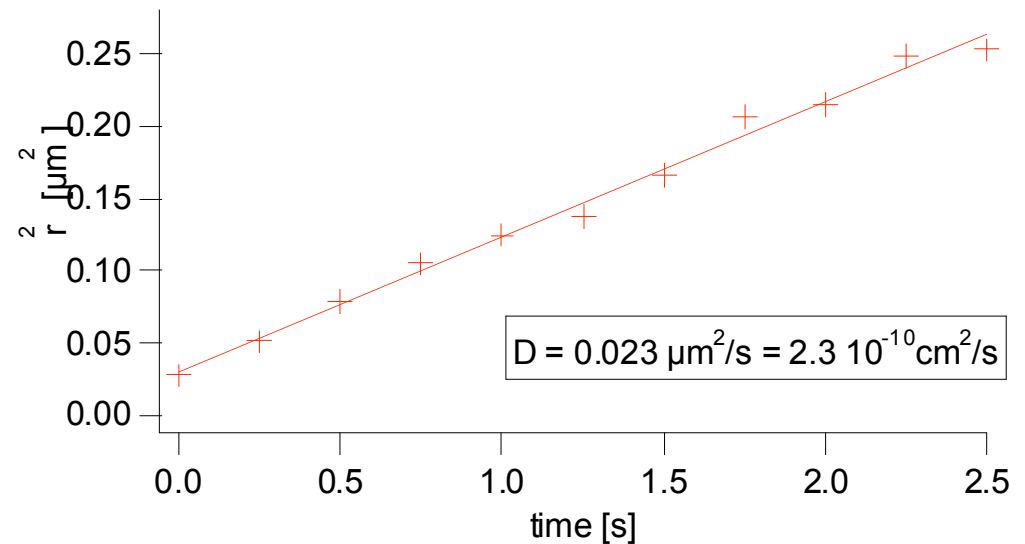
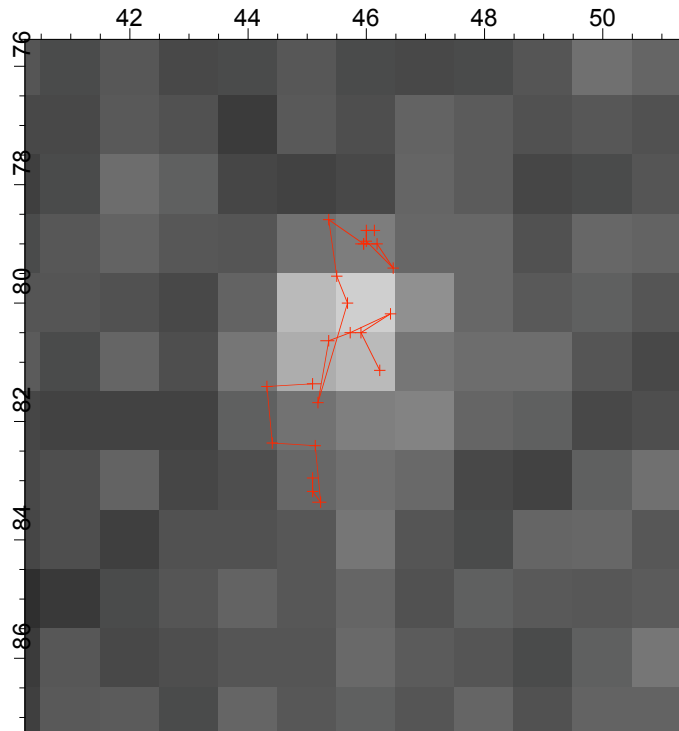
Due to noise, even an immobilized molecule will show an apparent displacement.



Localization accuracy **30 nm**

# Single-molecule tracking

The mean square displacement (*MSD*) is calculated from the extracted trajectories



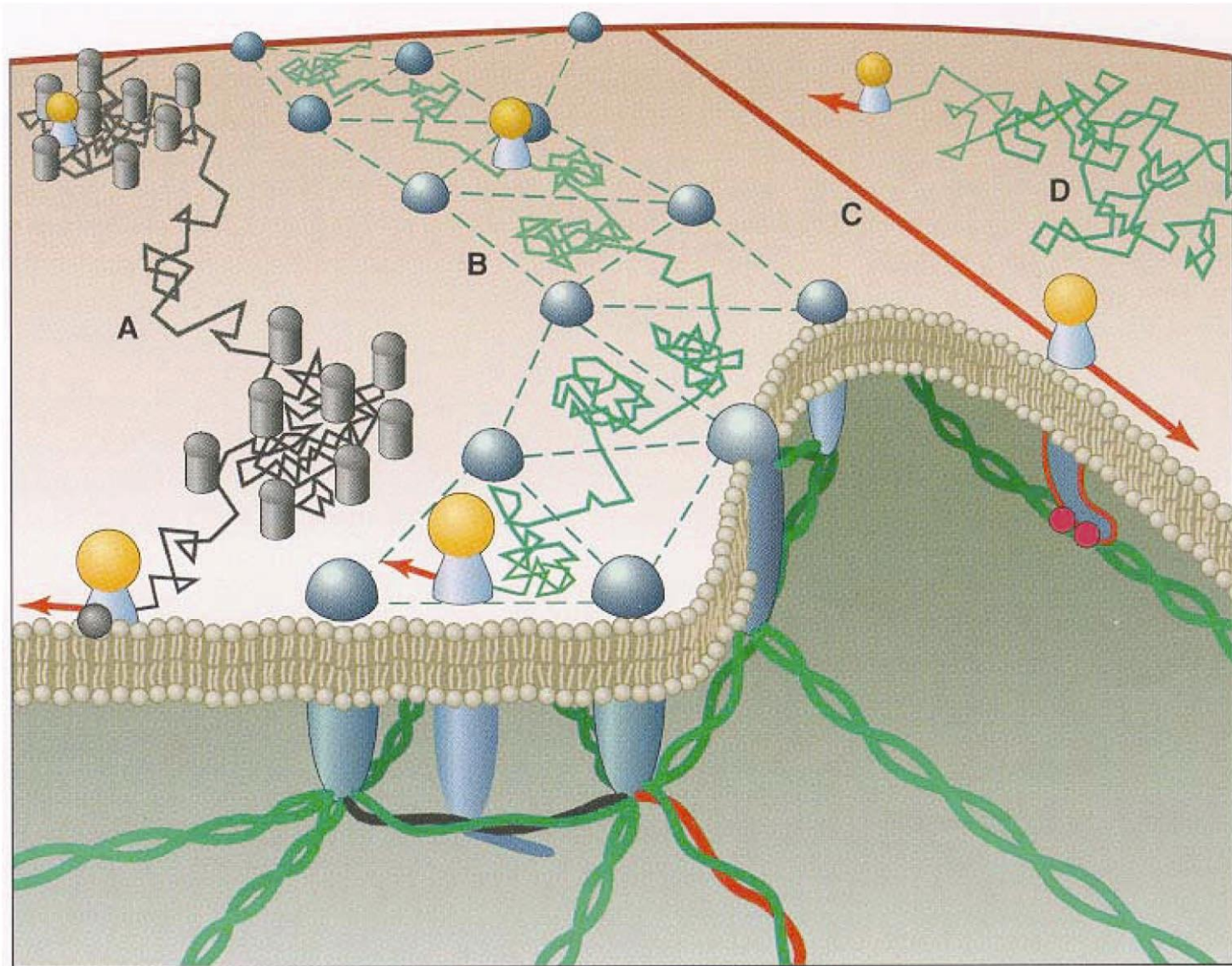
$$\text{MSD}(n\delta t) = \frac{1}{N-1-n} \sum_{j=1}^{N-1-n} \{ [x(j\delta t + n\delta t) - x(j\delta t)]^2 + [y(j\delta t + n\delta t) - y(j\delta t)]^2 \},$$

$$\text{MSD}(\tau) = 4D\tau$$

With *MSD*: mean square displacement, *D* diffusion coefficient,  $t=n\delta t$  time, *N* total # of measurements

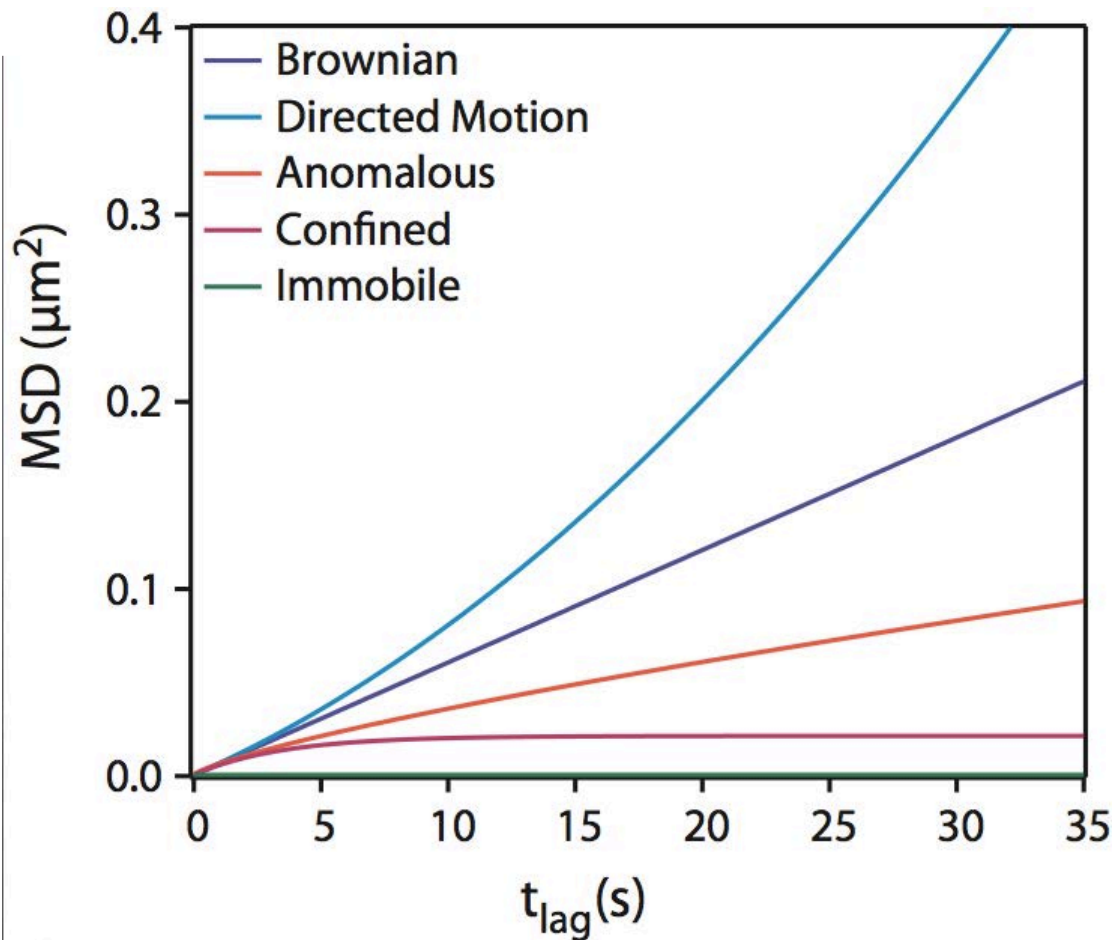
## Single-molecule tracking 4

- Examples of trajectories: (A) Diffusion with obstacles, (B) Diffusion within corrals, (C) Directed motion, (D) Brownian motion



## Single-molecule tracking 6

- In case of non-Brownian diffusion, *MSD* deviates from a linear relationship.
- MSD of a free-diffusing molecule (Brownian motion) is linear with time



$$\text{MSD}(t_{\text{lag}}) = 4 \cdot D_0 \cdot t_{\text{lag}}$$

$$\text{MSD}(t_{\text{lag}}) = 4Dt_{\text{lag}} + (vt_{\text{lag}})^2$$

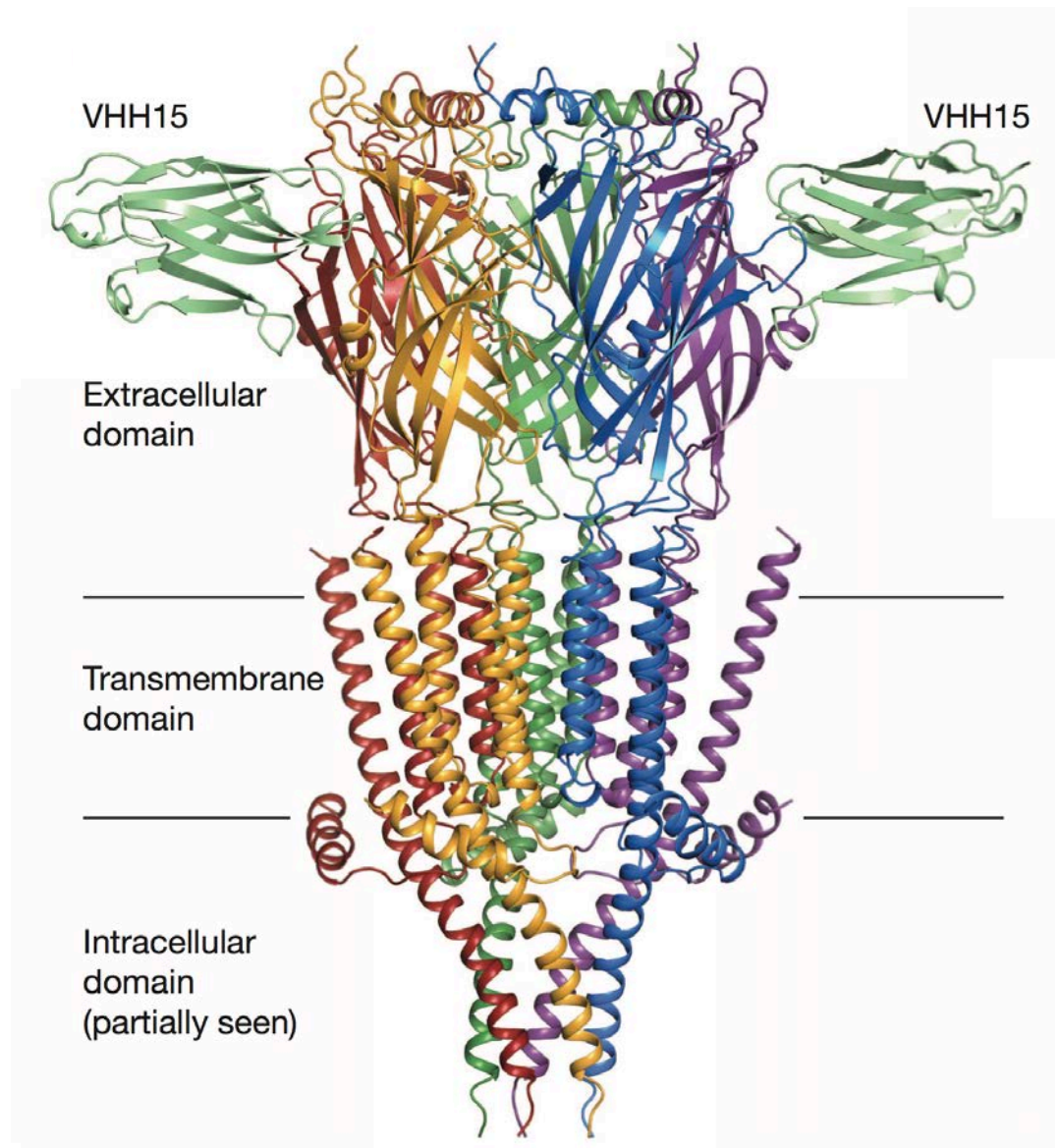
$$\text{MSD}(t_{\text{lag}}) = 4Dt_{\text{lag}}^\alpha$$

$$\text{MSD}(t_{\text{lag}}) = \frac{L_c^2}{3} \cdot \left( 1 - \exp\left(\frac{-12 \cdot D_0 \cdot t_{\text{lag}}}{L_c^2}\right) \right)$$

$$\text{noise} = 4Dt_{\text{aq}} + 2\sigma^2$$



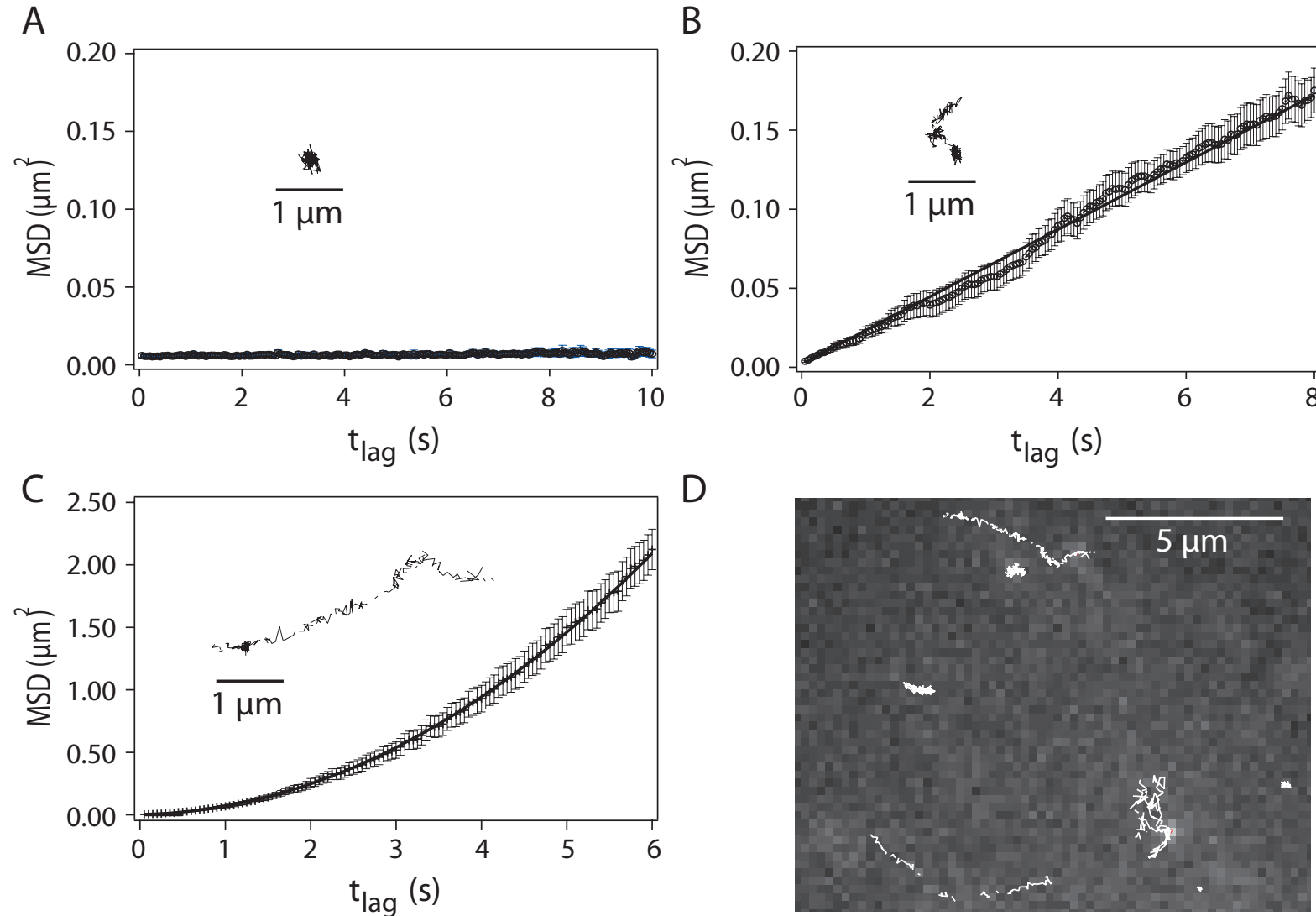
Example:  
Diffusion of 5HT<sub>3A</sub> receptor



Hassaïne G, Deluz C. et al. (2014) *Nature* 512:276–281

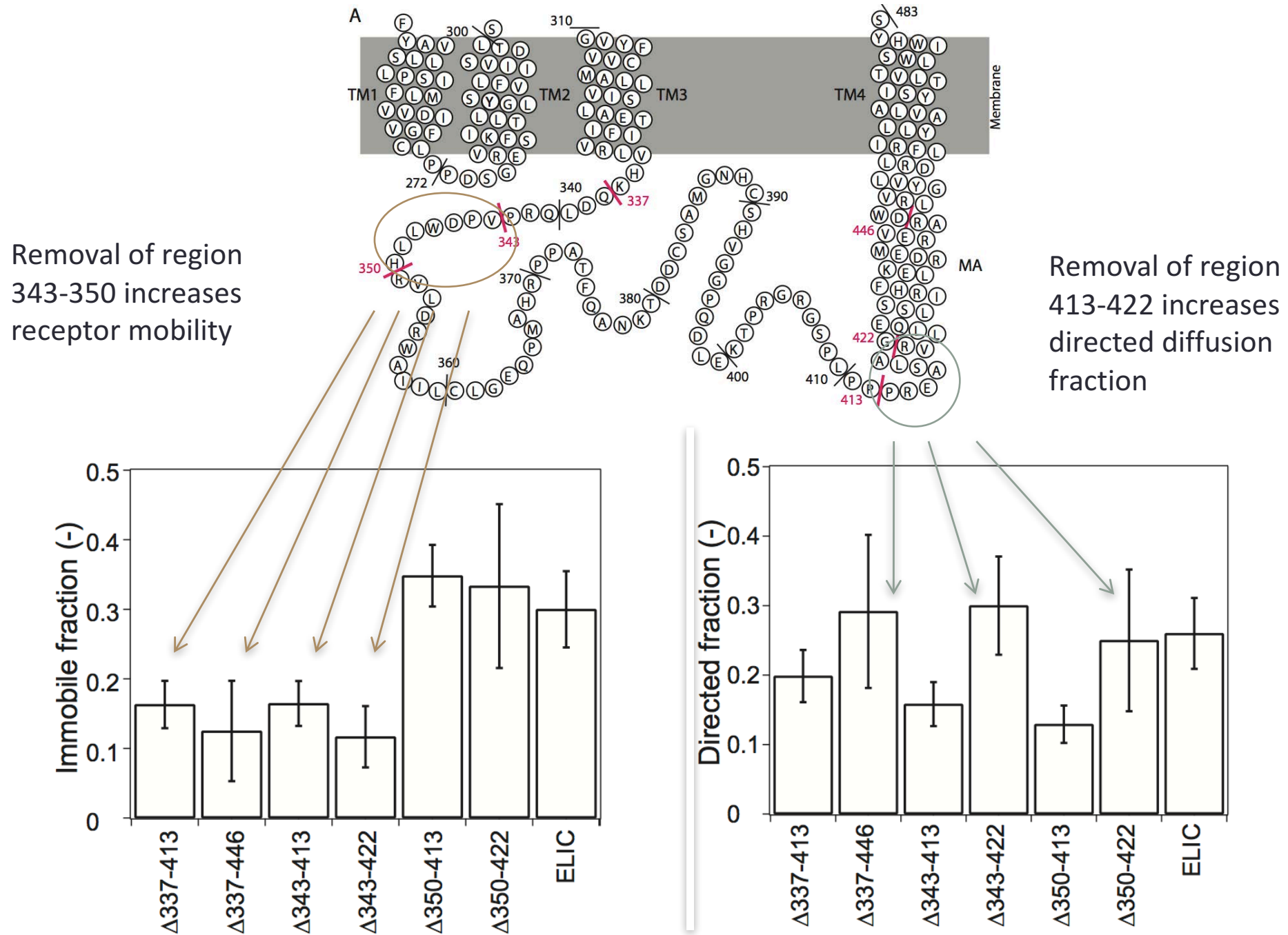
# Single-molecule tracking 7: Diffusion 5HT<sub>3A</sub> receptor

Three modes of diffusion observed on each cell:



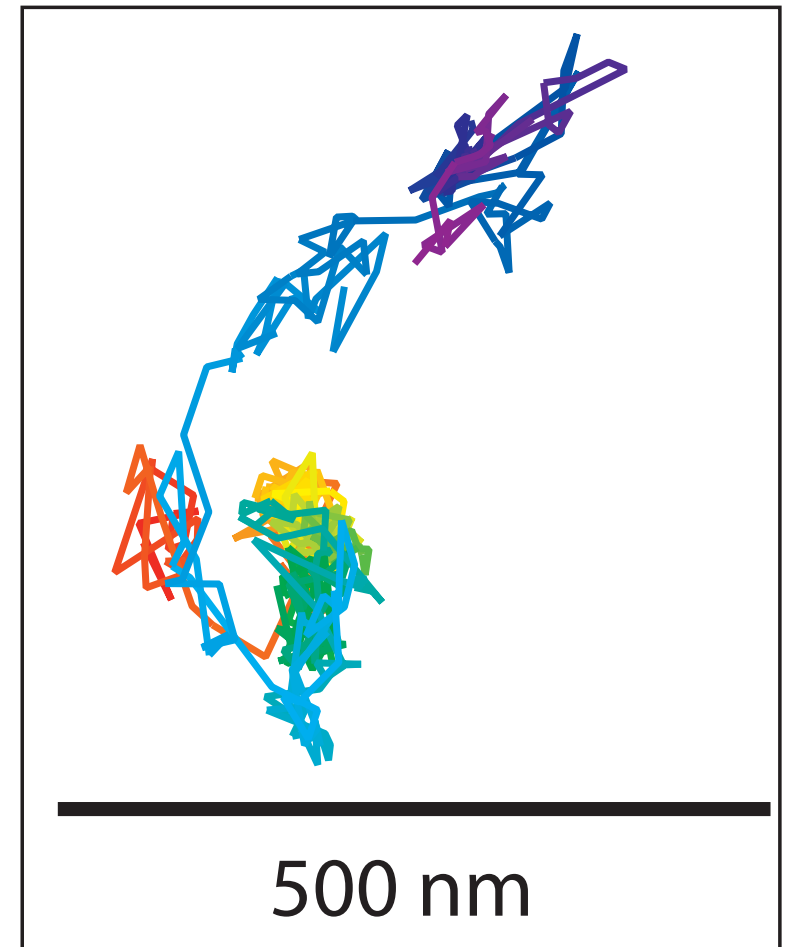
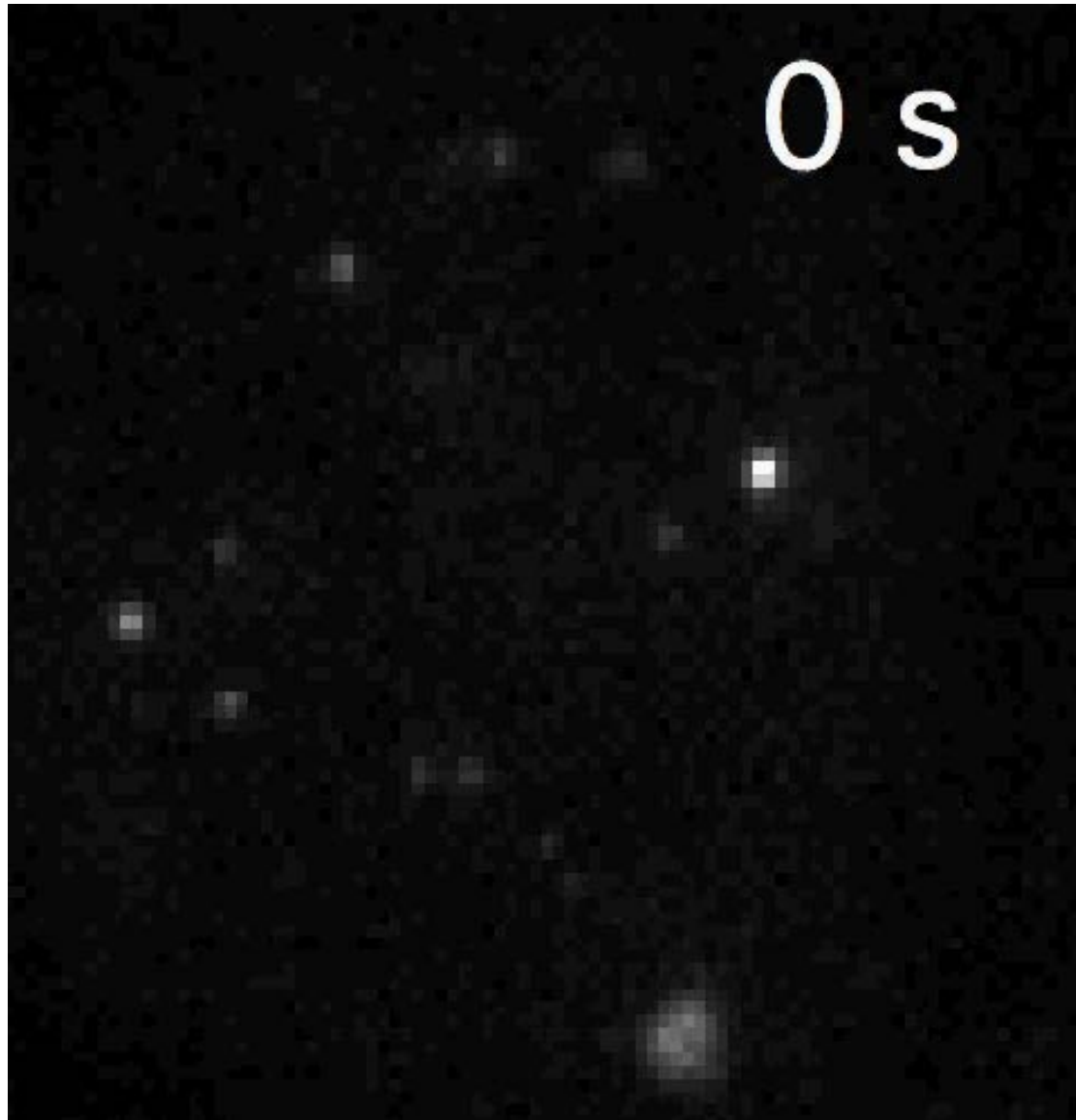


# Single-molecule tracking 8: Diffusion of modified 5HT<sub>3A</sub> receptor



## Single-molecule tracking 13

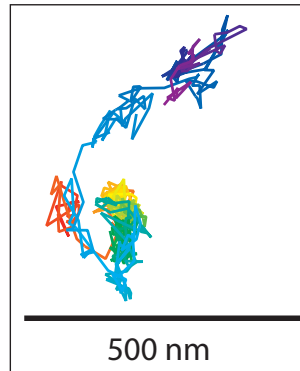
Changes of the diffusion behaviour within a trajectory. Self-similarity analysis



# Single-molecule tracking 14

Changes of the diffusion behaviour within a trajectory. Self-similarity analysis

A



## Data available:

Trajectory

MSD(t)

Instantaneous D

MSS analysis

Trajectory segment categorization

Moment scaling spectrum analysis give directly the diffusion type of a molecule or a fraction of a molecule trajectory.

MSS = 0.5 -> Free diffusion

MSS > 0.5 -> Directed diffusion

MSS < 0.5 -> Restricted motion

MSS = 0 -> Immobile

# Single-molecule tracking 15: multiparameter analysis

Using trajectory shape, size, velocity, symmetry to increase information content of single molecules

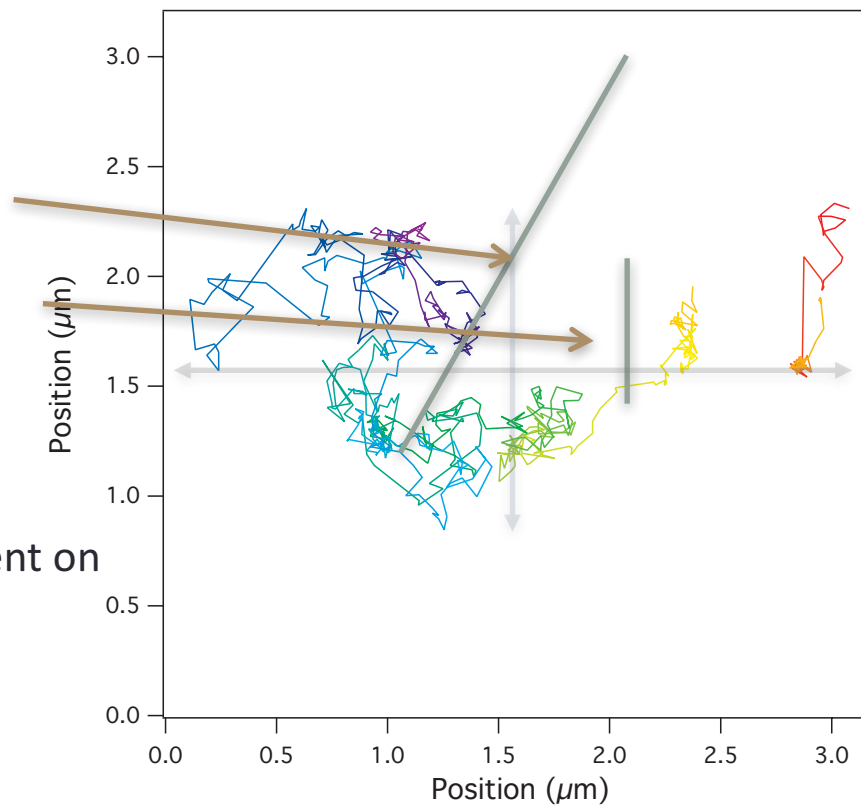
## Basic information

### 1. Net displacement

- Complete trajectory
- Segment of trajectory

### 2. Efficiency:

- Ratio of net displacement on sum of all single steps

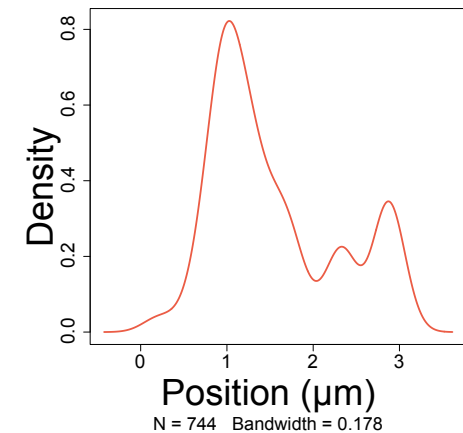


## Shape related information

### 3. Asymmetry

- Aspect ratio of the trajectory
- 0.254  $\rightarrow$  Brownian motion

## Distribution along main axis



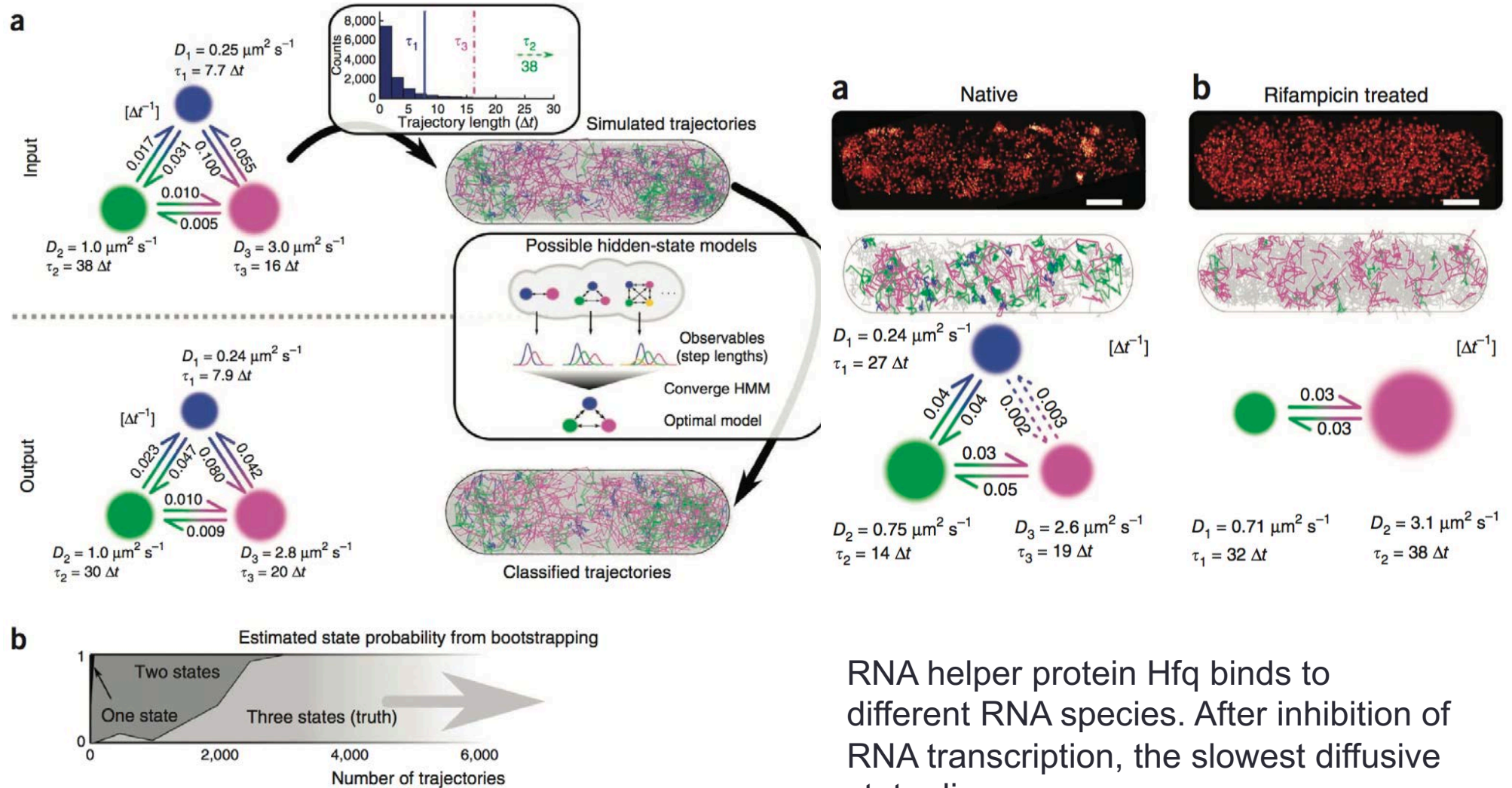
### 4. Skewness

### 5. Kurtosis

### 6. Length of displacement

# Single-molecule tracking 16: Subdiffusive states

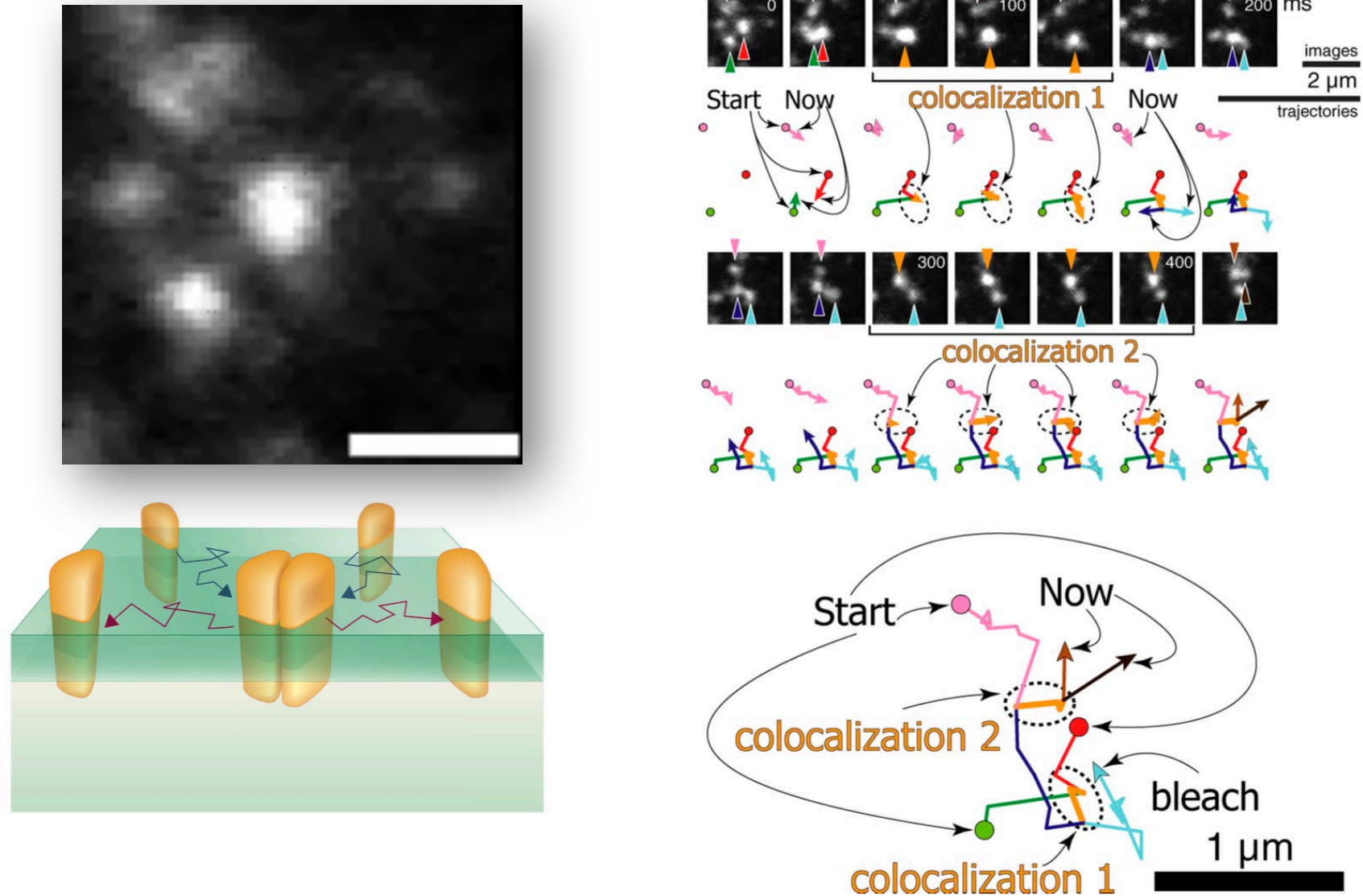
Variational Bayes SPT (vbSPT) allows to extract multiple unknown subdiffusive states





# Single-molecule tracking 17: Interactions

## Diffusion of N-formyl peptide receptor in CHO cells

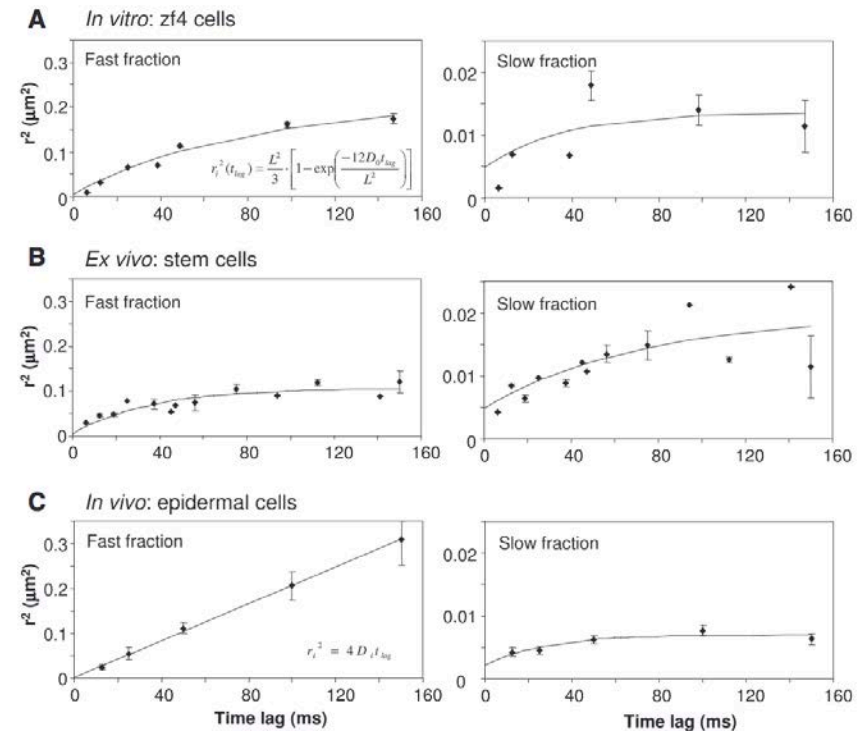
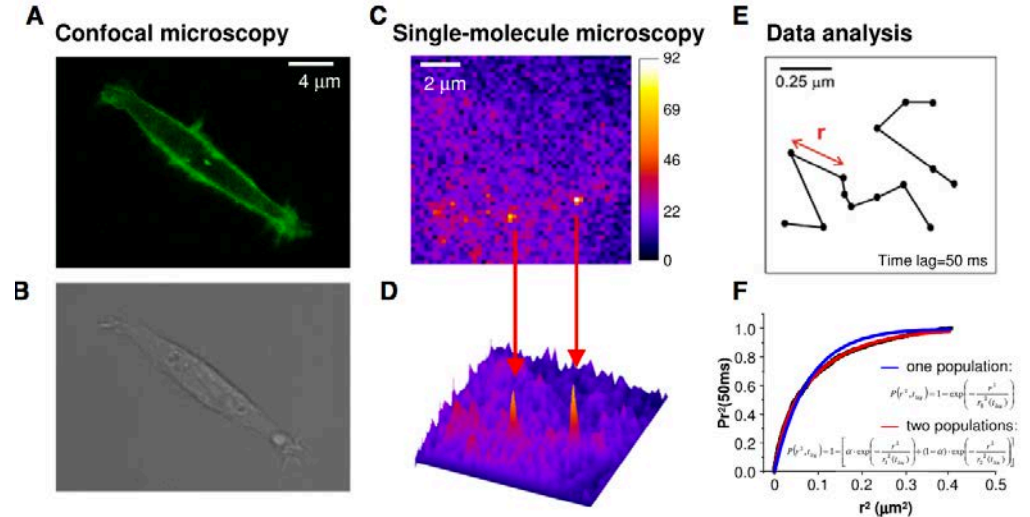
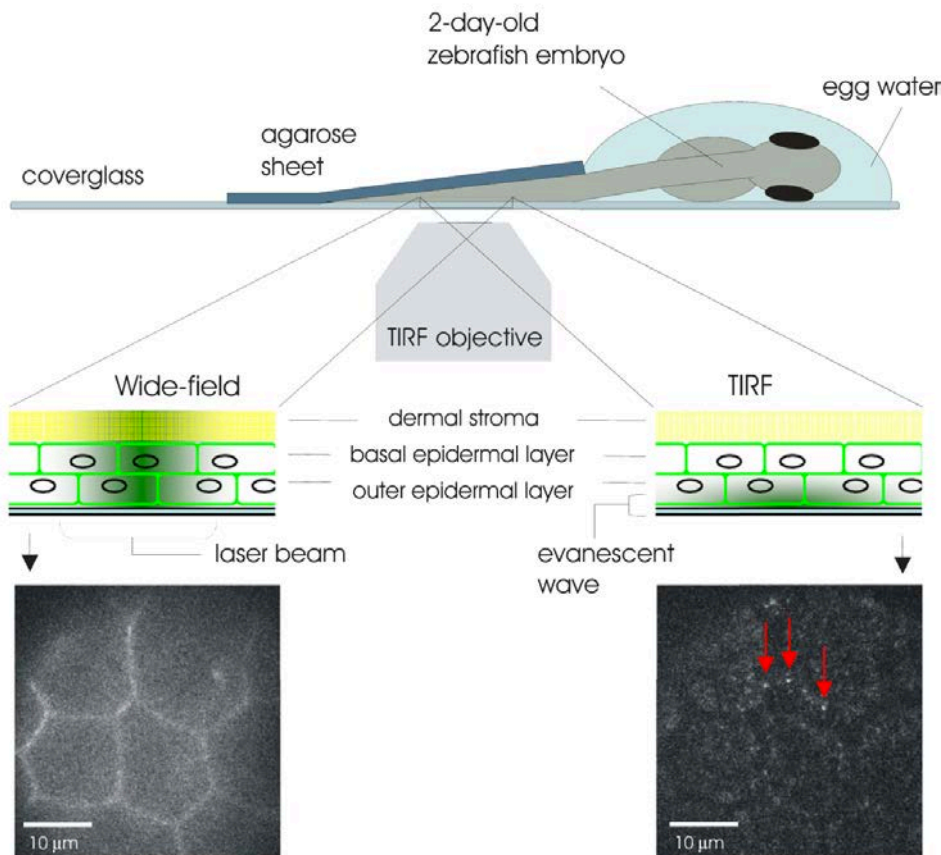


Kasai, R. S., et al. (2011) *The Journal of Cell Biology*, 192(3), 463–480. <http://doi.org/10.1083/jcb.201009128>

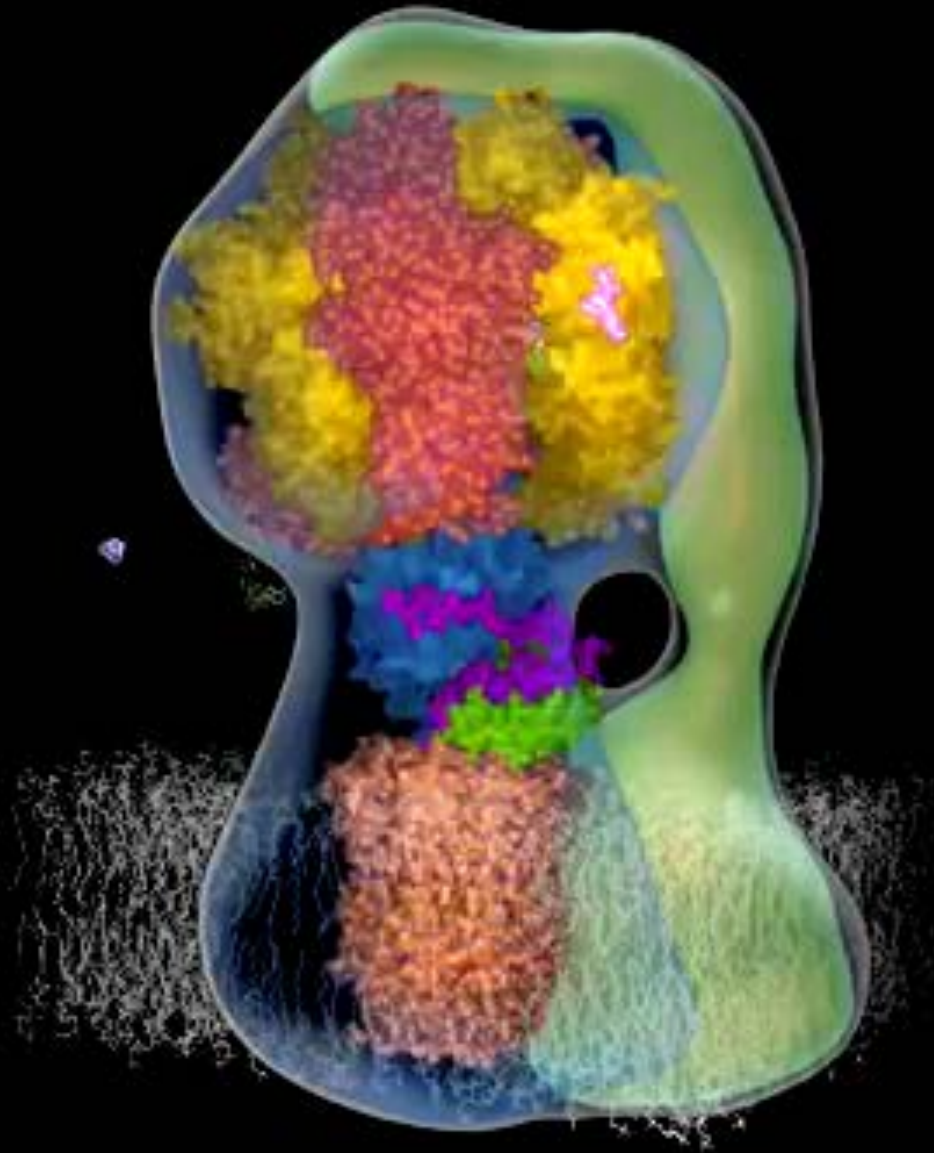
Kasai, R. S., & Kusumi, A. (2014). *Current Opinion in Cell Biology*, 27, 78–86. <http://doi.org/10.1016/j.ceb.2013.11.008>

# Single-molecule tracking 18: SMT in living organisms

Are the *ex vivo* or *in vitro* single-molecule tracking experiments relevant?



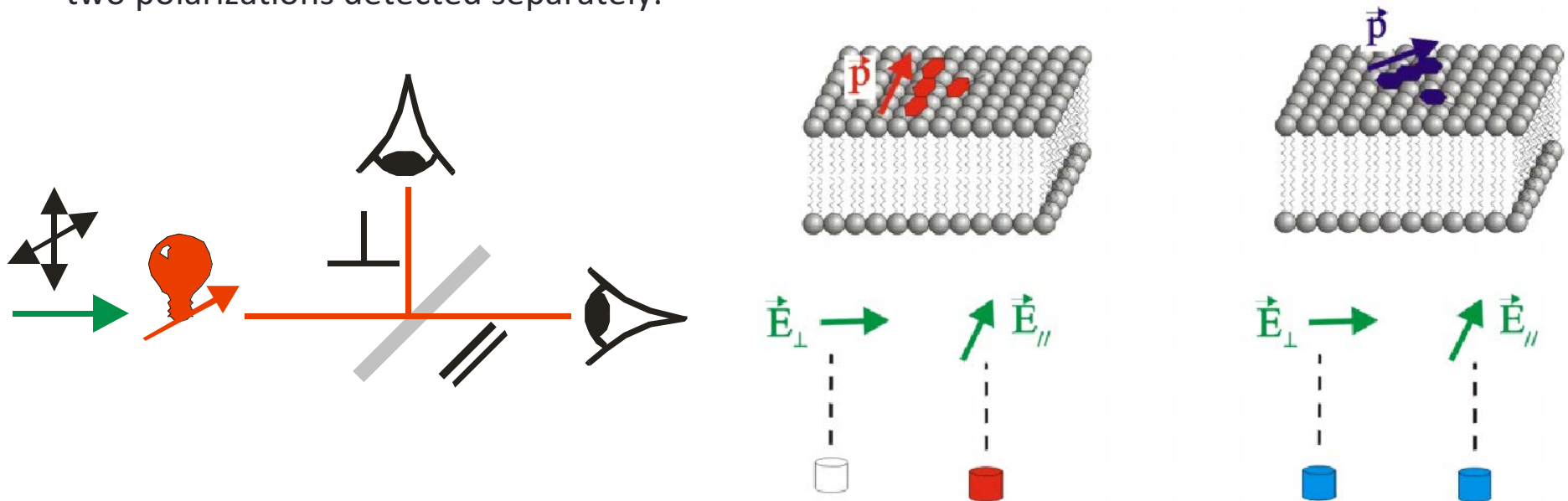
# Rotation



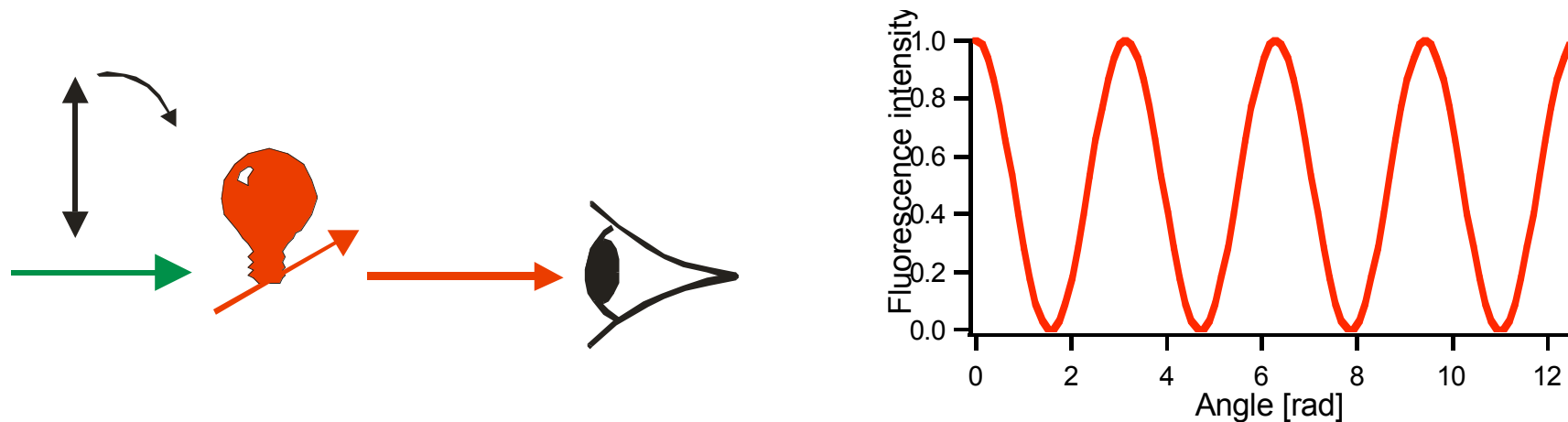


# Polarization allows monitoring of rotation. Two methods.

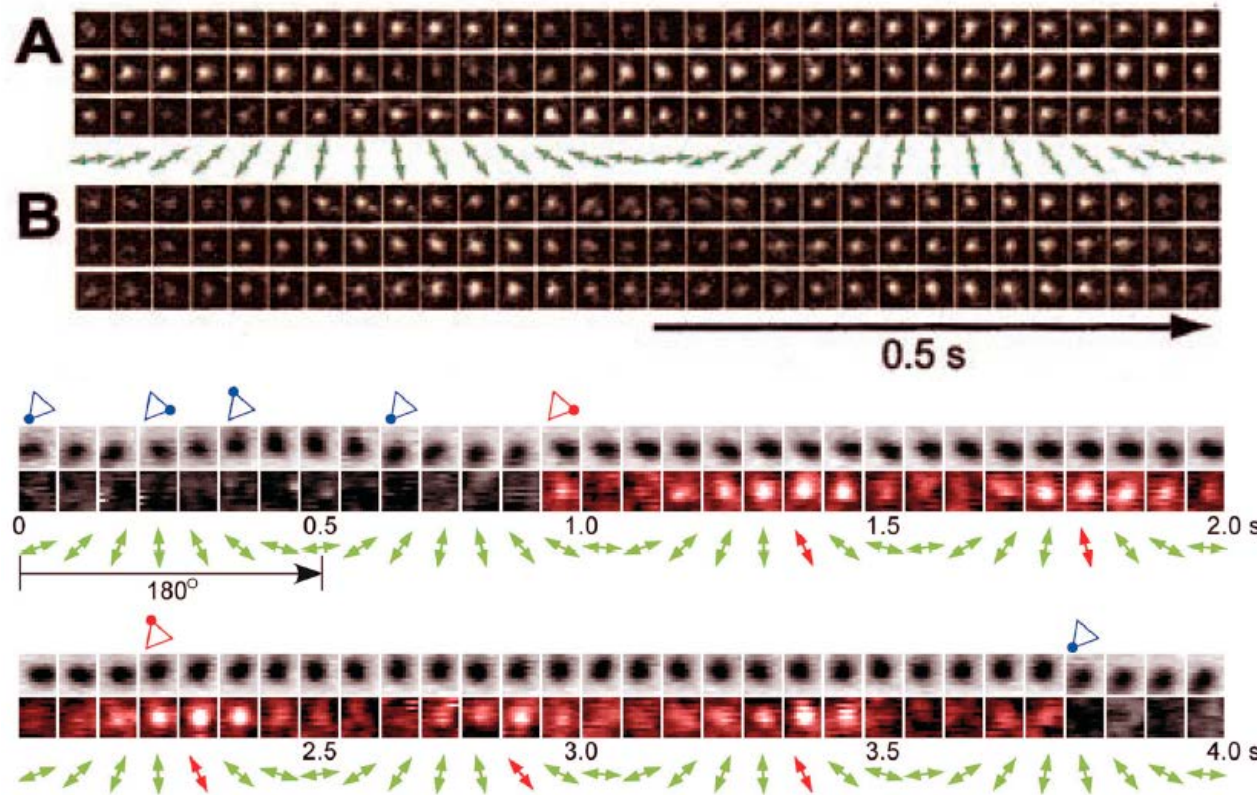
The single molecule is excited using circularly polarized light. The fluorescence is split into two polarizations detected separately.



The single molecule is excited using polarized light. The polarization is continuously rotated yielding a fluorescence intensity which varies with  $\cos^2(\text{angle})$ .

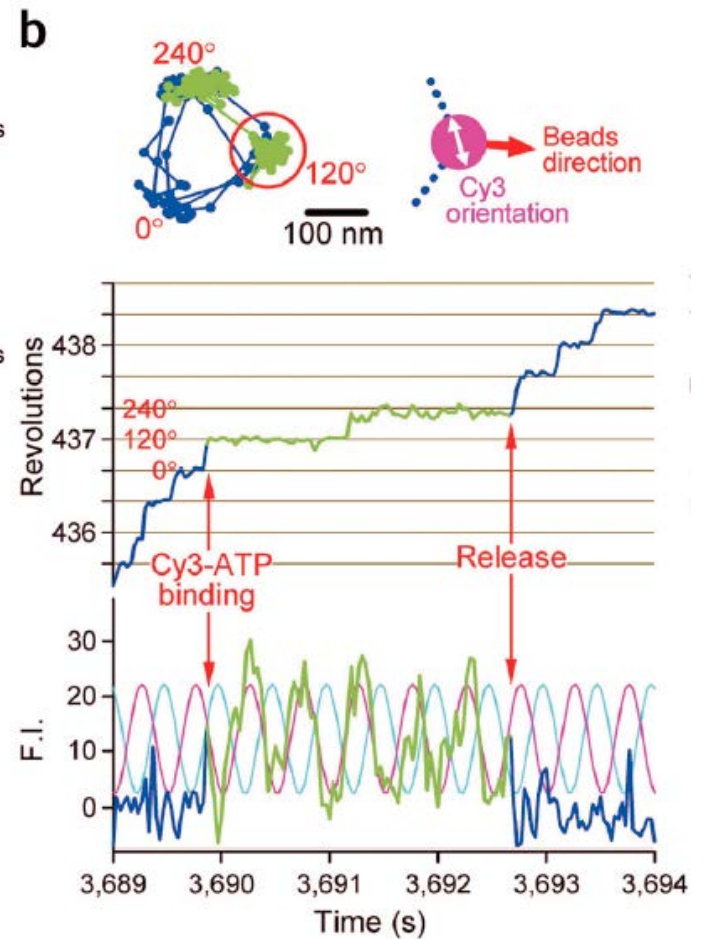
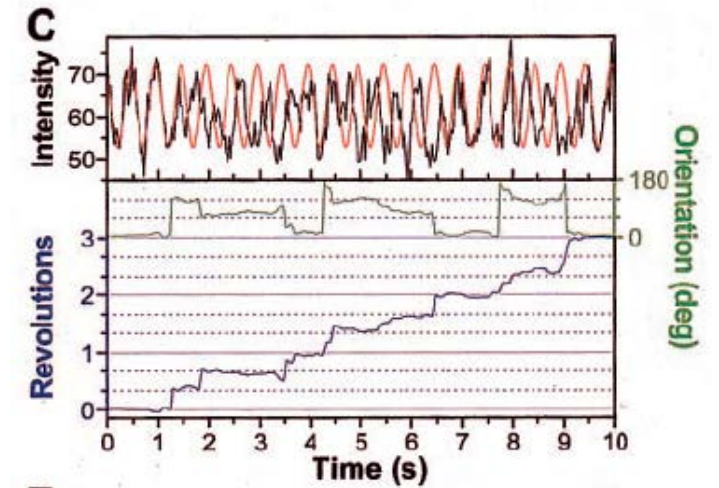
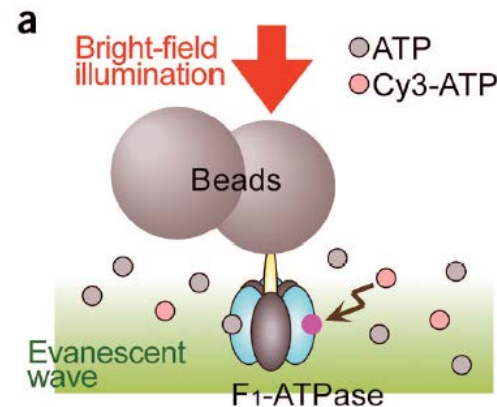


# Example: Rotation of F1-ATPase



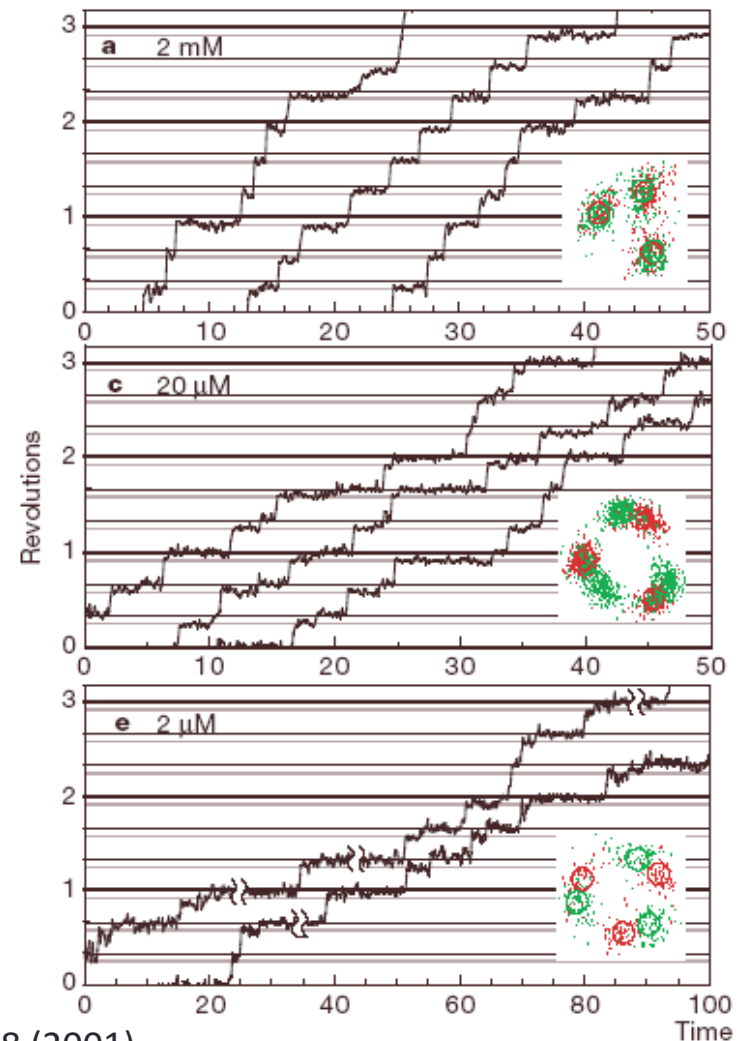
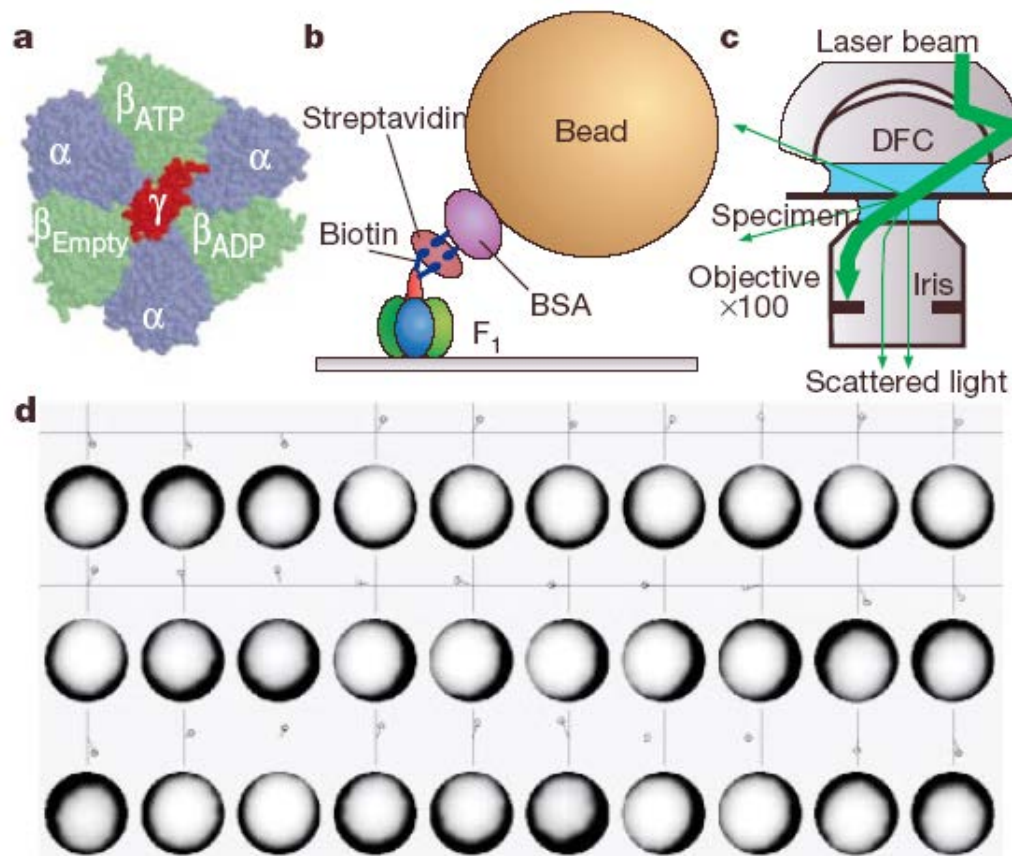
K. Adachi, K. Kinosita, et al. *Proc. Natl. Acad. Sci. USA* **97**, 7243 (2000)

T. Nishizaka, K. Kinosita, et al. *Nat. Struct. Biol.* **11**, 142 (2004)

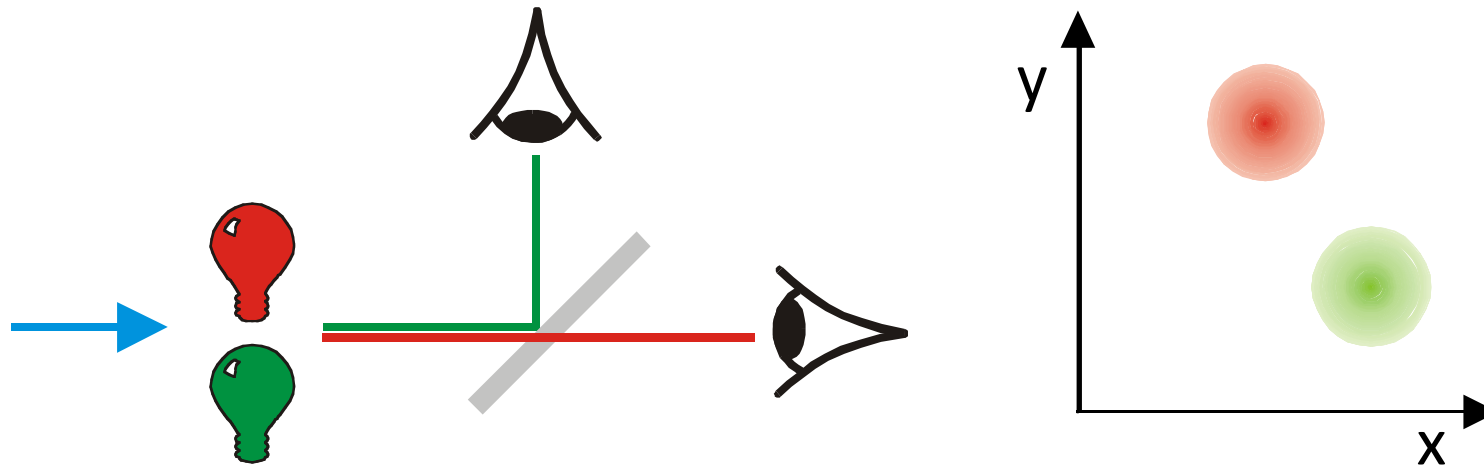


# Single-Particle Tracking (example: Rotation of F1-ATPase)

Instead of labelling the biomolecule with a fluorophore, a golden bead is used. Photobleaching is not anymore an issue and so extensively long traces can be recorded. Moreover, the time resolution is much better (submillisecond). The drawback is the size of the bead (ca. 40 nm) that may influence the properties of the biomolecule. Detection of the bead is usually performed using DIC microscopy.



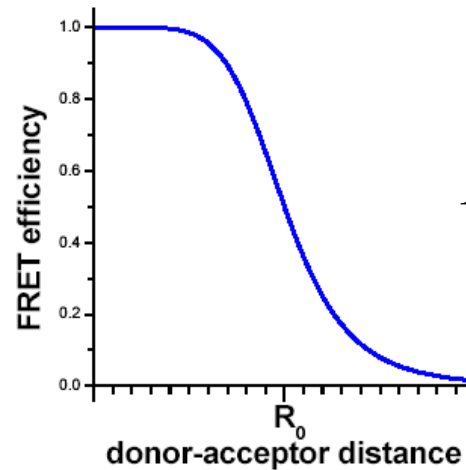
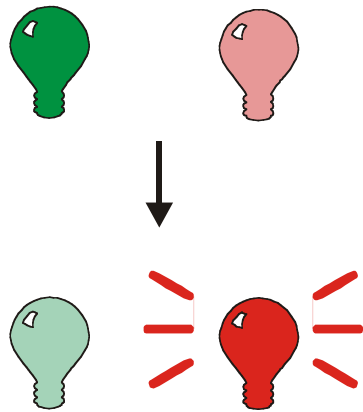
## Two colours: 2 labelled biomolecules



- Owing to the precision in the position measurements, the interaction between 2 biomolecules can be observed with a precision in the order of 30 nm.



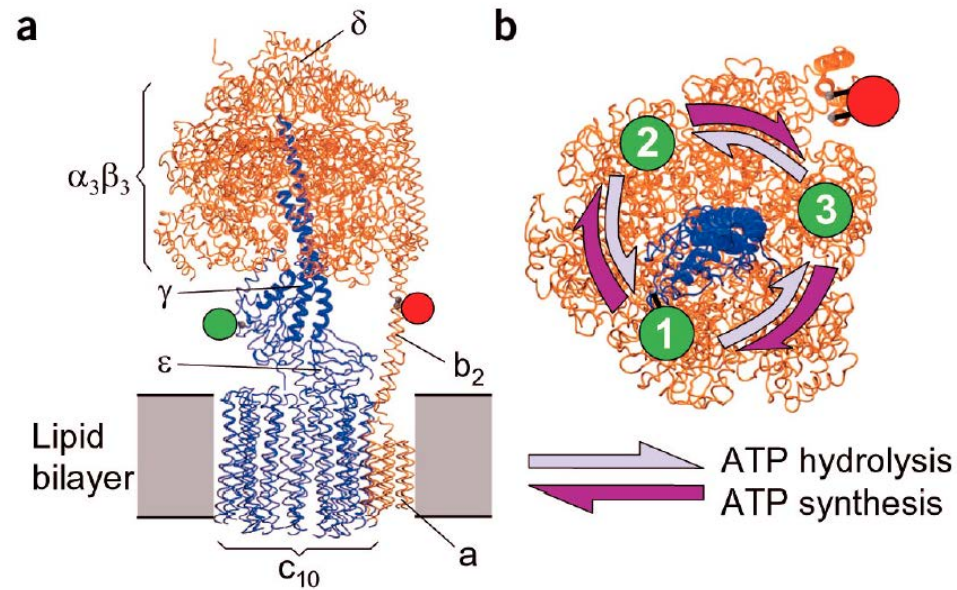
# Fluorescence resonance energy transfer (FRET)



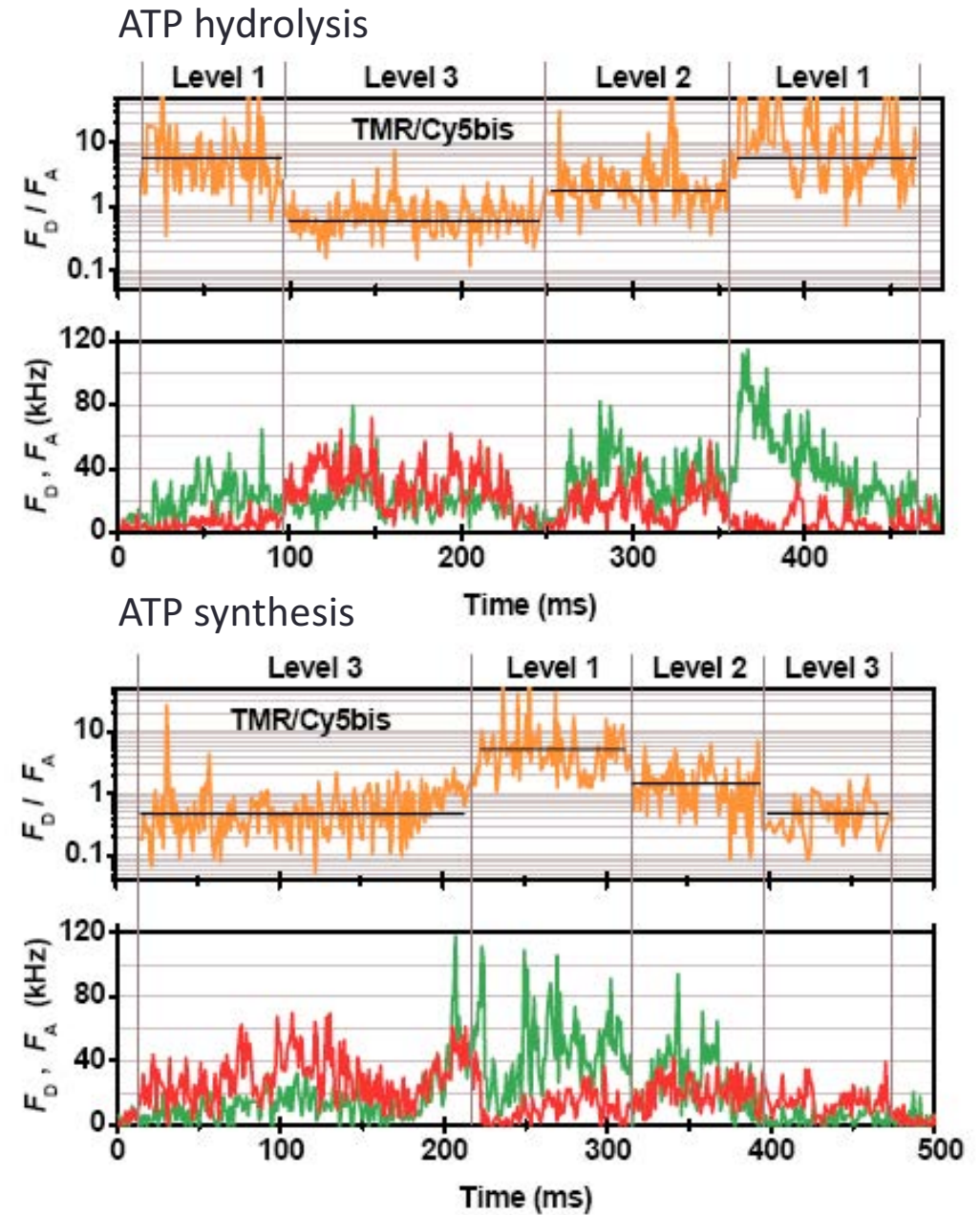
$$E = 1 - \frac{F_{\text{DA}}}{F_{\text{D}}} = \frac{R_0^6}{R_0^6 + R^6}$$

- In the formula,  $E$  is the FRET efficiency;  $F_{\text{DA}}$  is the fluorescence of the donor with acceptor present;  $F_{\text{D}}$  is the fluorescence of the donor with acceptor absent;  $R_0$  is Förster's radius;  $R$  is the distance.
- Allow the observation of the interaction between two biomolecules with nanometer precision.
- Allow the observation of conformational changes.
- $R_0$  depends on the donor-acceptor pair. It is possible to vary  $R_0$  by carefully choosing the pair.

# Example: Conformational changes in $F_0F_1$ -ATP synthase

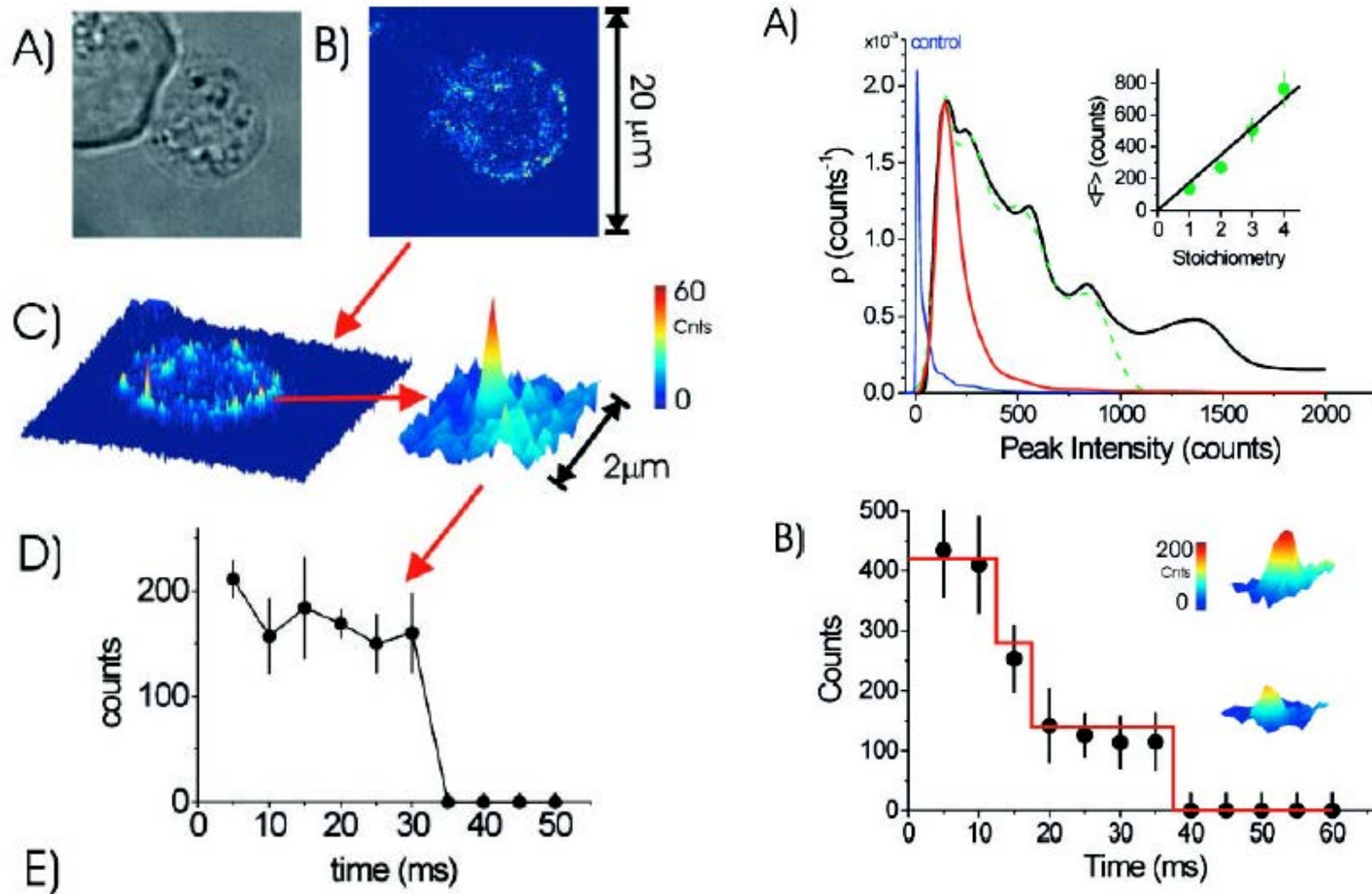


M. Diez, P. Gräber et al.,  
*Nat. Struc. Biol.* **11**, 135 (2004)



# Signal intensity/photobleaching: Information about the presence of multiple fluorophores

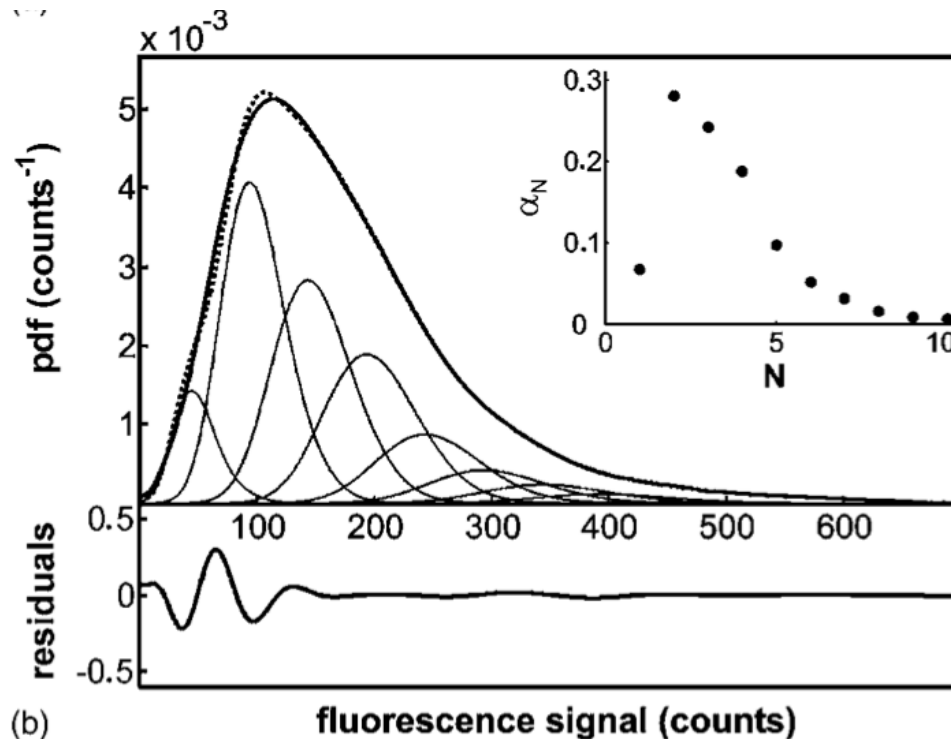
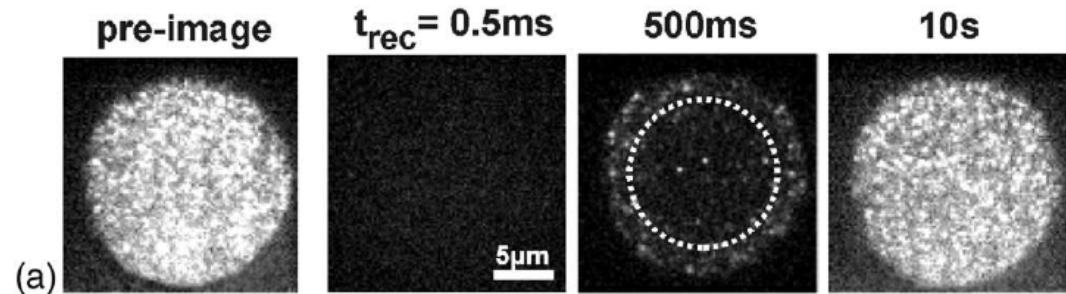
- Example: Oligomerization of the L-type  $\text{Ca}^{2+}$  channel



# Signal intensity/photobleaching: Information about the presence of multiple fluorophores

Thinning out clusters while conserving stoichiometry of labeling (TOCCSL)

FRAP followed by tracking of single-molecule diffusing in the photobleached region

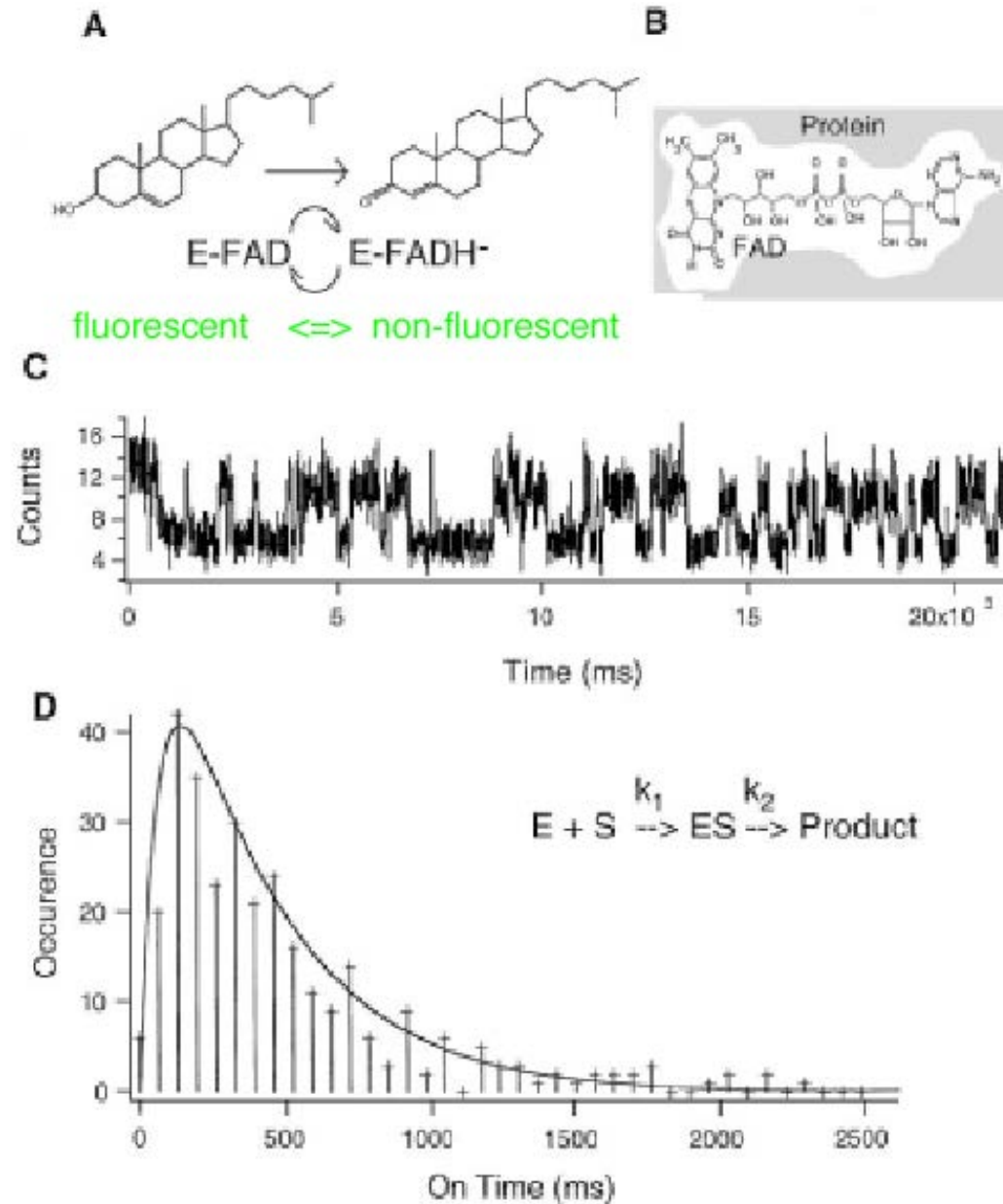


The probability density function of the cluster is fitted with a multiple normal distribution centered at multiple of single-molecule fluorescence



# Blinking 1: Monitoring of chemical reactions

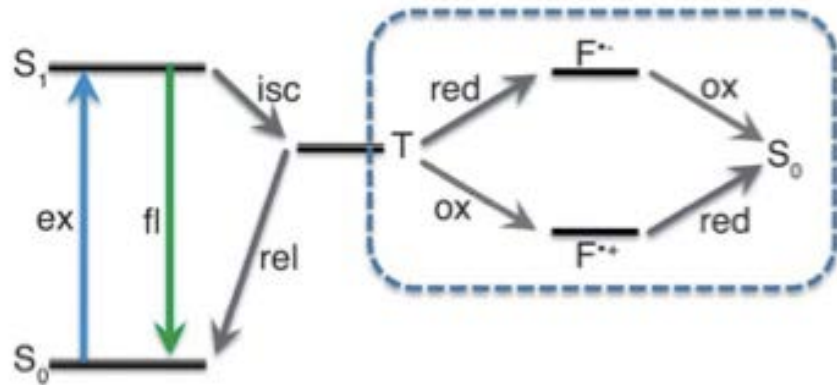
Example: Observing an enzyme at work (Cholesterol oxidase)



H.P. Lu, L. Xun, X.S. Xie, *Science* **282**, 1877 (1998)

# Blinking 2: Controlled intermittent emission of single molecule

## Organic fluorophore



Henriques 2011 *Biopolymers*

Triplet state can be stabilized using reductant and oxidant solutions leading to a controlled blinking of the dye.

## Nanocrystals of semi conductors (quantum dots)

Quantum dots are naturally blinking molecules mainly due to photo-ionization at the surface of the particle. There is no easy method to control QD blinking.

## Fluorescent proteins

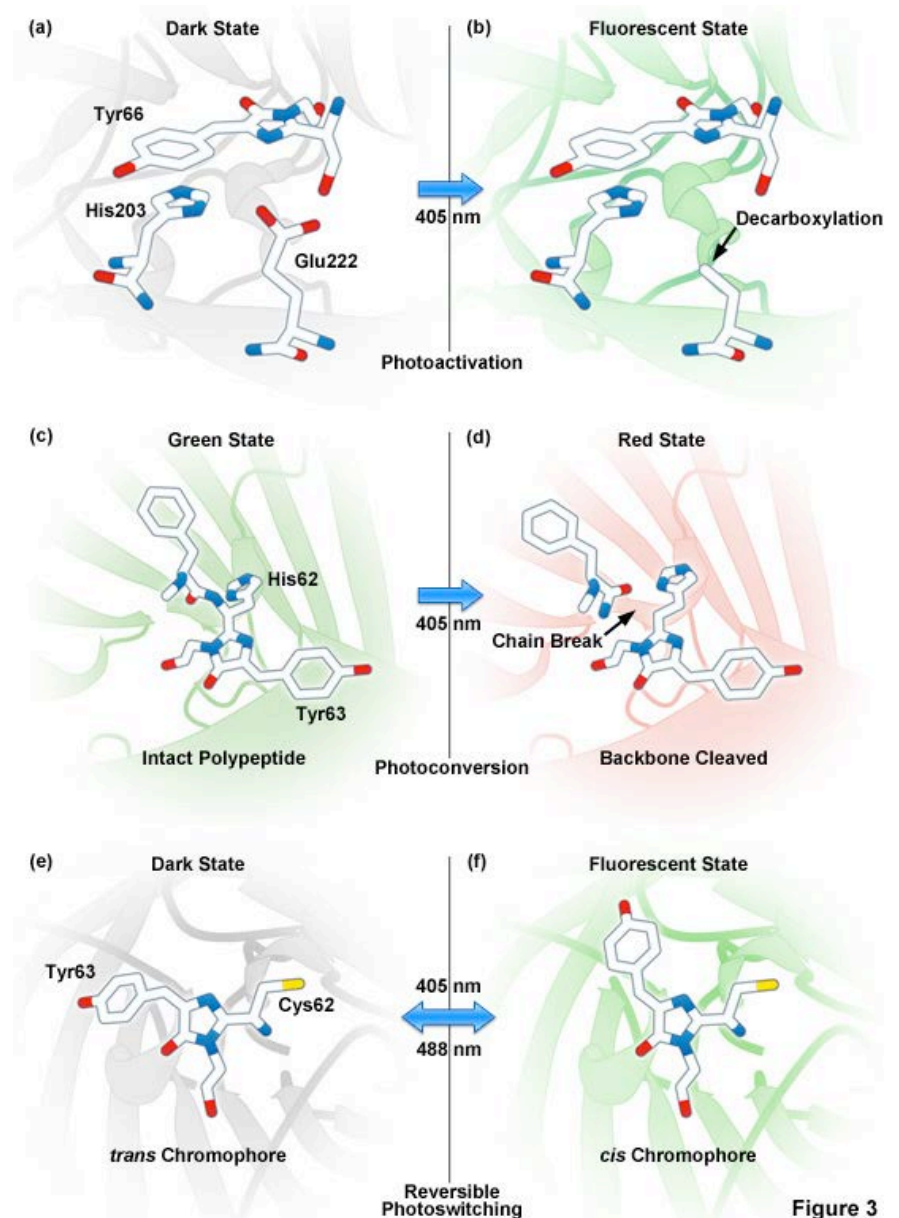
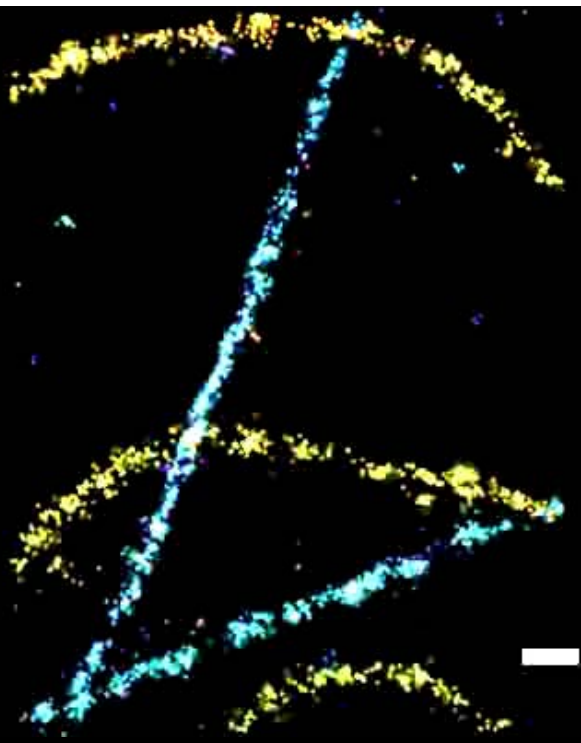
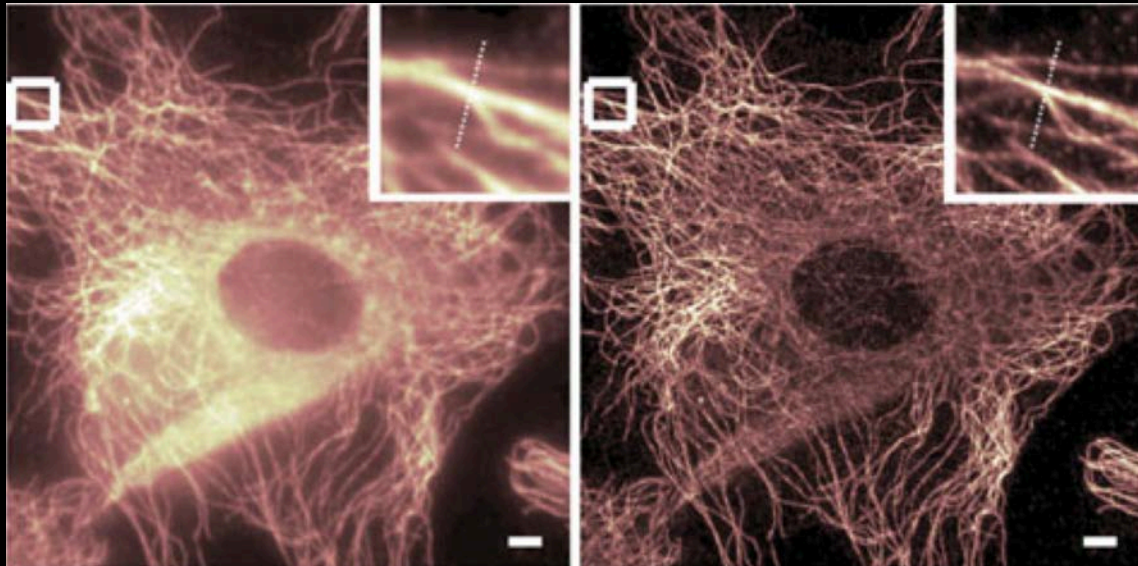


Figure 3



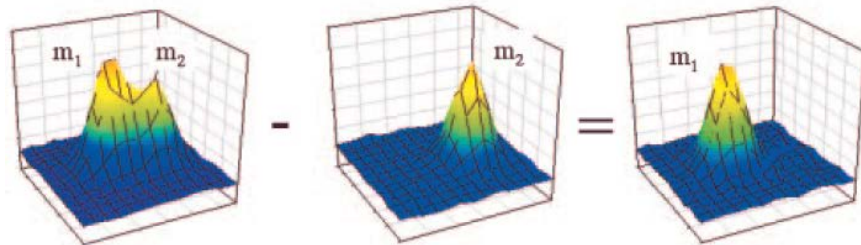
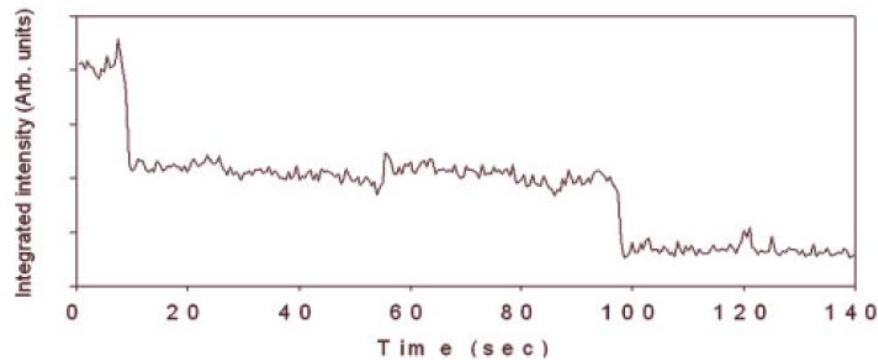
# Fluorescence nanoscopy



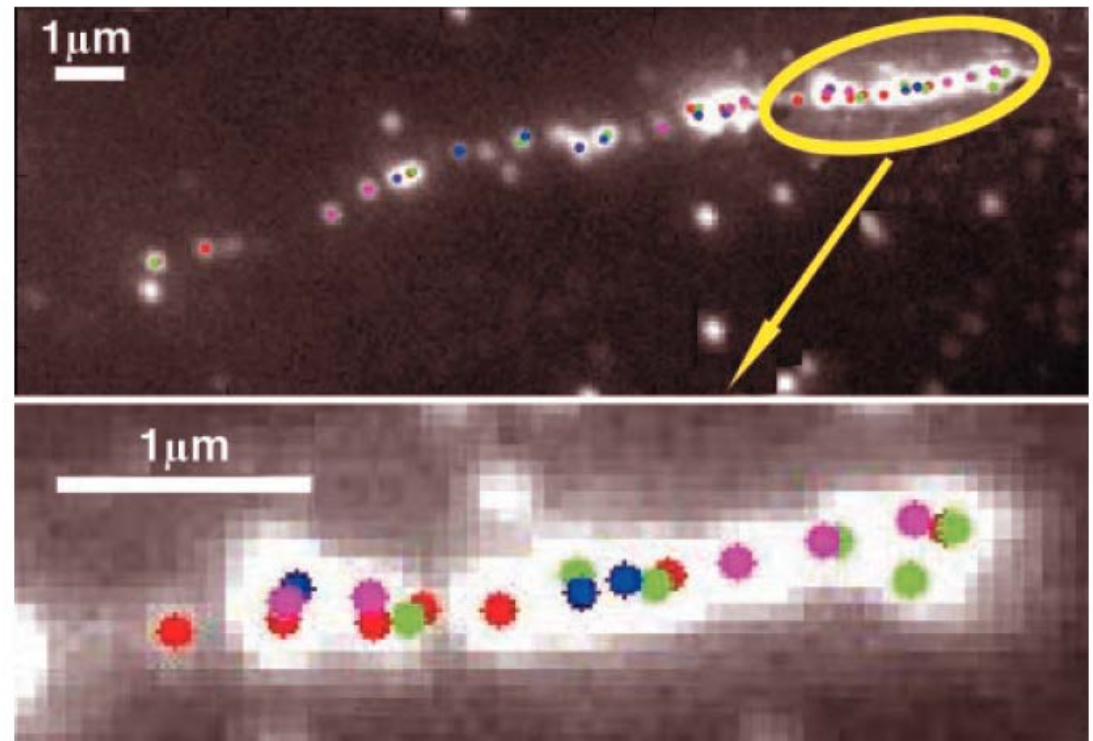
# Photobleaching: Distance measurements in the nanometer range

Distance measurements have the same accuracy as position measurements (10-30 nm).  
Principle: the last molecule to photobleach is fitted using a gaussian. This gaussian is then used to fit the two-molecule emission profile, and so on.

Example in a two-molecule case



DNA mapping



X. Qu, D. Wu, L. Mets, N.F. Scherer, *Proc. Natl. Acad. Sci. USA* **101**, 11298 (2004)

M.P. Gordon, T. Ha, P.R. Selvin, *Proc. Natl. Acad. Sci. USA* **101**, 6462 (2004)



# Dyes for superresolution microscopy (nanoscopy)

**TABLE 1.** Spectral properties of photoswitchable fluorescent proteins and organic dyes

Fluorophore	Activation (nm)	Before activation		After activation		Reference(s)
		Absorption max (nm)	Emission max (nm)	Absorption max (nm)	Emission max (nm)	
Fluorescent proteins						
PA-GFP	405	400	515	504	517	Patterson and Lippincott-Schwartz (2002)
PS-CFP2	405	400	468	490	511	Chudakov et al. (2004)
Dendra-2	405	490	507	553	573	Gurskaya et al. (2006)
Kaede	405	508	518	572	582	Ando et al. (2002)
EosFP, mEos2	405	506	516	571	581	Wiedenmann et al. (2004), McKinney et al. (2009)
mKikGR	405	507	517	583	593	Tsutsui et al. (2005), Habuchi et al. (2008)
Dronpa	405	—	—	503	518	Habuchi et al. (2005)
Dronpa-2	405	—	—	486	513	Ando et al. (2007)
bs-Dronpa	405	—	—	460	504	Andresen et al. (2008)
rsFastLime	405	—	—	496	518	Stiel et al. (2007)
eYFP	405	—	—	514	529	Dickson et al. (1997), Biteen et al. (2008)
PA-mCherry	405	—	—	570	596	Subach et al. (2009)
Synthetic dyes						
Cy5	350–570 <sup>a</sup>	—	—	649	670	Bates et al. (2005, 2007), Heilemann et al. (2005), Dempsey et al. (2009a)
Cy5.5	350–570 <sup>a</sup>	—	—	675	694	Bates et al. (2005, 2007), Dempsey et al. (2009a)
Cy7	350–570 <sup>a</sup>	—	—	747	776	Bates et al. (2005, 2007), Dempsey et al. (2009a)
Alexa Fluor 647	350–570 <sup>a</sup>	—	—	650	665	Bates et al. (2005, 2007), Dempsey et al. (2009a)
Photochromic rhodamine B	375	—	—	565	580	Folling et al. (2007)
Rhodamine spiroamides	375			537–591 <sup>b</sup>	555–620 <sup>b</sup>	Belov et al. (2009)
Azido-DCDHF		—	—	570	613	Lord et al. (2009)

PA, photoactivatable; GFP, green fluorescent protein; PS, photoswitchable; CFP, cyan fluorescent protein; eYFP, enhanced yellow fluorescent protein; azido-DCDHF, azido-2-dicyanomethylene-3-cyano-2,5-dihydrofuran.

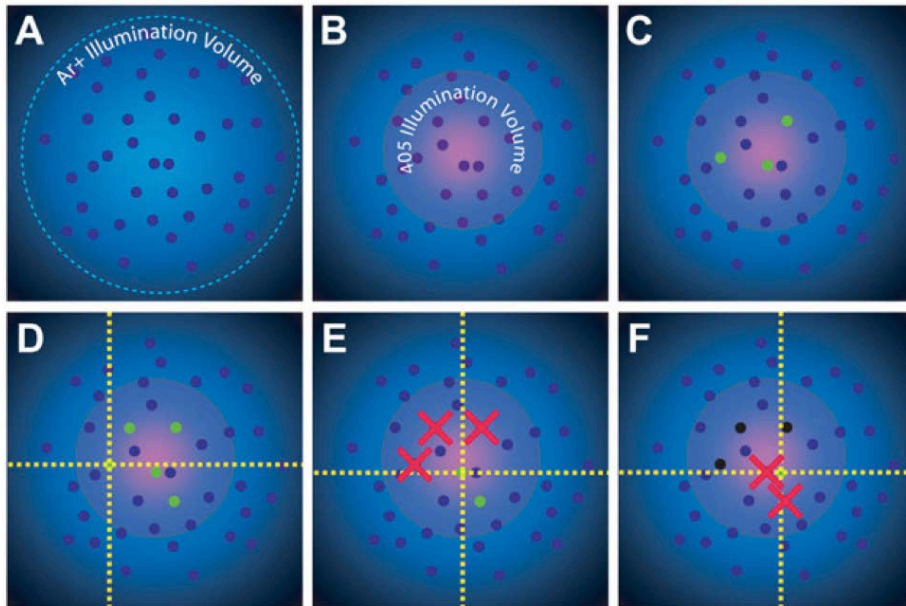
<sup>a</sup>Dependent on the activator dye, if present.

<sup>b</sup>Dependent on the specific compound.

Bates M, Jones SA, Zhuang X (2013) *Cold Spring Harbor Protocols* 2013

# Super-resolution 1: PALM

## Photoactivated localization microscopy (PALM)

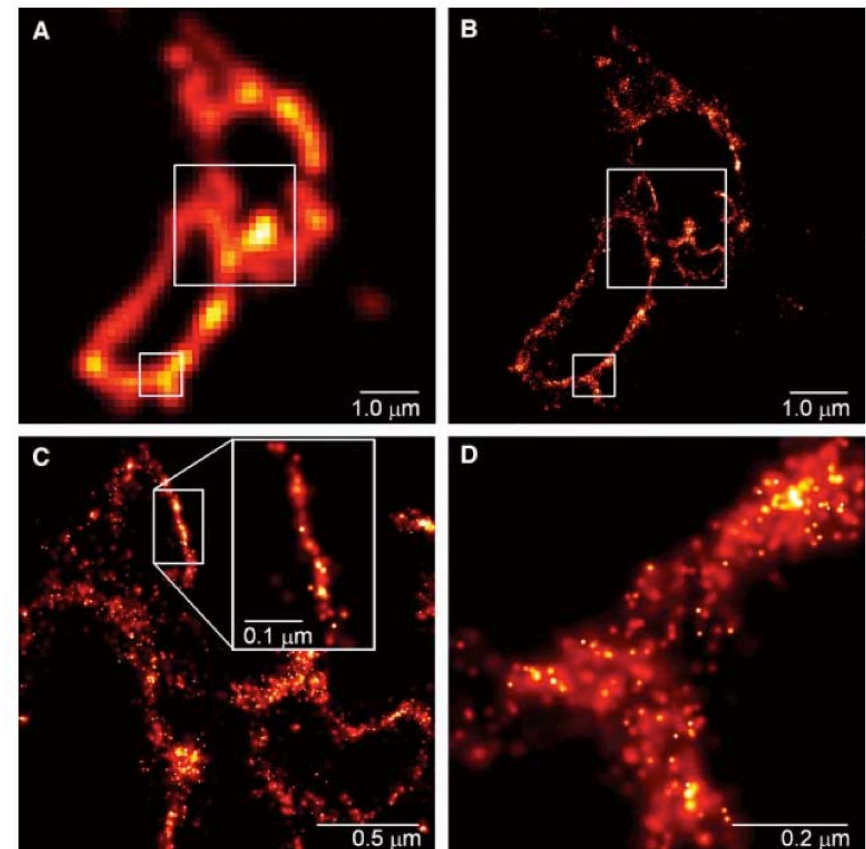
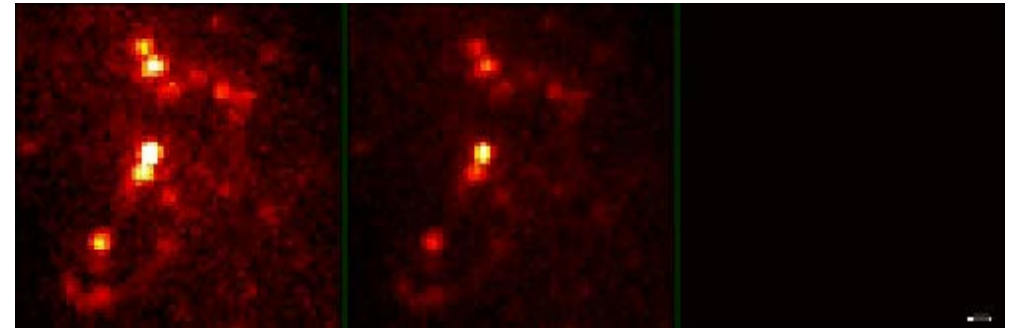


Hess, *Biophys J*, 2006

Fluorescent protein is activated or switched at low rate: molecules appear as single fluorescent spots.

Requirements:

- Photoactivatable or photoconvertible fluorescent protein (eg. mEOS2, Dronpa PA-GFP, PA-mCherry, EYFP)
- Relatively low protein expression



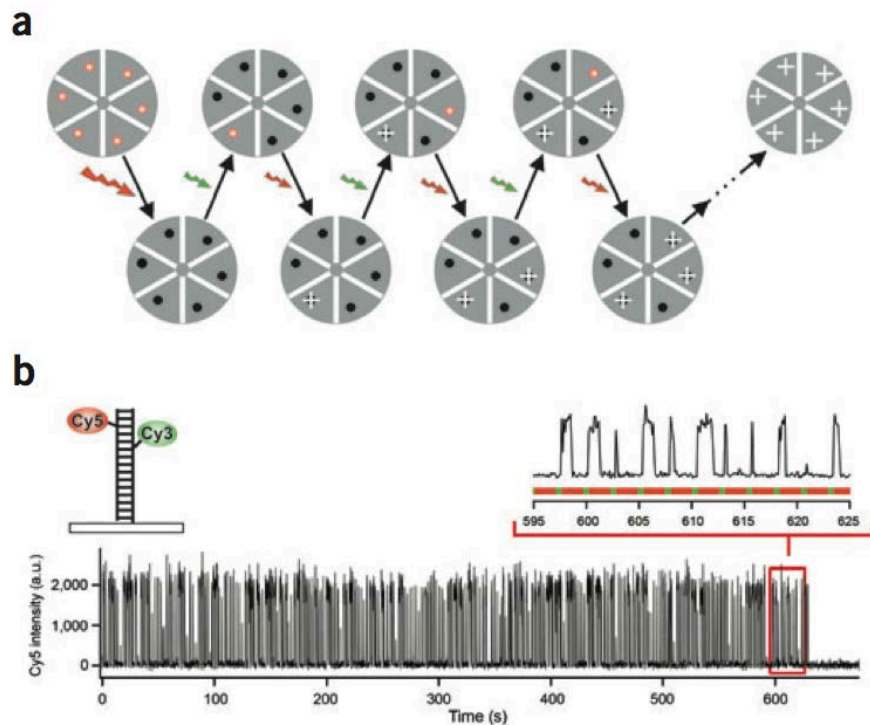
Betzig, *Science*, 2006



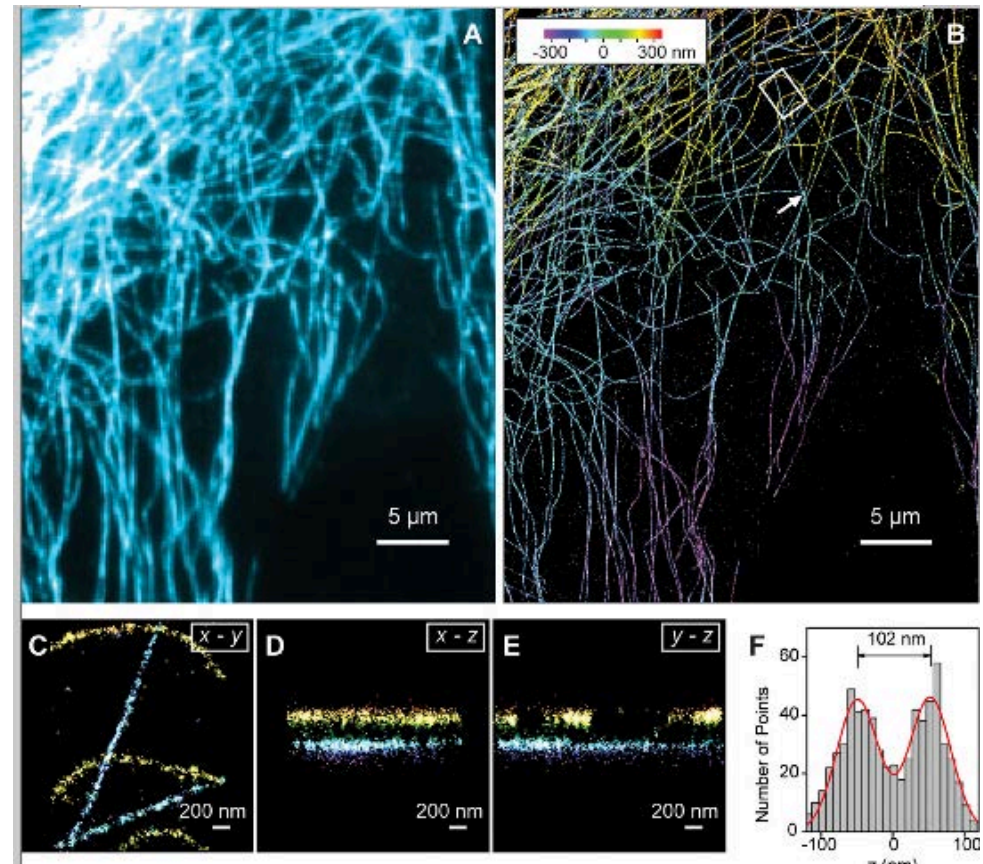
# Super-resolution 2: STORM

## Stochastic optical reconstruction microscopy (STORM)

### Principle



Rust, *Nat Meth*, 2006



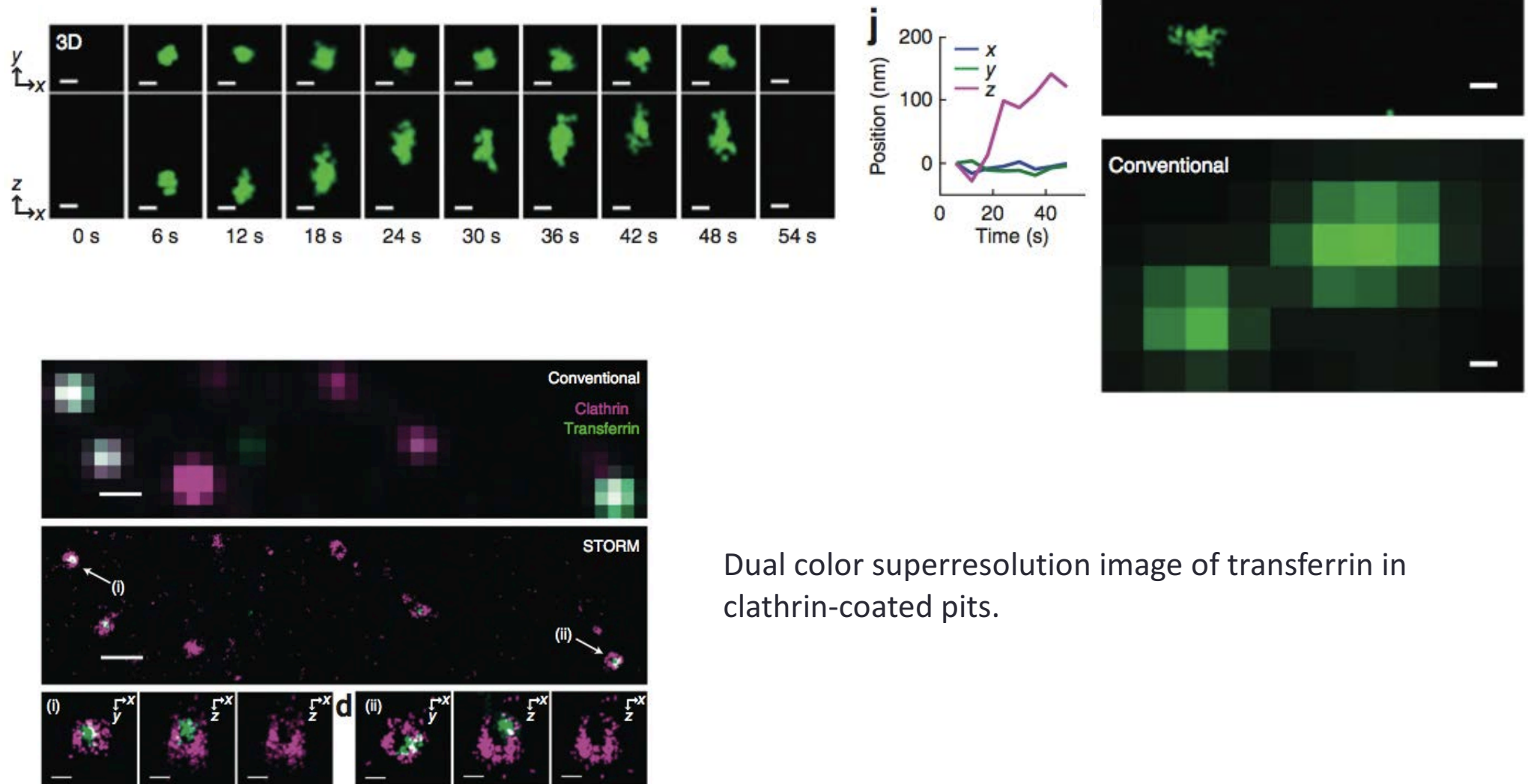
Huang, *Science*, 2008

A dye is maintained in a dark state using strong excitation light. A fraction of the dye is reactivated using another wavelength. This can be mediated using another dye (STORM) or without (dSTORM)  
Requirements:

- A pair of dye (eg Cy5 & Cy3) in close proximity (nanometer range) or a dye with stable triplet state
- An adapted buffer environment.
- Post-translational labelling (generally outside cells or *in vitro*)

# Super-resolution 3: Dynamic STORM in living cell

Dynamic STORM image of transferrin in live cell

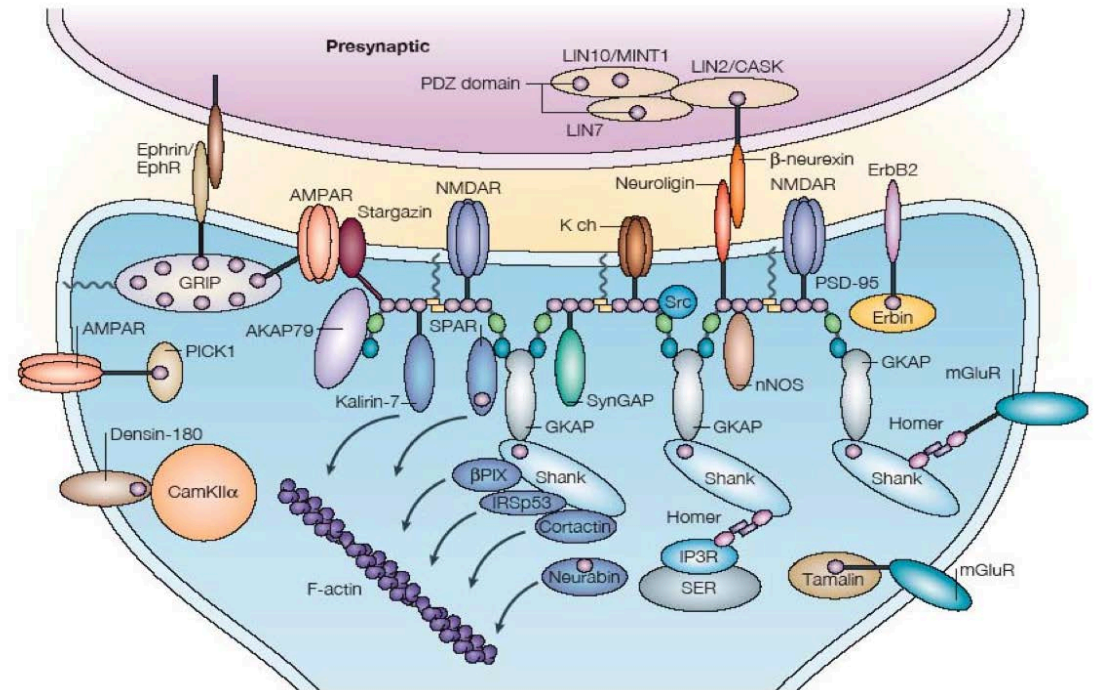
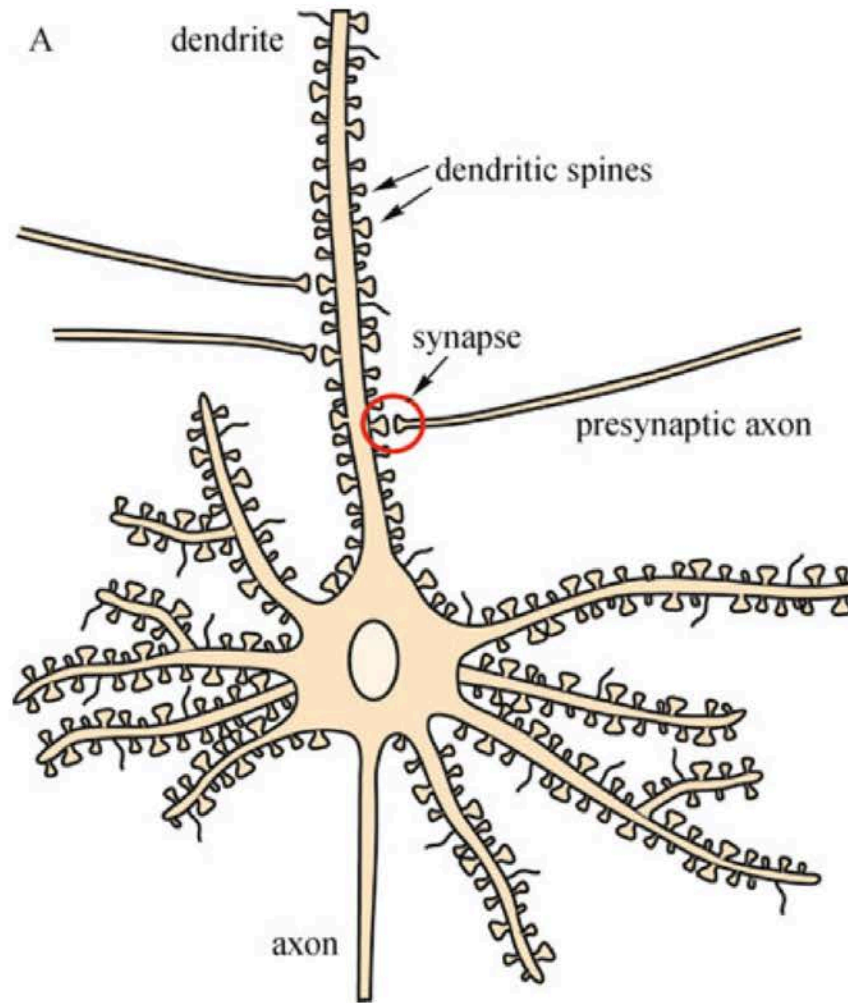


Dual color superresolution image of transferrin in clathrin-coated pits.



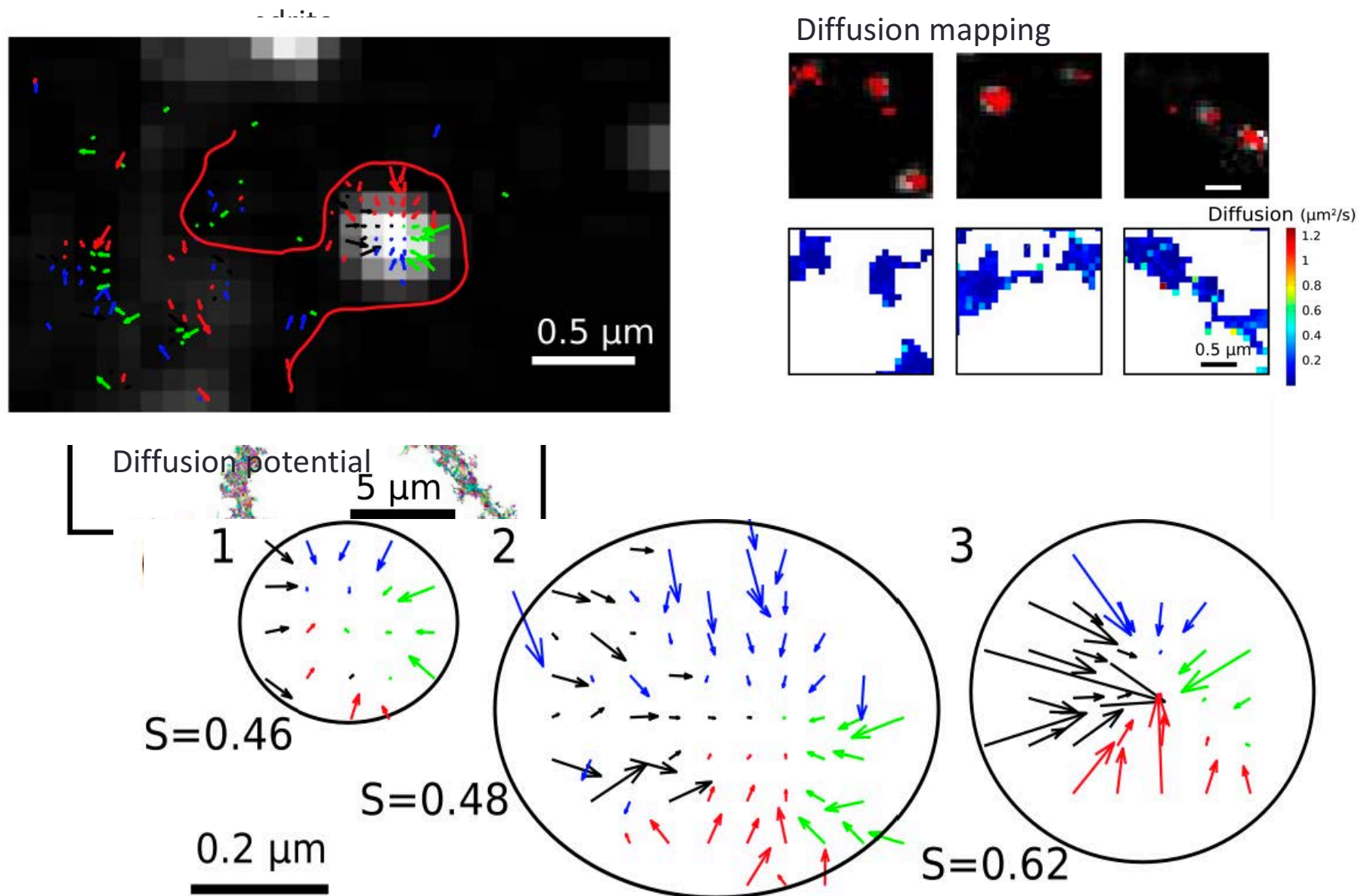
# Super-resolution 4: Dynamic STORM in neuron

How do receptors diffuse in post-synaptic membrane ?



# Super-resolution 5: Dynamic STORM in neuron

How do receptors diffuse in post-synaptic membrane ?

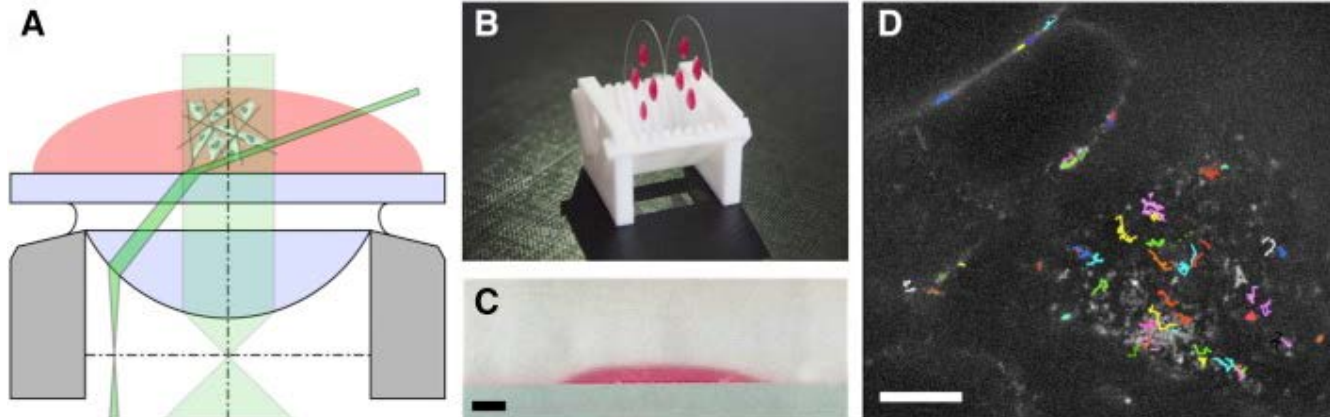
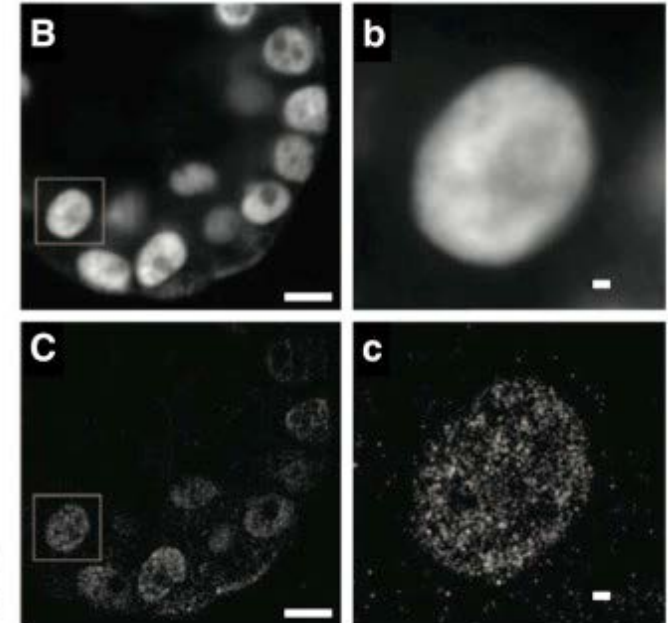
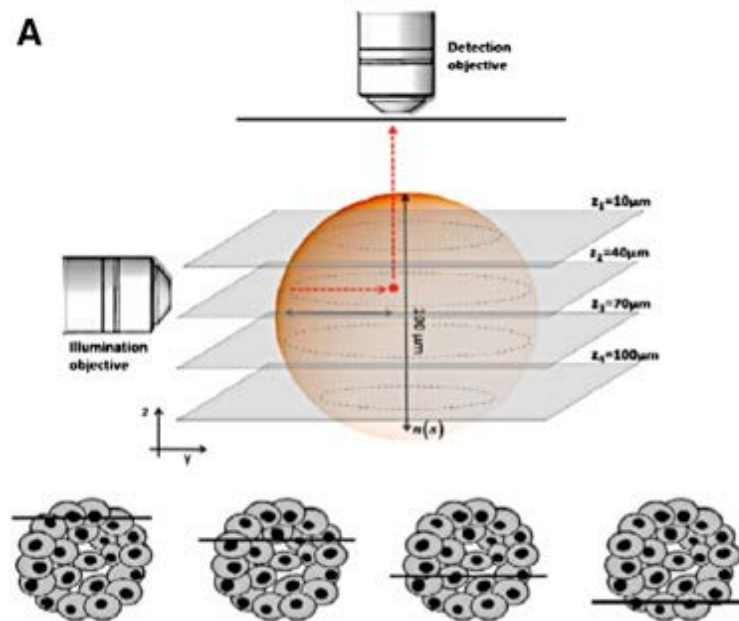


# Single-molecule tracking/superresolution: Light-sheet

Single-molecule localization in 3D is achieved by using a light-sheet to illuminate the sample

Light-sheet microscopy on spheroid.

A second objective is used for illumination

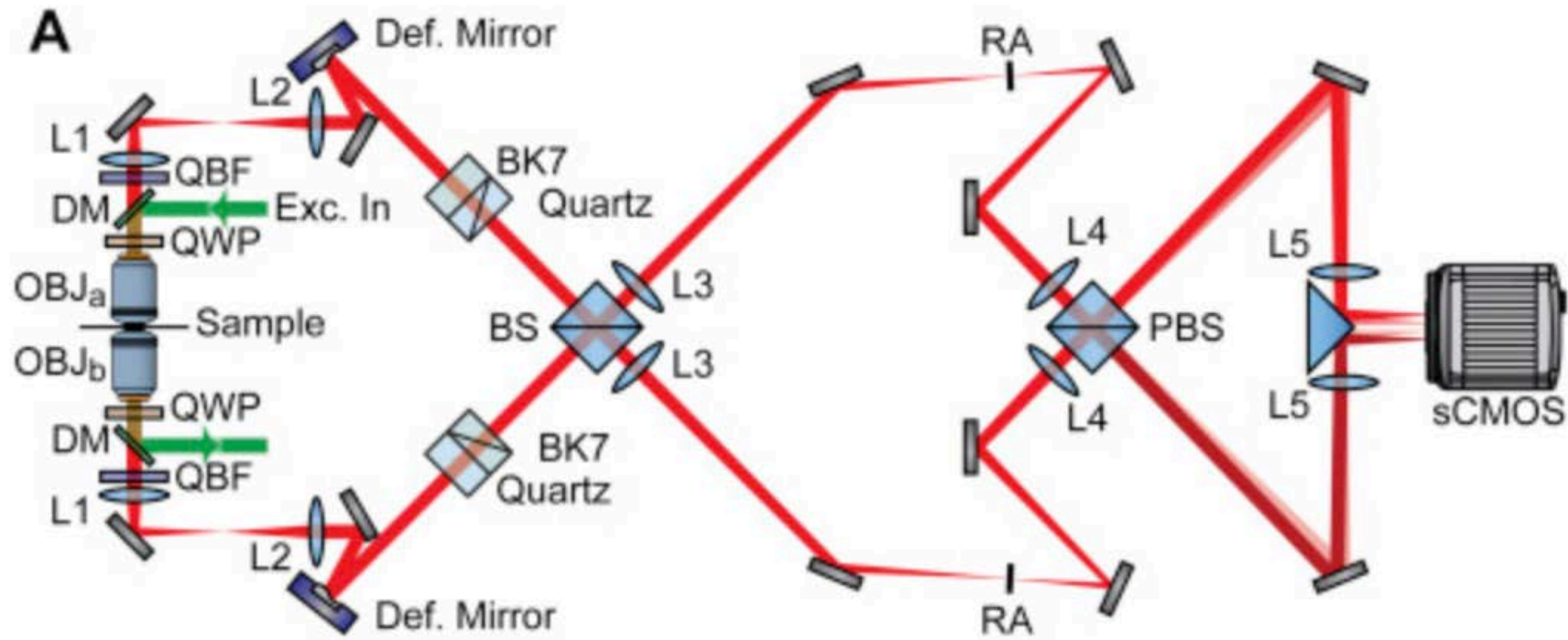


Highly Inclined Laminated Optical Sheet (HILO) of a 3D cell culture in collagen



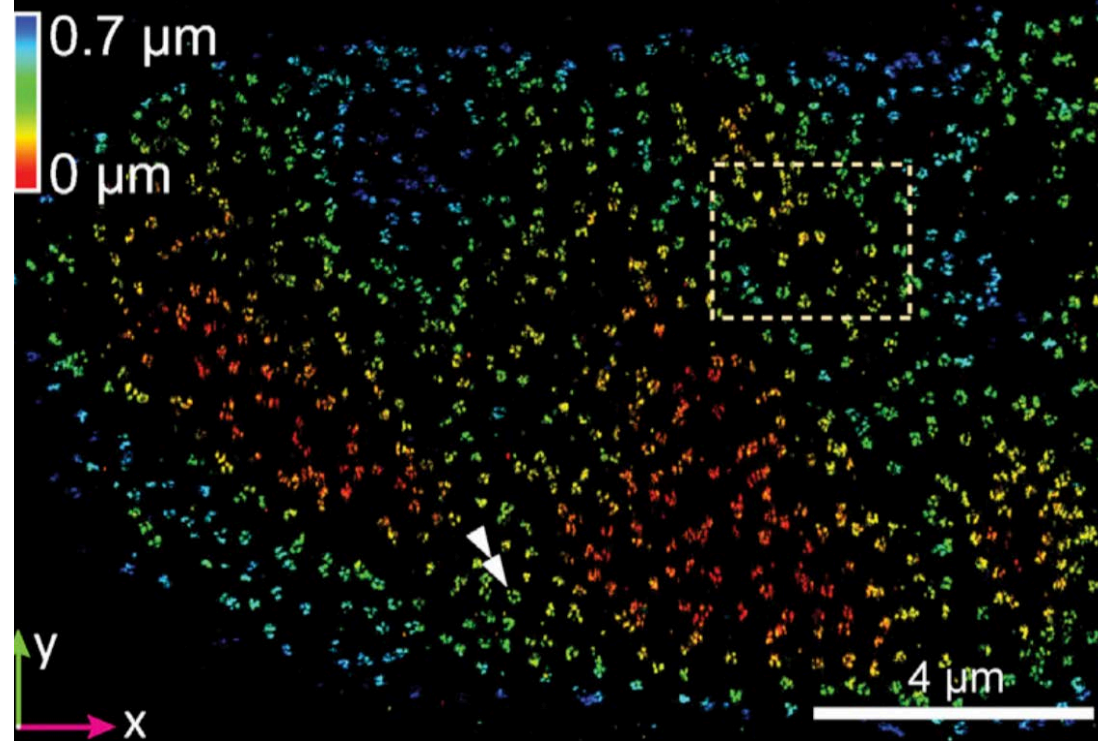
## Super-resolution 6: 3D image of whole cells

Whole-cell 4Pi single-molecule switching nanoscopy (W-4PiSMSN):  
Combination of PALM, 4Pi-microscopy and iPALM

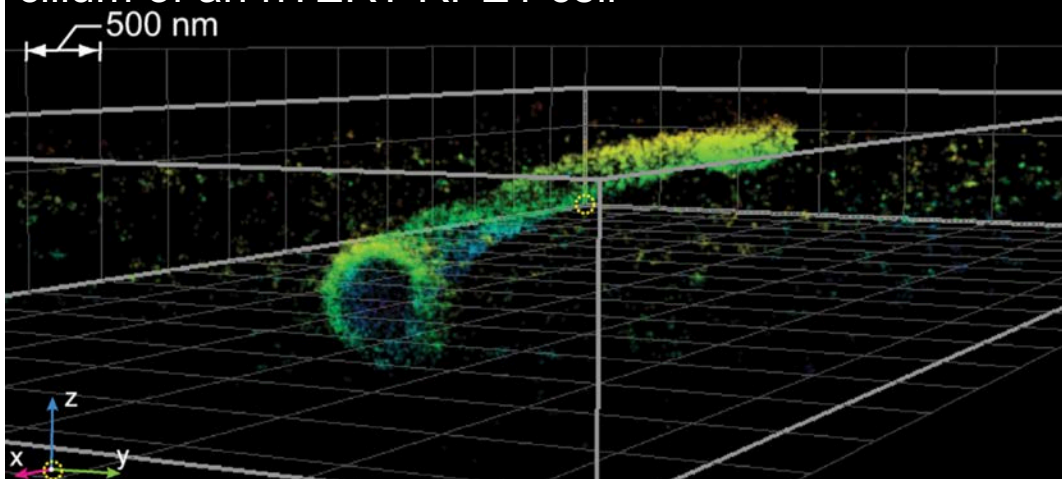


- The lateral resolution is increased by a factor 1.7 thanks to the 2 objectives
- The 4Pi configuration of the objective allows to reach a 10 nm axial resolution

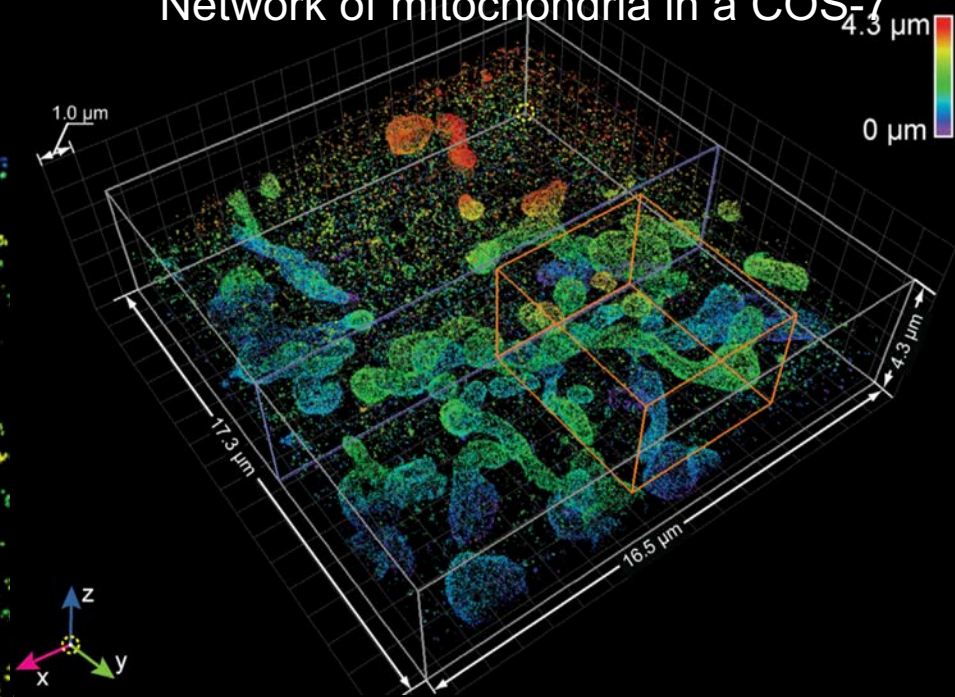
## Nuclear Pore Complexes



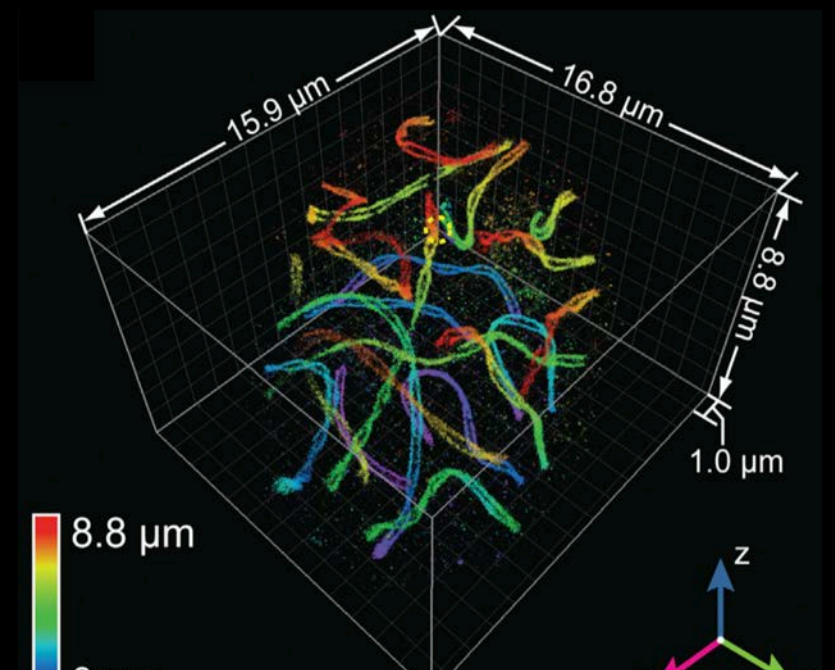
pH- SMO (a GPCR) on the primary cilium of an hTERT-RPE1 cell



## Network of mitochondria in a COS-7



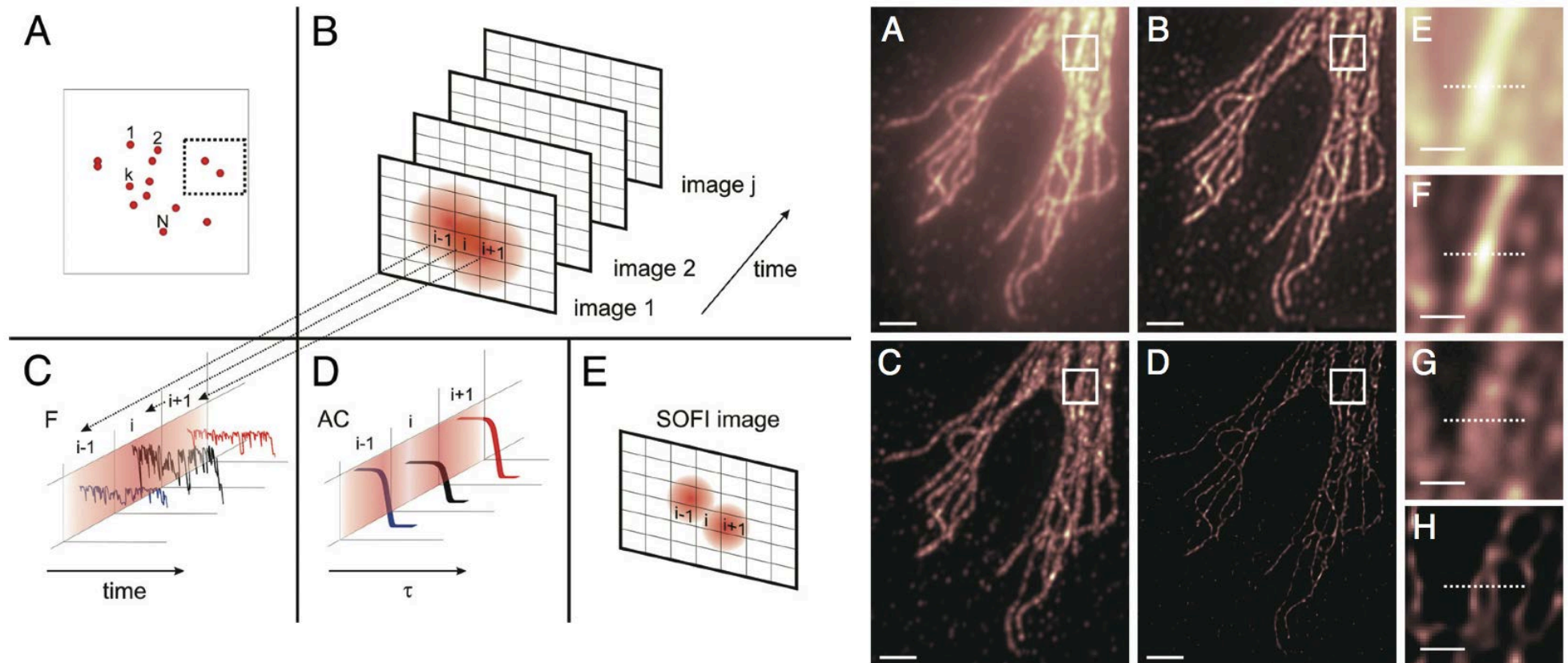
## Synaptonemal Complexes in a Whole-Mouse Spermatocyte





# Super-resolution 7: SOFI

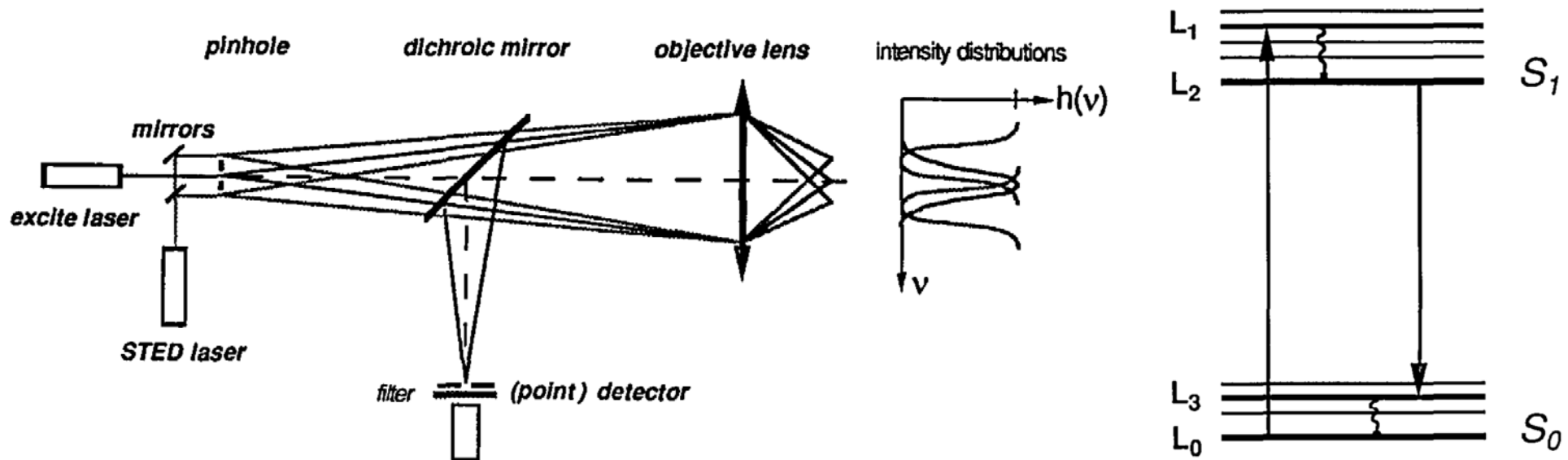
Blinking of fluorescent probe is used to increase image resolution !



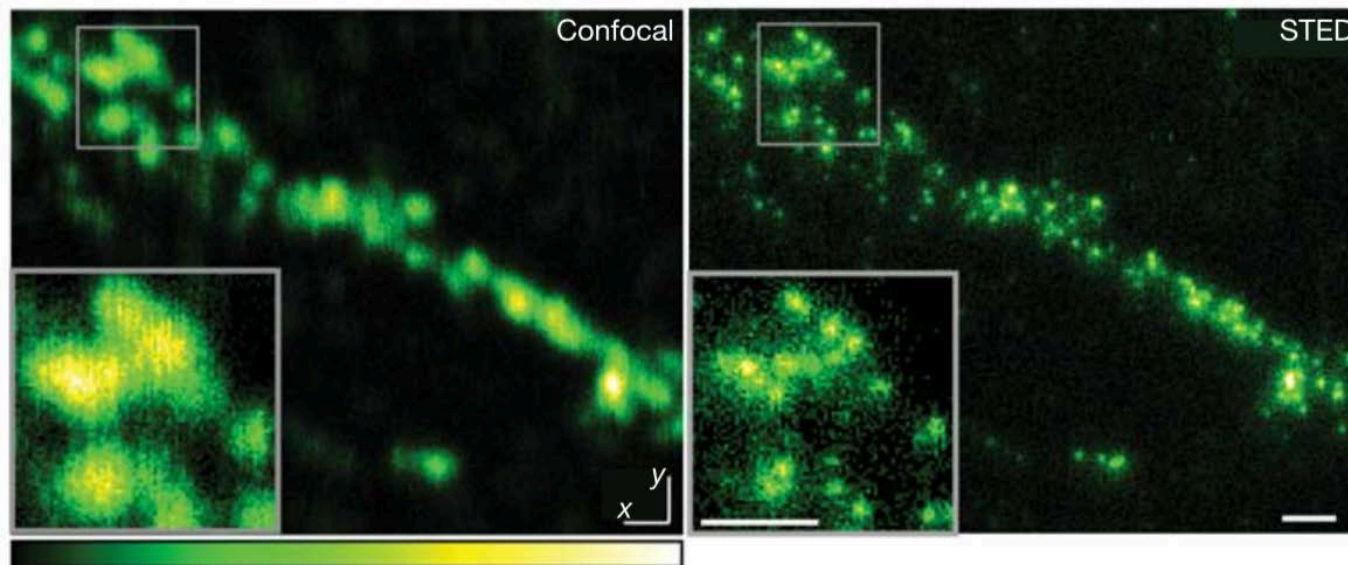
Dertinger, T., Colyer, R., Iyer, G., Weiss, S., & Enderlein, J. (2009) *PNAS*, 106(52), 22287–22292



# Super-resolution 8 : Confocal STED microscopy

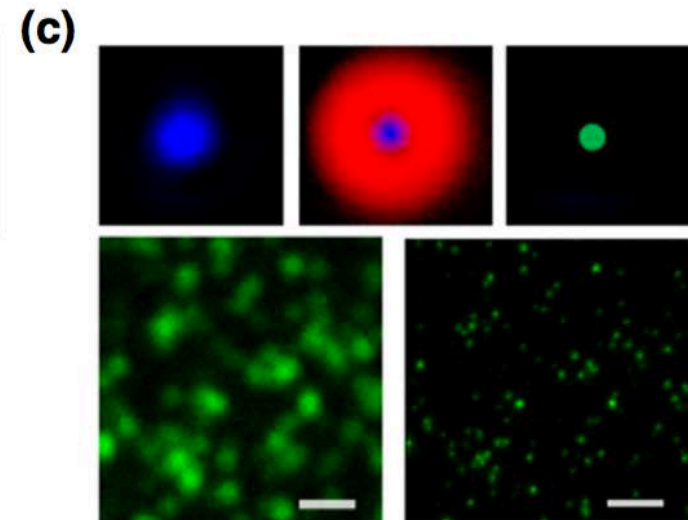
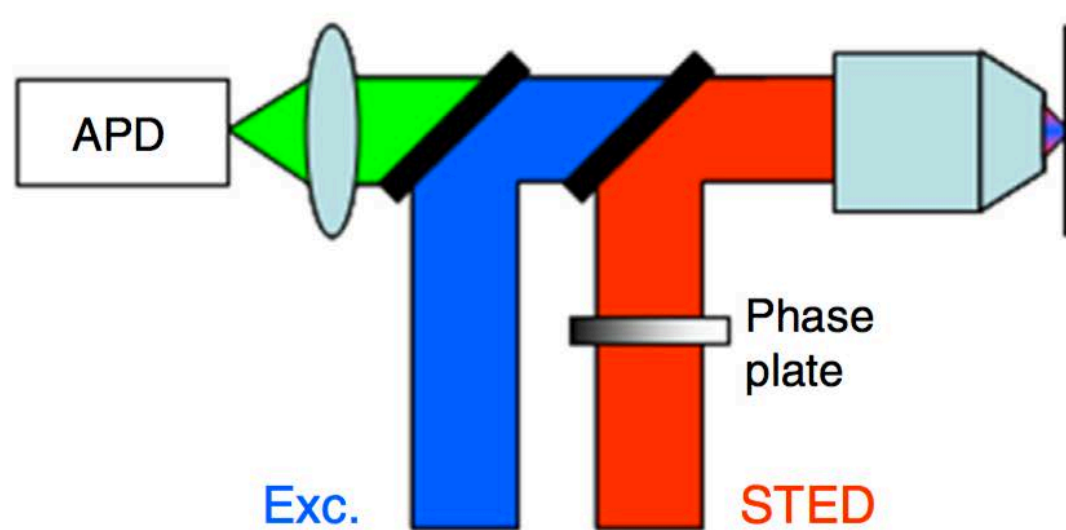
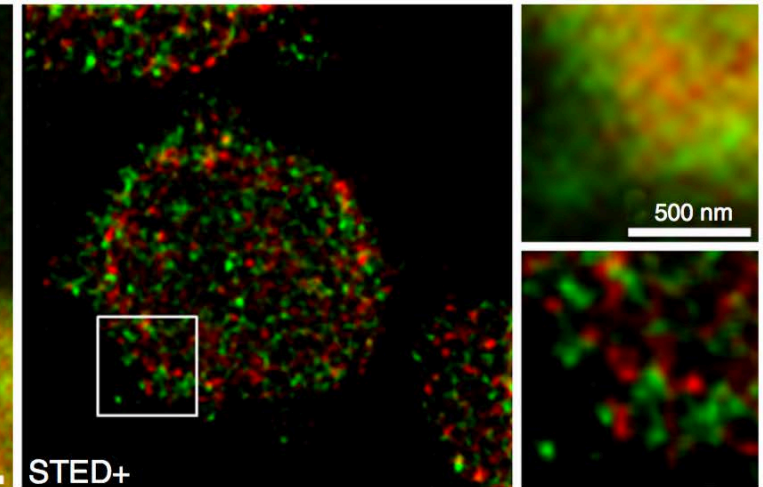
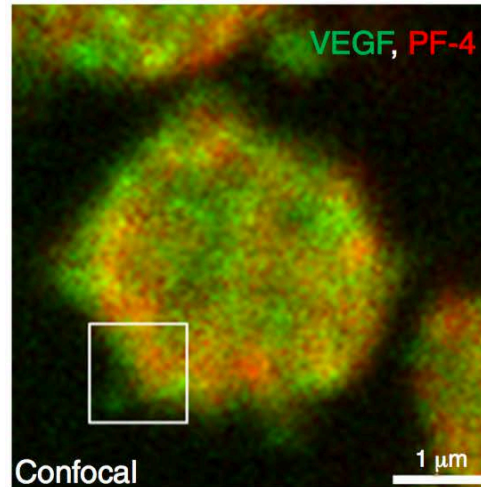
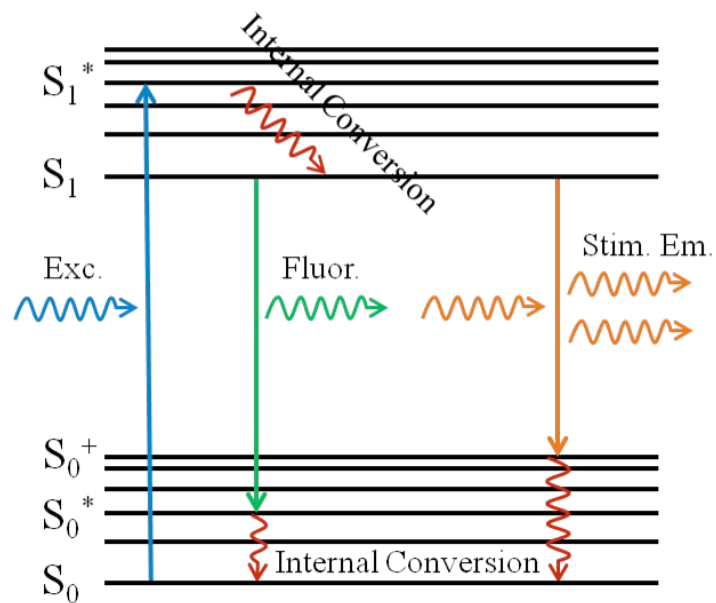


Hell, S. W., & Wichmann, J. (1994). *Optics Letters*, 19(11), 780–782.



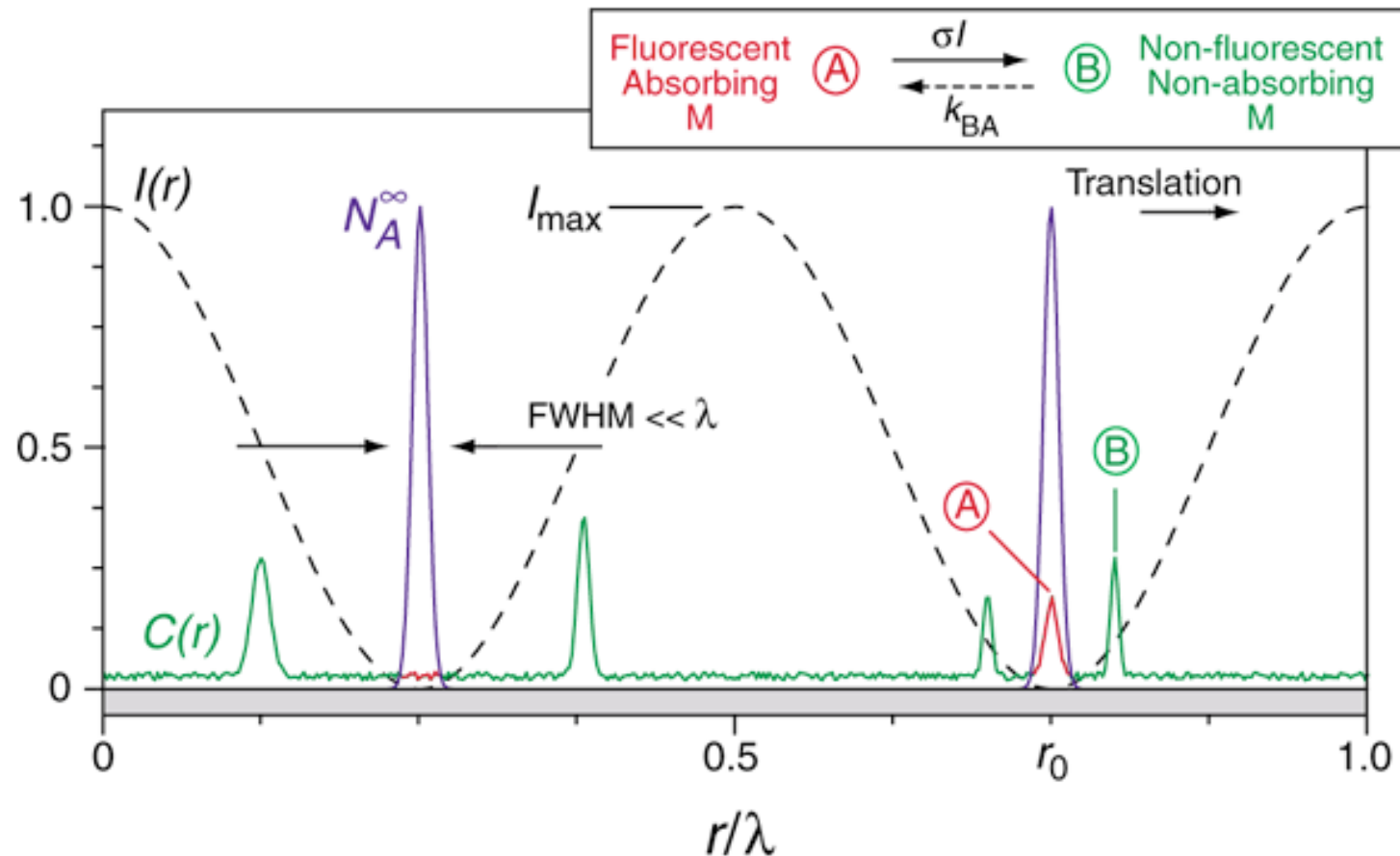
Willig, K. I., Rizzoli, S. O., Westphal, V., Jahn, R., & Hell, S. W. (2006). *Nature Cell Biology*, 440(7086), 935–939. <http://doi.org/10.1038/nature04592>

## Super-resolution 9: Confocal STED microscopy



## Super-resolution 10: RESOLFT

Use of another “dark” molecular state to break the diffraction limit.  
Molecules outside the intensity minimum are switched off

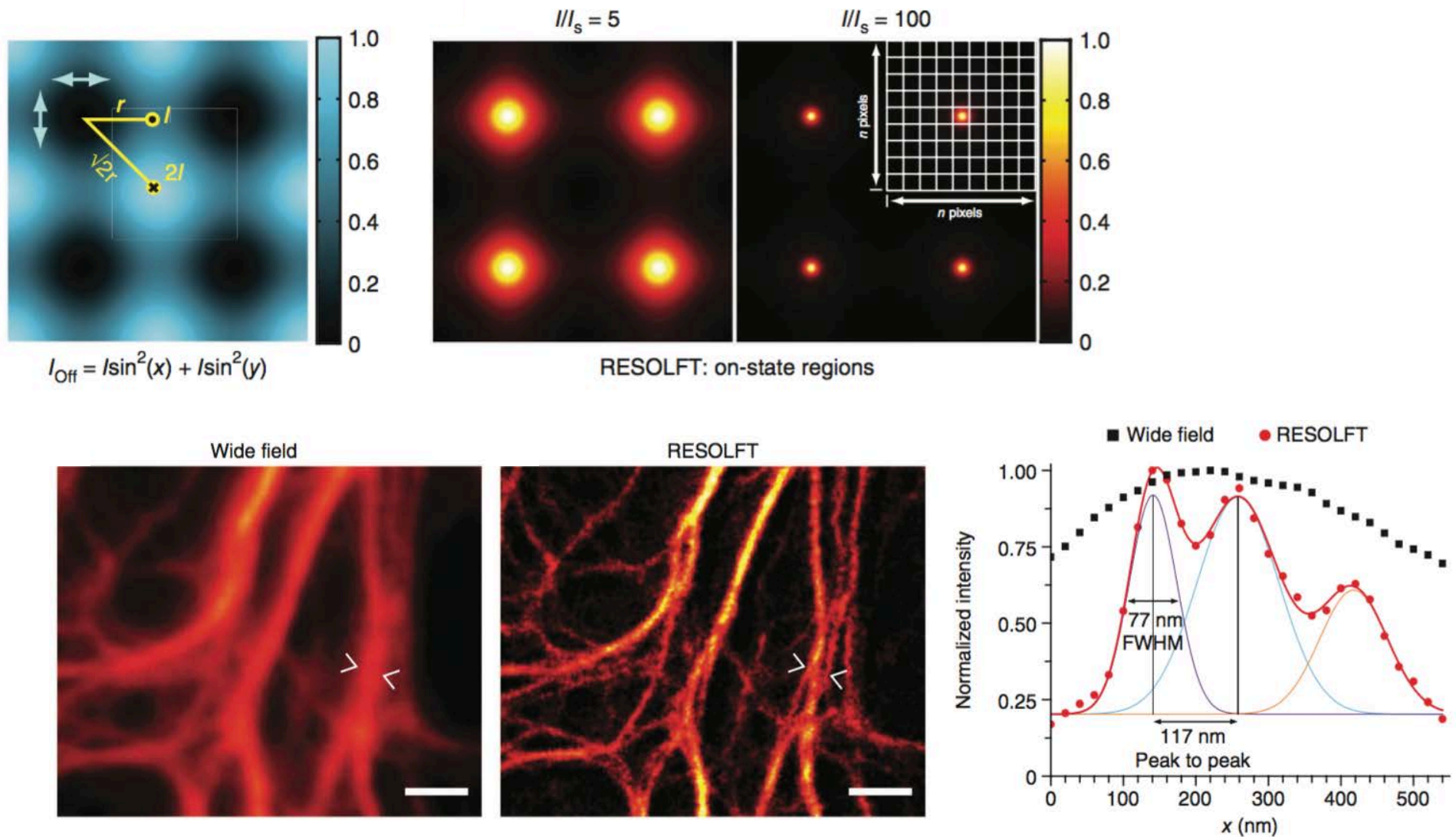


The energy required to switch off the molecule are low compare to STED:

- Less damage to the sample
- Possibility to use pattern for illumination

# Super-resolution 11: RESOLFT

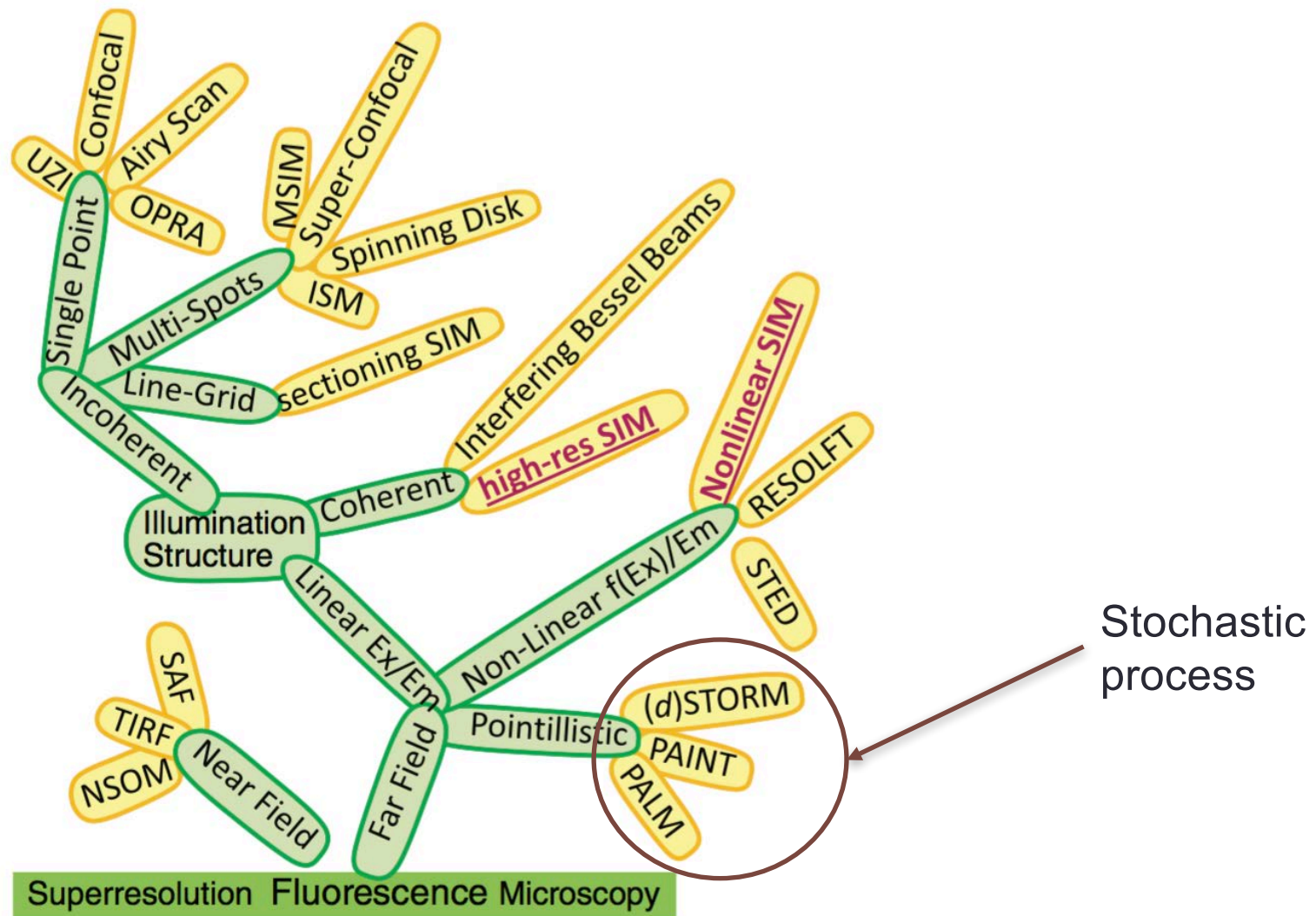
The low energy required to populate the dark state allow to use a network of foci



Chmyrov, A. *et al.* Nanoscopy with more than 100,000 'doughnuts'. *Nat Methods* **10**, 737–740 (2013).



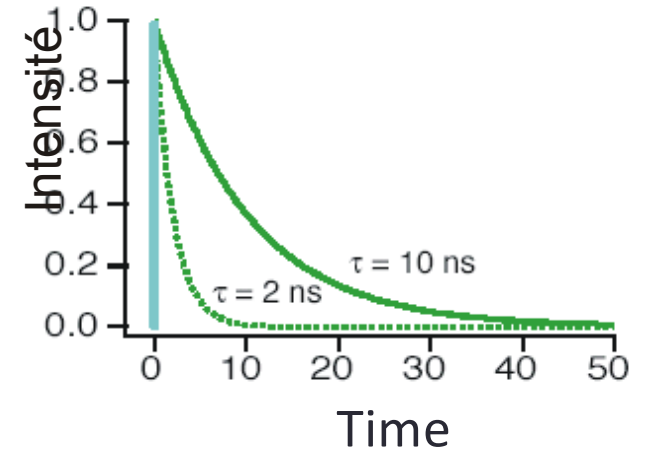
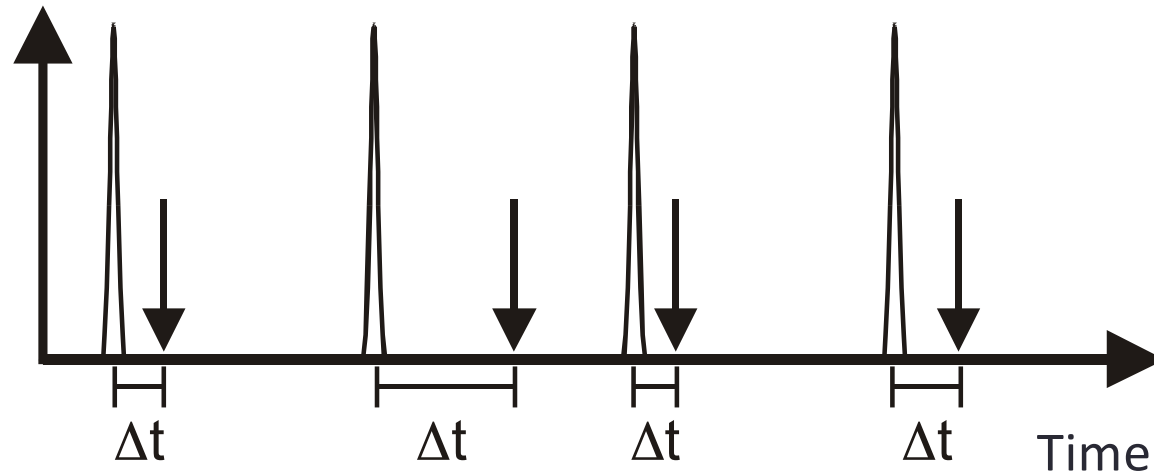
# Super-resolution



# Single-molecule detection and fluorescence signal correlation

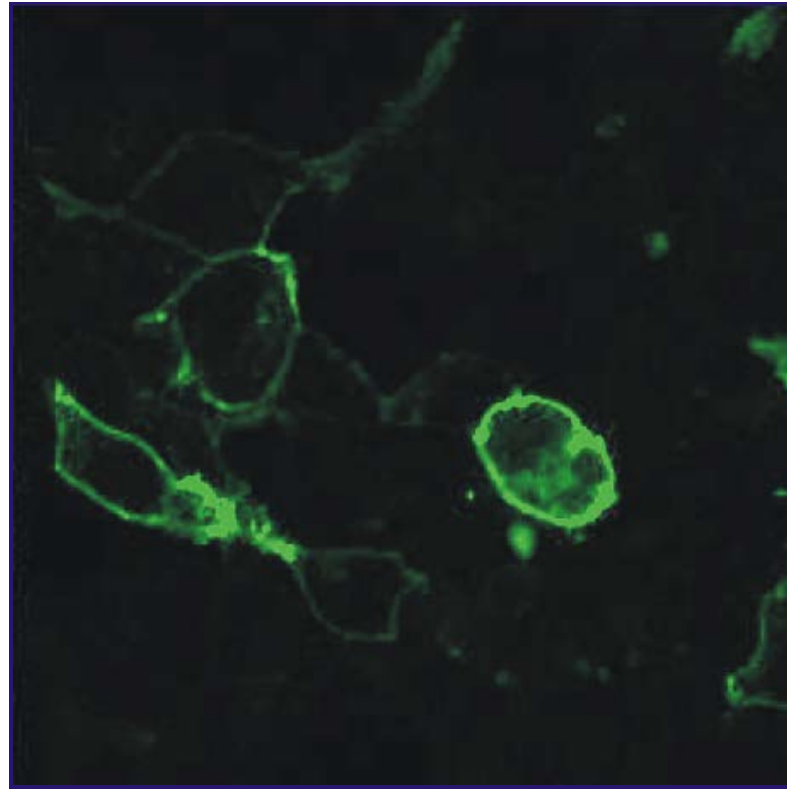


# Fluorescence lifetime



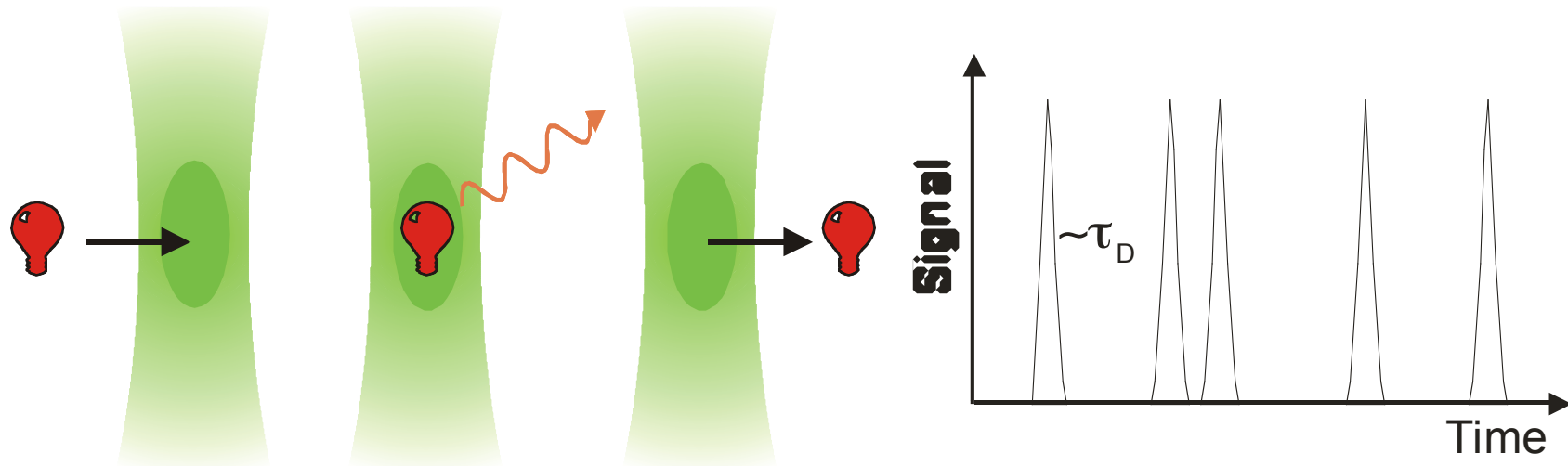
- The fluorescence lifetime is directly connected to the fluorescence quantum yield. This is a way to measure variations in the fluorescence quantum yield that is less sensitive to intensity fluctuations.
- The fluorescence quantum yield is strongly influenced by the environment (hydrophilic, hydrophobic).

## Rapidly diffusing molecules: Single-molecule detection (SMD) and fluorescence correlation spectroscopy (FCS)



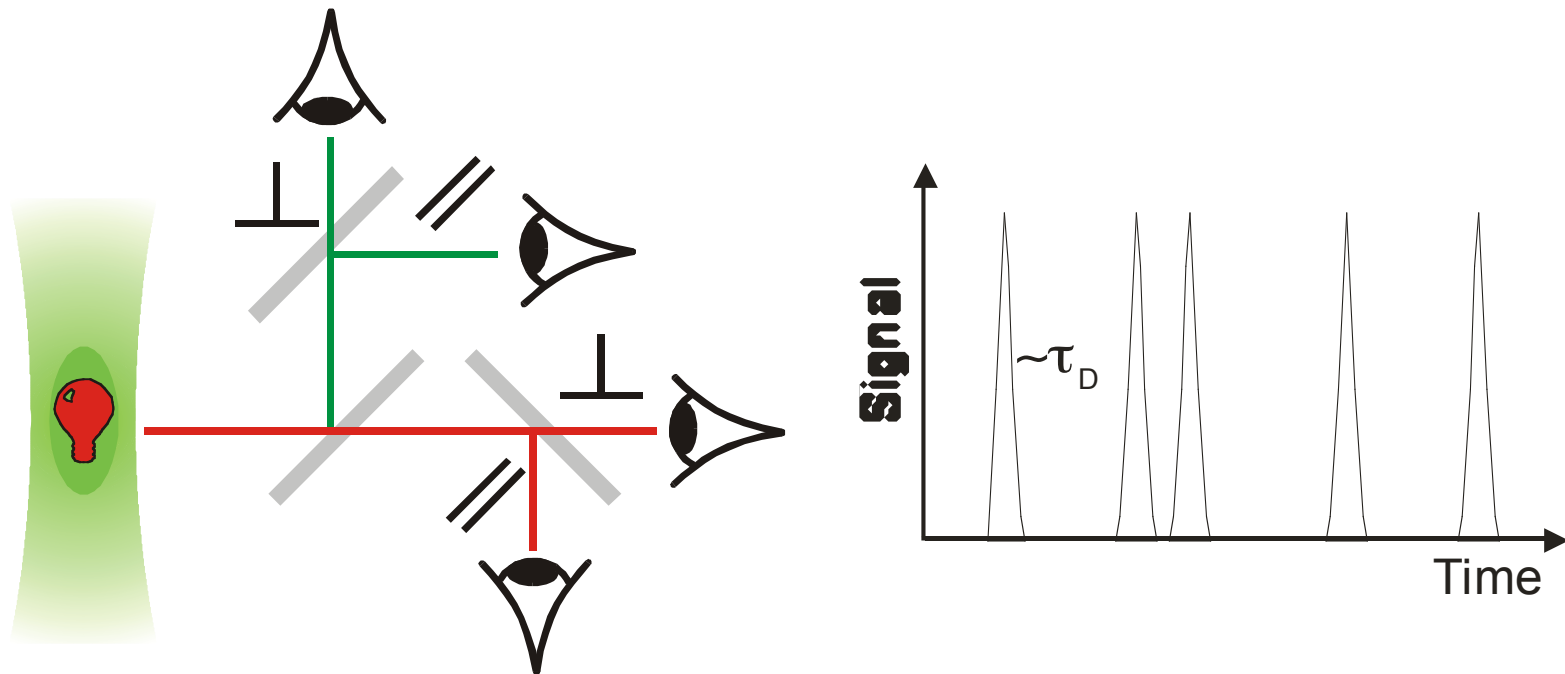
- Diffusion is too fast to be measured by single-molecule tracking
- High concentration of label
- Single-molecule measurement in solution

## Confocal volume fixed at a particular location



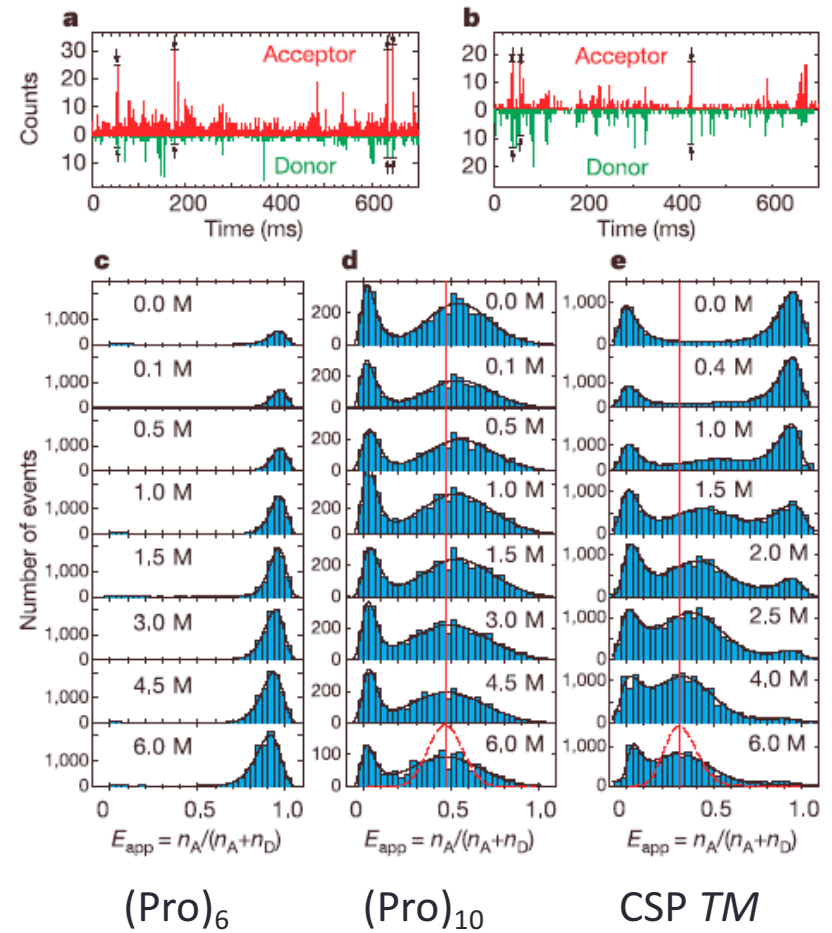
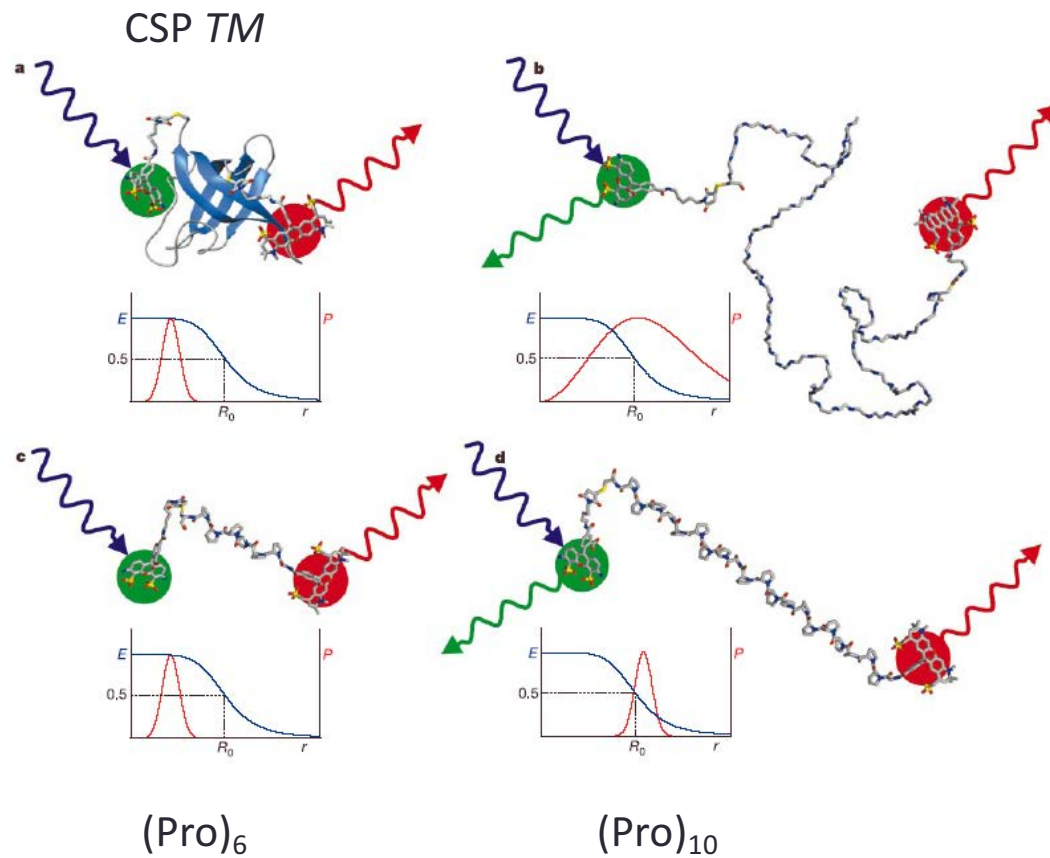
- Remark: The signal emitted by a single molecule when it is diffusing through the confocal volume is extremely small. It is necessary to average over several single molecules.

# Multiparameter Fluorescence Detection (MFD) or Single-Molecule Detection (SMD)



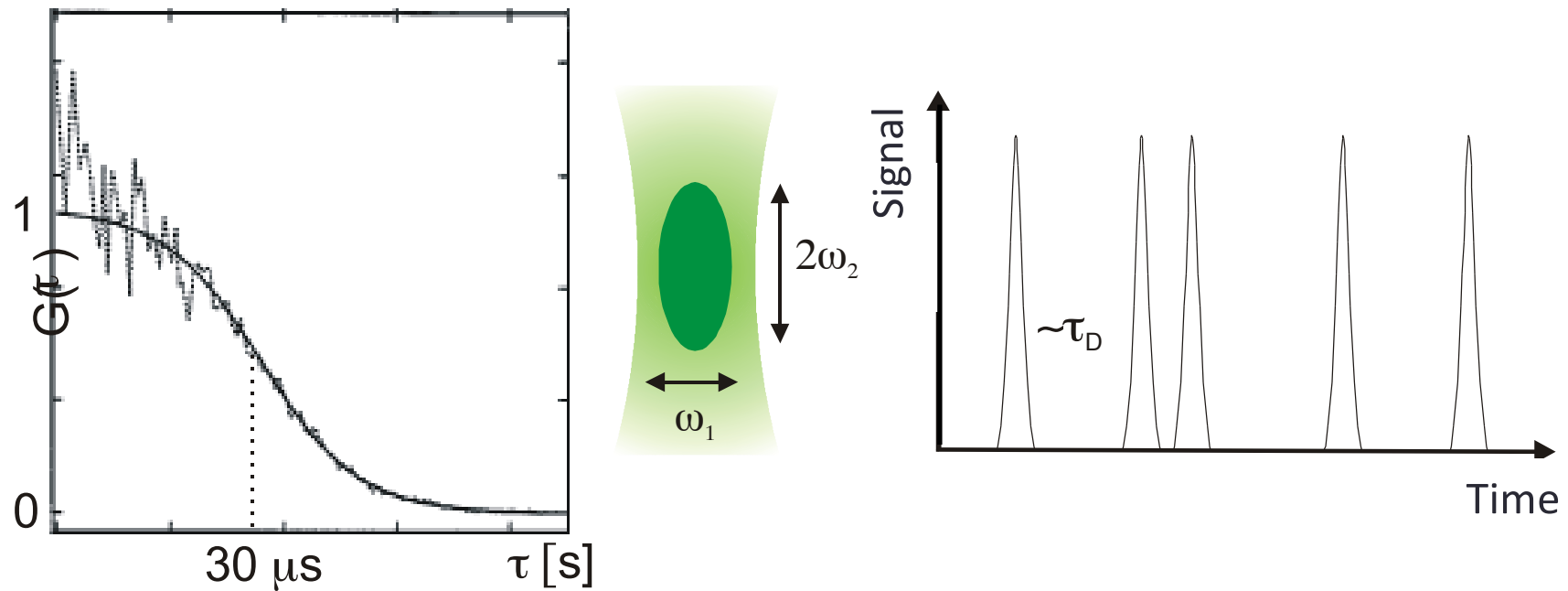
- Many parameters are simultaneously measured: colour, FRET efficiency, polarization (anisotropy), fluorescence lifetime, arrival time (absolute time), intensity, diffusion.
- By correlating the parameters, novel observations can be made.

# Example: protein folding



B. Schuler, E.A. Lipman, W.A. Eaton, *Nature* **419**, 743 (2002)

# Fluorescence autocorrelation function

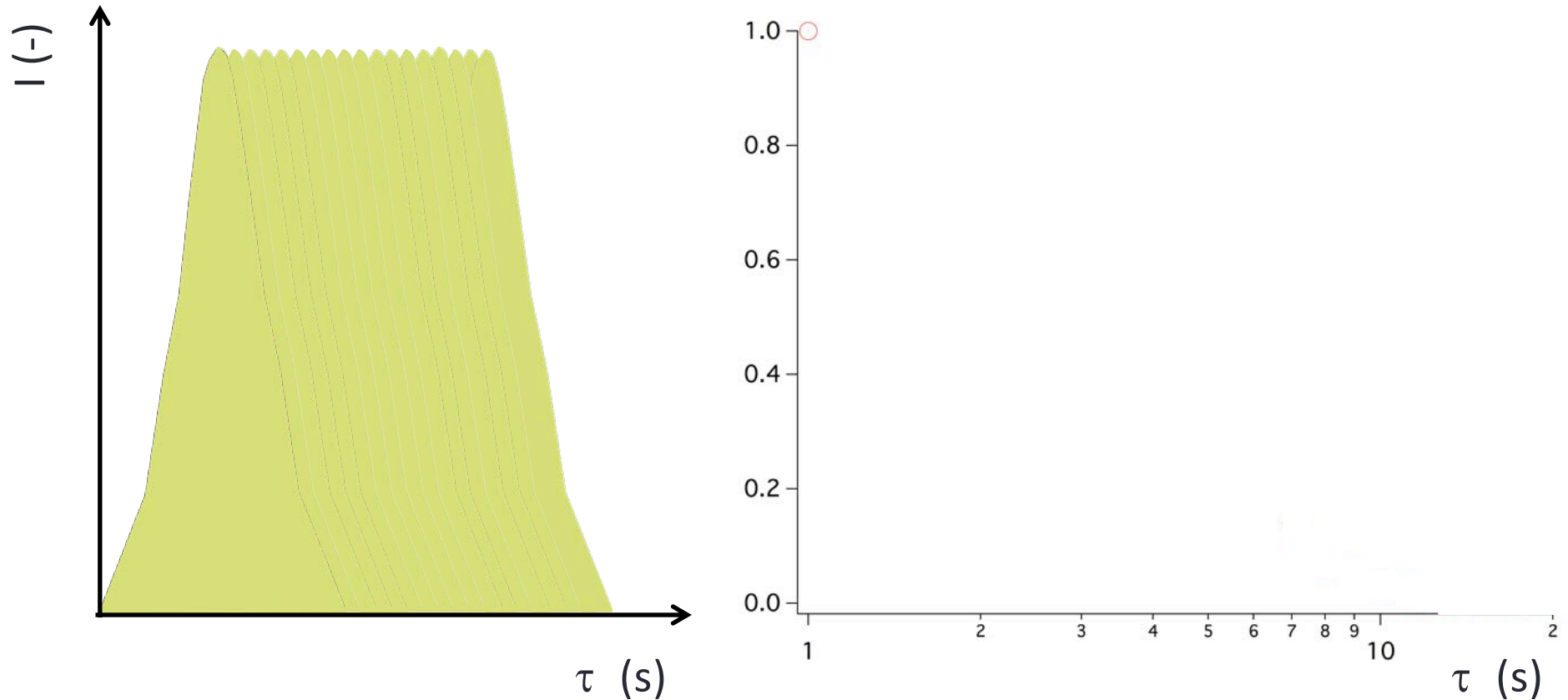


$$G'(\tau) = \langle I(t) \cdot I(t + \tau) \rangle = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T \langle I(t) \cdot I(t + \tau) \rangle dt$$

- $G'$  denotes the non-normalized autocorrelation function,  $t$  the time difference,  $I$  the intensity and  $T$  the measurement time



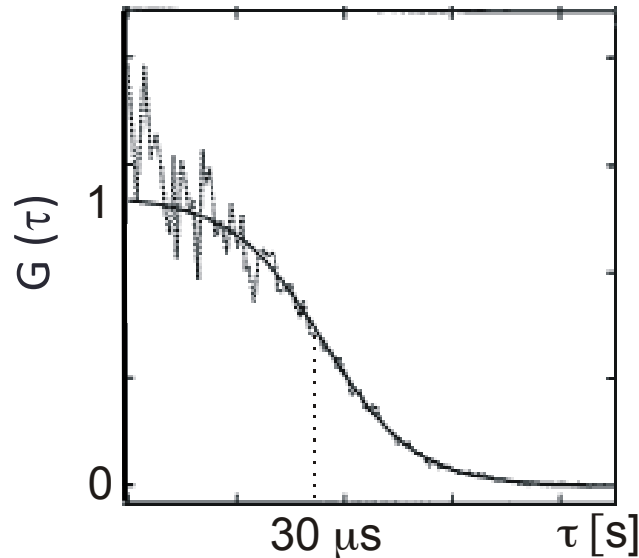
# Fluorescence autocorrelation function



$$G'(\tau) = \langle I(t) \cdot I(t + \tau) \rangle = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T \langle I(t) \cdot I(t + \tau) \rangle dt$$

- $G'$  denotes the non-normalized autocorrelation function,  $t$  the time difference,  $I$  the intensity and  $T$  the measurement time

## Influence of diffusion

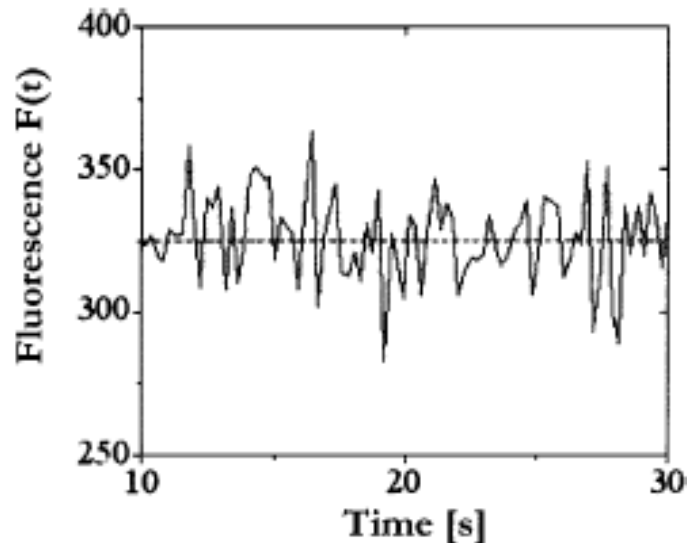


$$\tau_D = \frac{\omega_1^2}{4D} \quad D = \frac{k_B T}{6\pi\eta r} \quad r = \sqrt[3]{\frac{3M / N_A}{4\pi\rho}}$$

$$\frac{\tau_{D,\text{ref}}}{\tau_{D,\text{unknown}}} = \frac{D_{\text{unknown}}}{D_{\text{ref}}} = \sqrt[3]{\frac{M_{\text{ref}}}{M_{\text{unknown}}}}$$

- In the formulas:  $t_D$ : diffusion time,  $w_1$ : diameter of the focus,  $D$ : diffusion constant,  $M$ : molecular weight,  $N_A$ : Avogadro number,  $r$ : density,  $r$ : hydrodynamic radius,  $\eta$ : viscosity. This model is only correct for spherical molecules.
- For proteins  $r=1.2 \text{ g/cm}^3$ ; For nucleic acids  $r=1.8 \text{ g/cm}^3$ ; For lipids  $r=0.9\text{-}1.1 \text{ g/cm}^3$ .
- When the molecular weight changes by a factor of two, the diffusion constant only changes by a factor of 1.26 (detection limit).
- With  $w_1=230 \text{ nm}$ ,  $t_D=37 \text{ ms}$  for a usual dye ( $M=550 \text{ D}$ ,  $D=360 \text{ mm}^2/\text{s}$ ) and 235 ms for an antibody ( $M=140 \text{ kD}$ ).

## Extension to multiple molecules: fluorescence correlation spectroscopy (FCS)



$$G'(\tau) = \langle I(t) \cdot I(t + \tau) \rangle$$

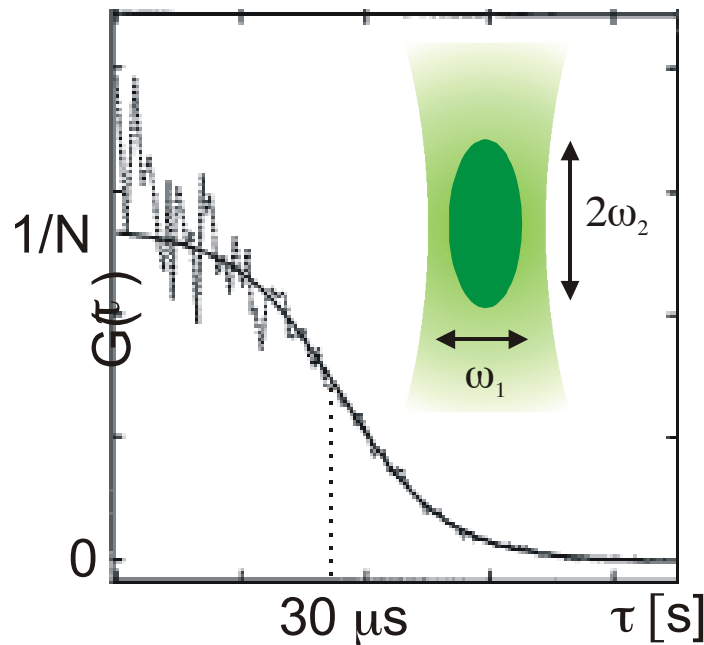
$$I(t) = I + \langle \delta I(t) \rangle$$

$$G'(\tau) = \langle I \rangle^2 + \langle \delta I(t) \delta I(t + \tau) \rangle$$

$$G(\tau) = \frac{G'(\tau)}{\langle I \rangle^2} - 1 = \frac{\langle \delta I(t) \delta I(t + \tau) \rangle}{\langle I \rangle^2} \quad \text{ou} \quad G(\tau) = \frac{G'(\tau)}{\langle I \rangle^2}$$

- In the formulas:  $G$ : normalized autocorrelation function.  $\delta I$ : intensity fluctuation from the averaged intensity.

# Fluorescence autocorrelation function for multiple molecules



The number of molecules in the confocal volume fluctuates with poissonian statistics

$$\lim_{x \rightarrow 0} \langle \delta I(t) \delta I(t + \tau) \rangle / \langle I^2 \rangle = \frac{1}{N}$$

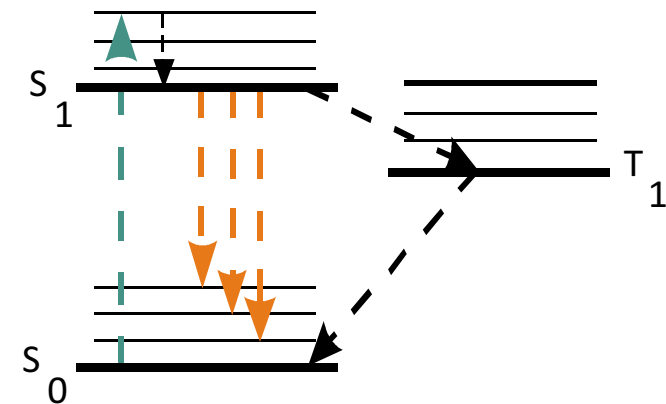
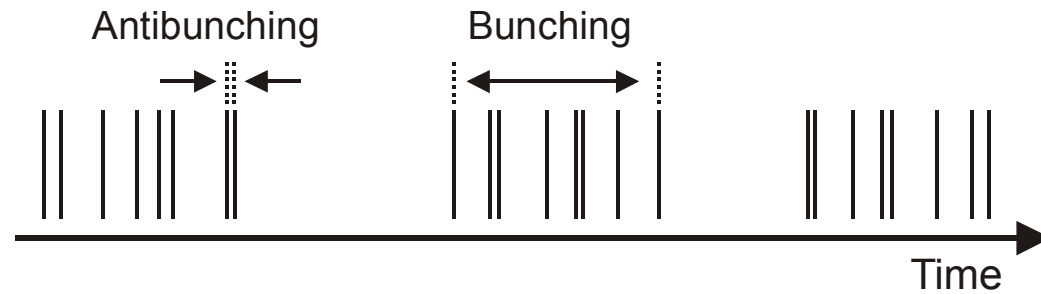
For a gaussian profile in the confocal volume:

$$G(\tau) = \frac{1}{N} \cdot \frac{1}{1 + 4D\tau / \omega_1^2} \left[ \frac{1}{1 + 4D\tau / \omega_2^2} \right]^{1/2}$$

$$\omega_2 = S \cdot \omega_1 \quad V = \omega_1^2 \cdot \pi \cdot 2 \cdot \omega_2 = 2 \cdot \pi \cdot S \cdot \omega_1^3 \quad c = \frac{N}{N_A \cdot V}$$

- In the formulas:  $N$ : averaged number of molecules in the confocal volume,  $S$ : structure parameter,  $V$ : volume,  $c$ : concentration.
- $S$  typically is 5;  $\omega_1$  is diffraction-limited, i.e.  $\sim 0.5\lambda = 250$  nm for a laser at 500 nm;  $S$  and  $\omega_1$  are determined using a standard.

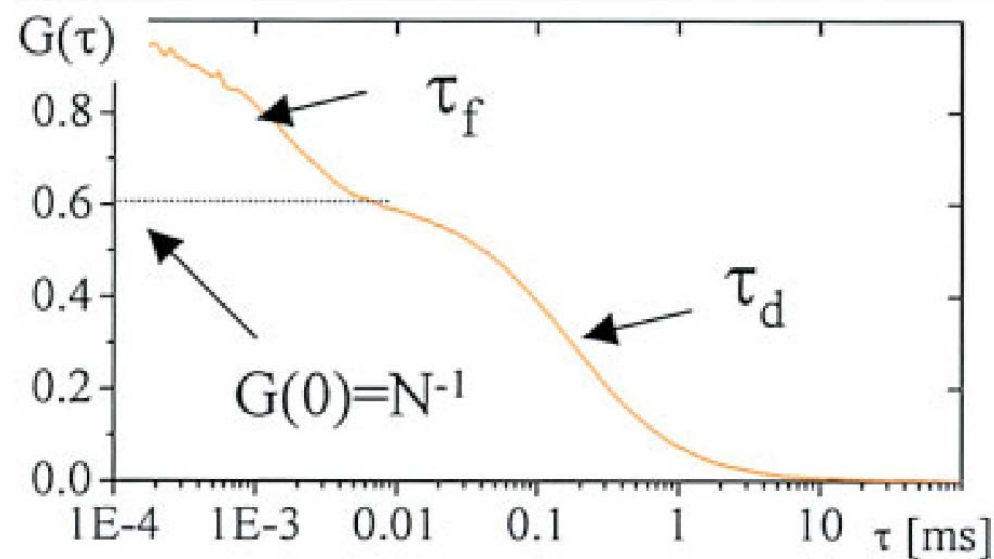
# Influence of the triplet state



The presence of the triplet state adds a term to the autocorrelation function:

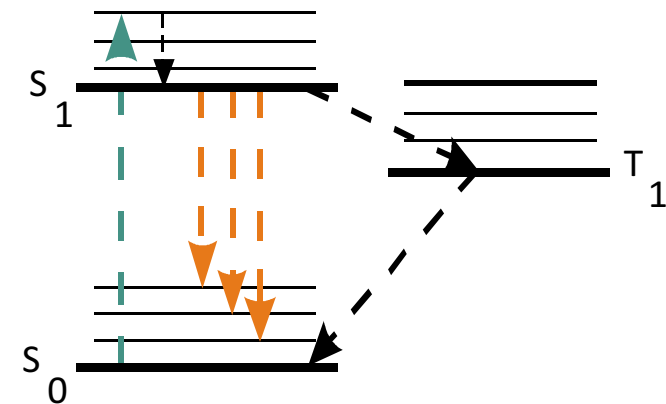
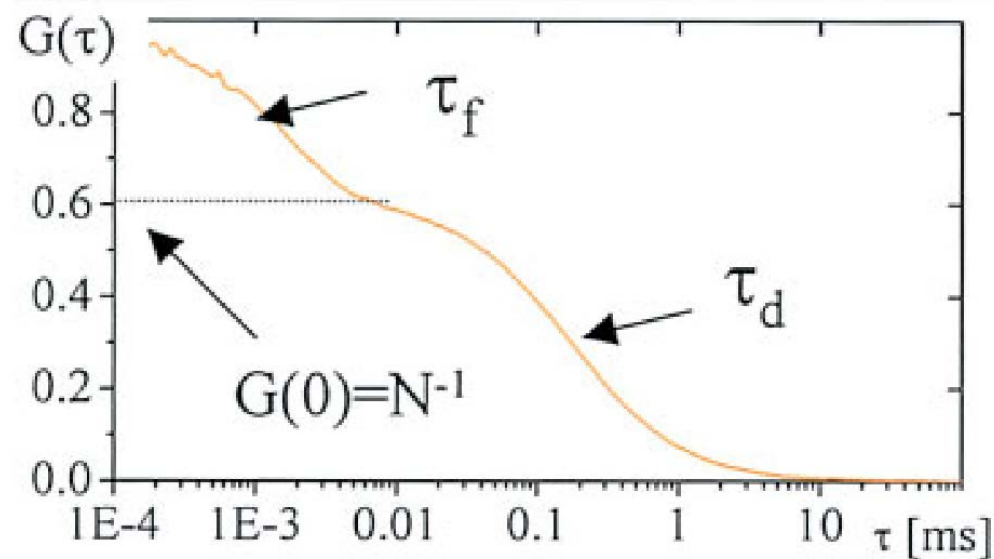
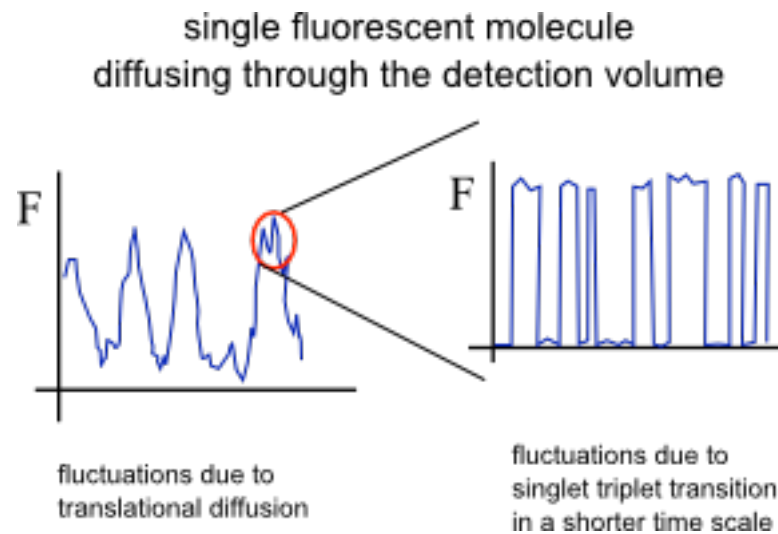
$$\frac{1 - F + F \exp(-\tau / \tau_T)}{1 - F}$$

With  $F$ : fraction of molecules in the triplet;  $t_T$ : triplet lifetime





# Influence of the triplet state

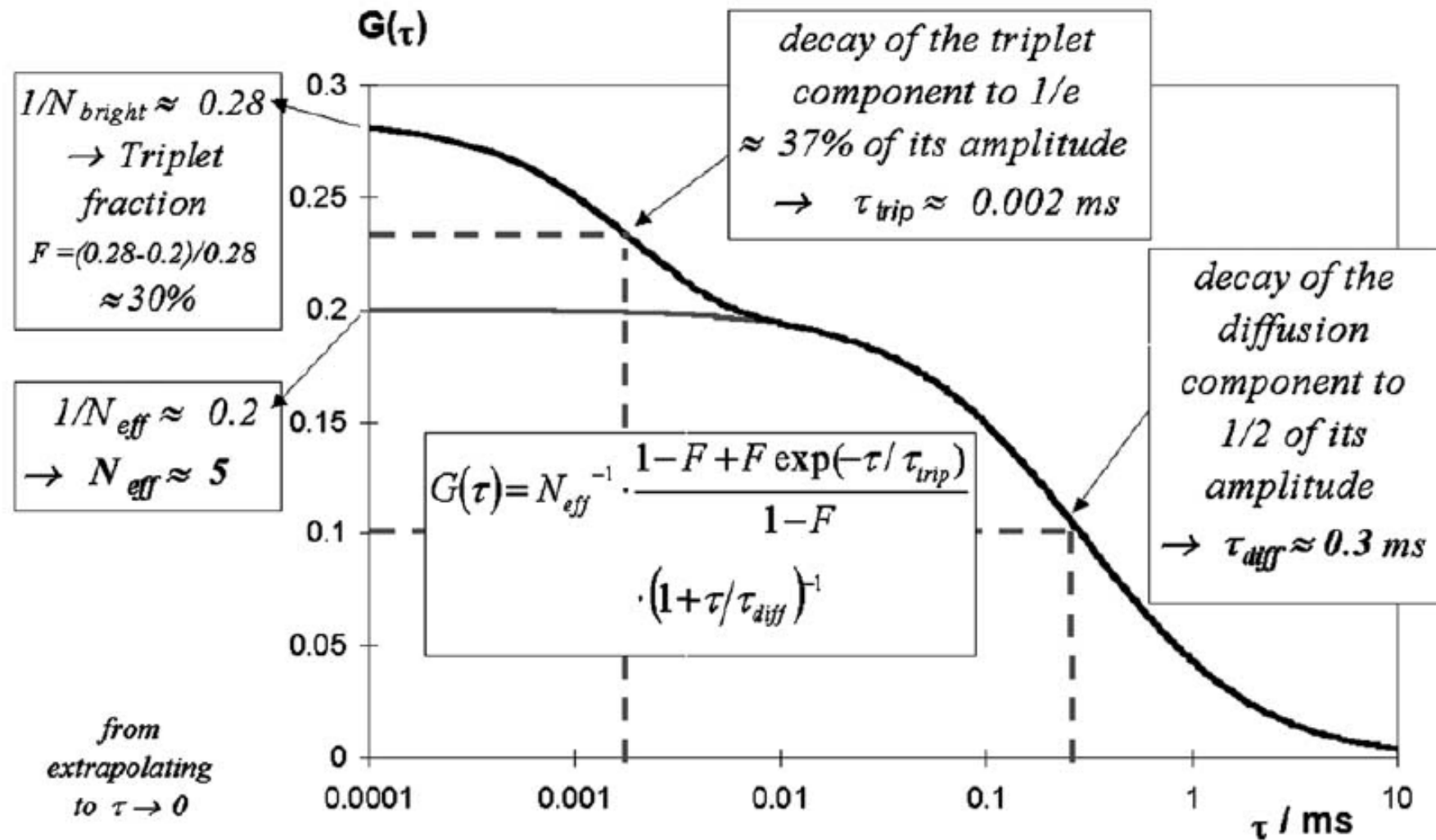


The presence of the triplet state adds a term to the autocorrelation function:

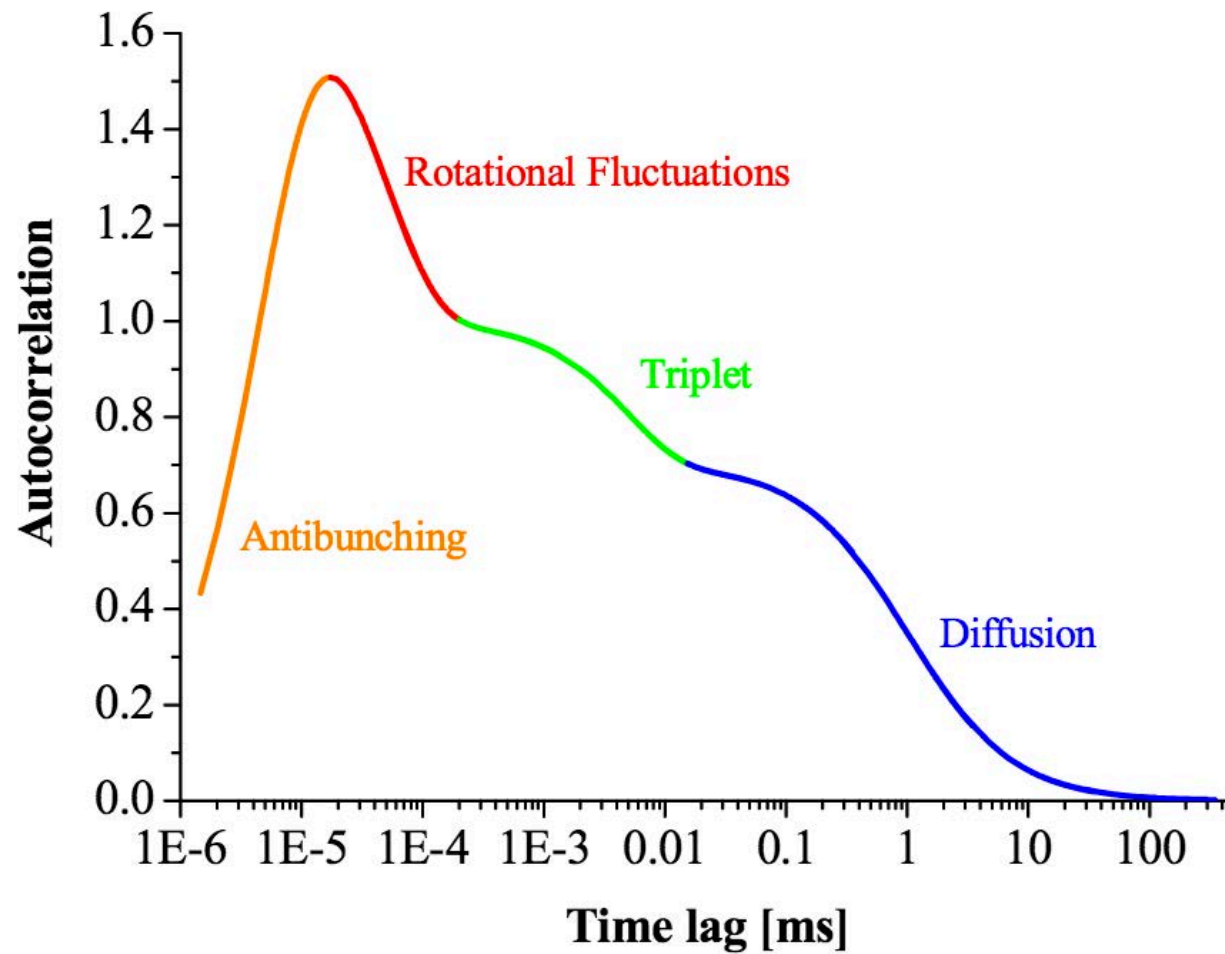
$$\frac{1 - F + F \exp(-\tau / \tau_T)}{1 - F}$$

With  $F$ : fraction of molecules in the triplet;  $t_T$ : triplet lifetime

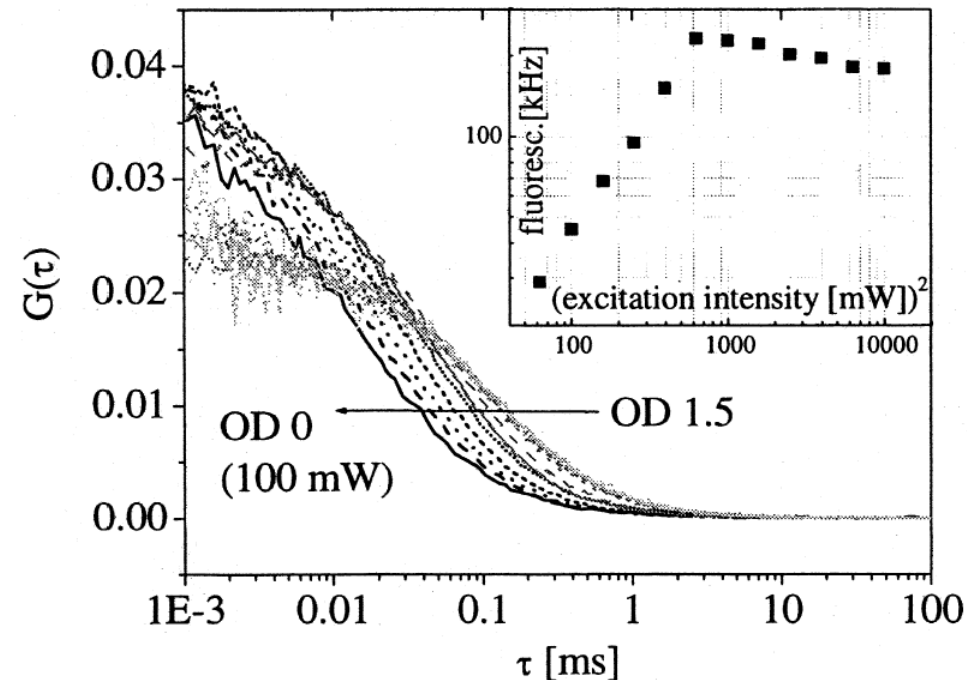
## Fluorescence autocorrelation function: summary



## Fluorescence autocorrelation function: summary

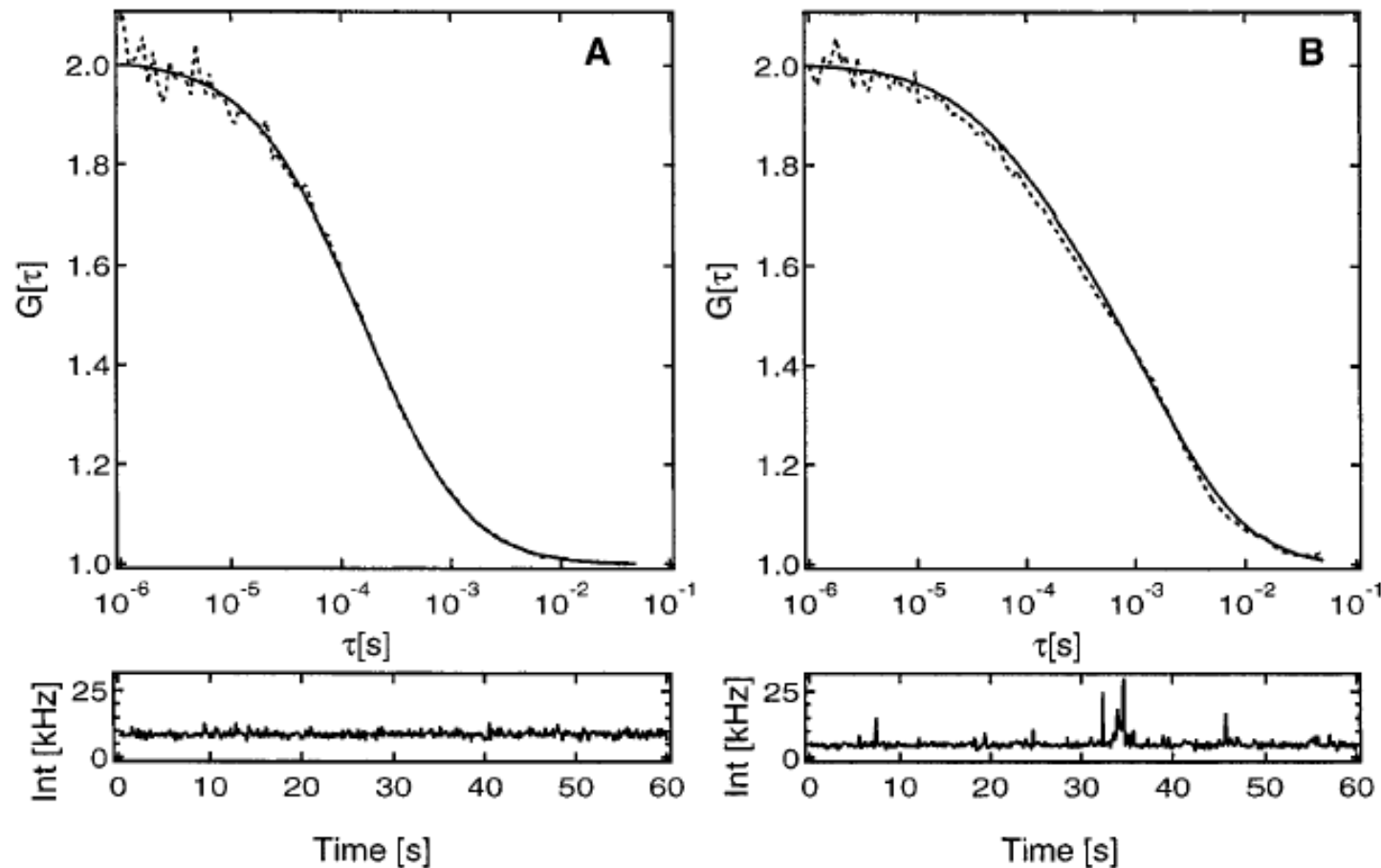


# Influence of photobleaching



- Photobleaching yields apparently higher diffusion constants. Moreover, the shape of the curve at longer times is modified. It is important to work well below saturation intensity (factor 5-10).
- Working near saturation intensity can also yield shorter apparent diffusion constants if photobleaching is negligible.
- It is always wise to control that the excitation intensity doesn't have any influence on the autocorrelation function.

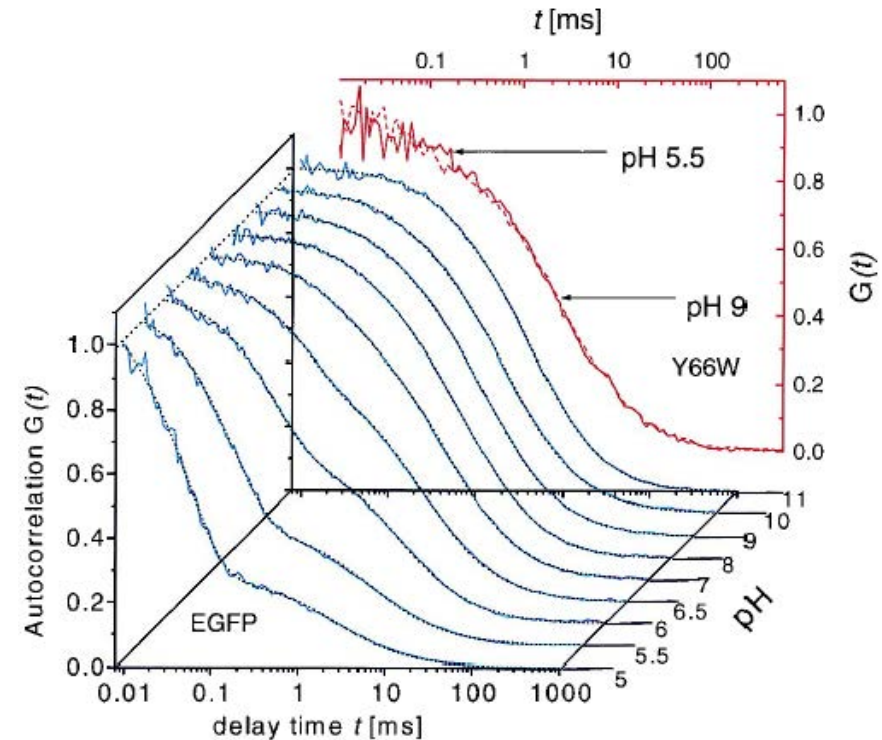
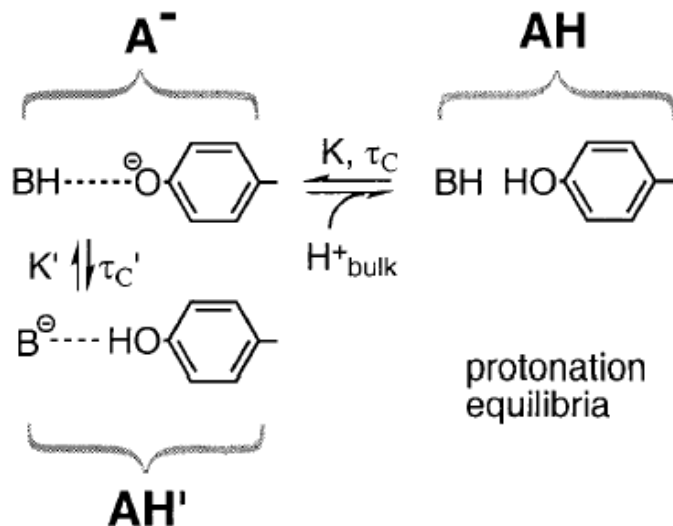
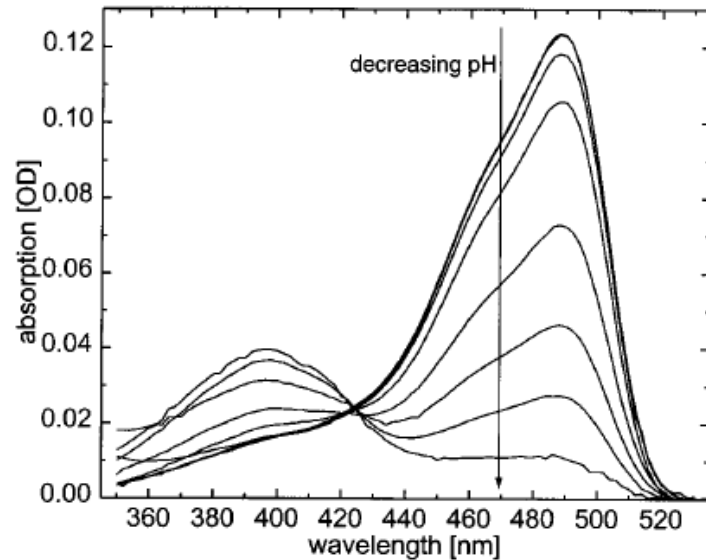
## Example: Measurements of binding constants



- Principle: The molecular weight of the labelled molecule drastically changes upon binding or reaction. Typical case: The binding of small ligands on receptors.
- Since the fluorescence from the various species is not correlated, the autocorrelation function is the sum of the autocorrelation functions of the different species.

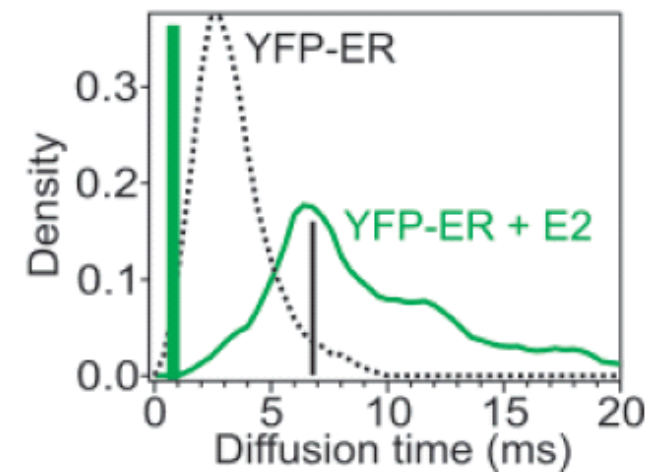
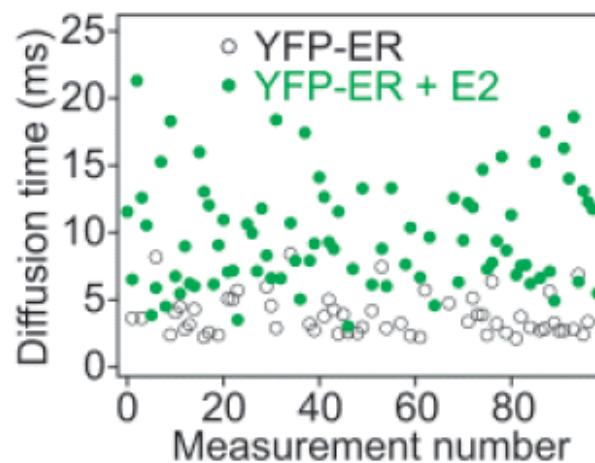
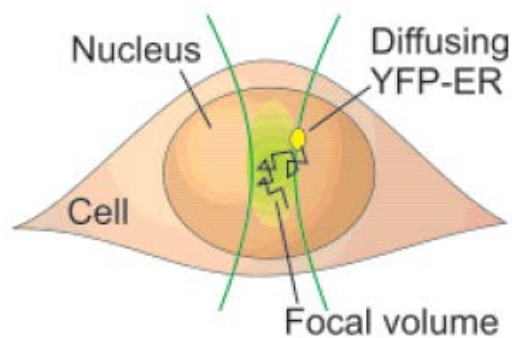
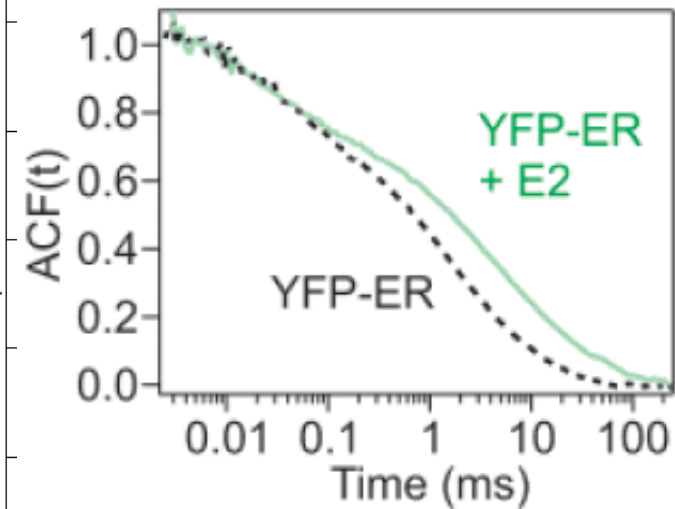
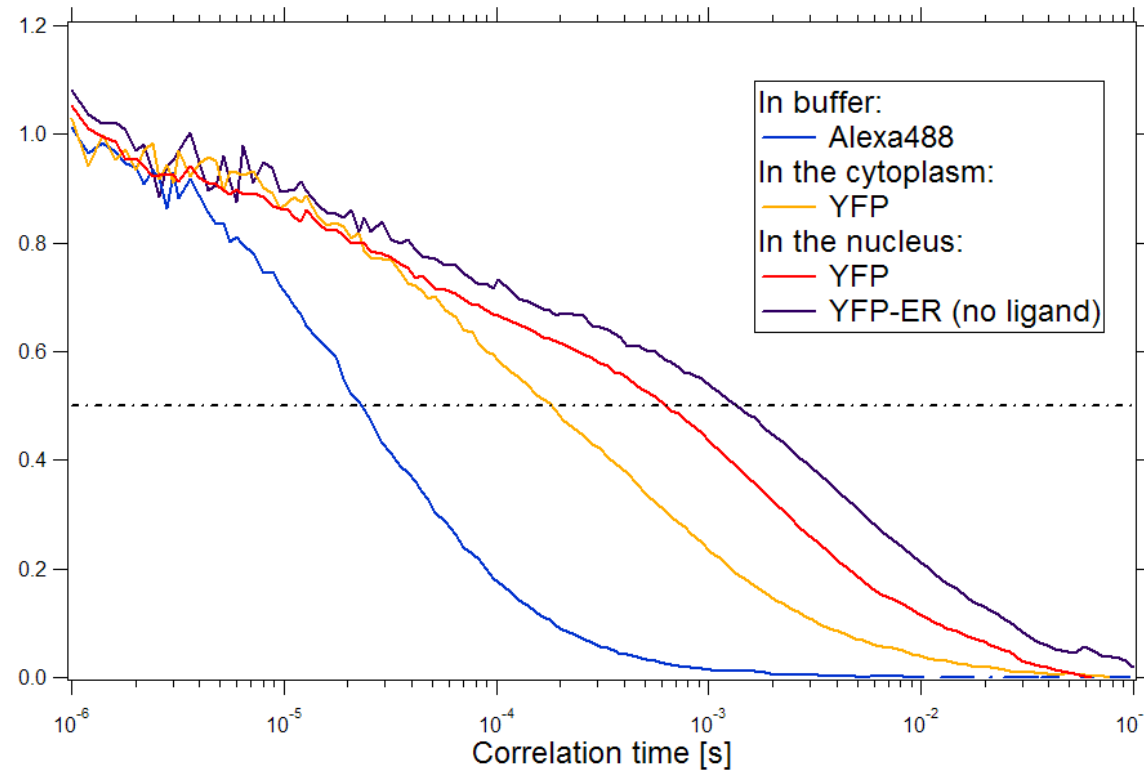


## Example: photophysics of GFP

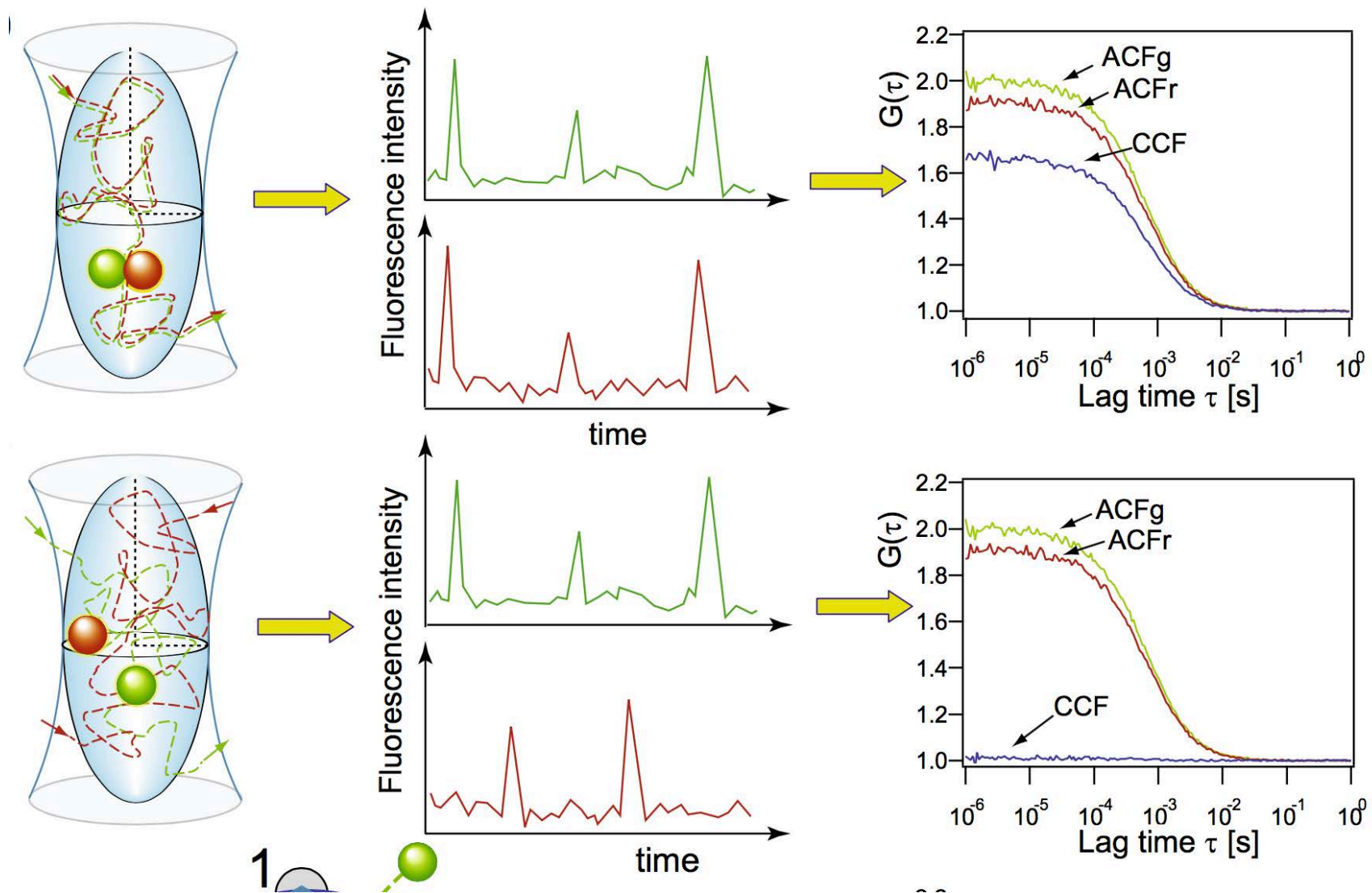


- Dynamics of transition between two states can be observed by FCS if one of the two states is non-fluorescent
- The fluorescence autocorrelation function directly yields the respective fractions in the two states

## Example: The estrogen receptor



# Cross-correlation

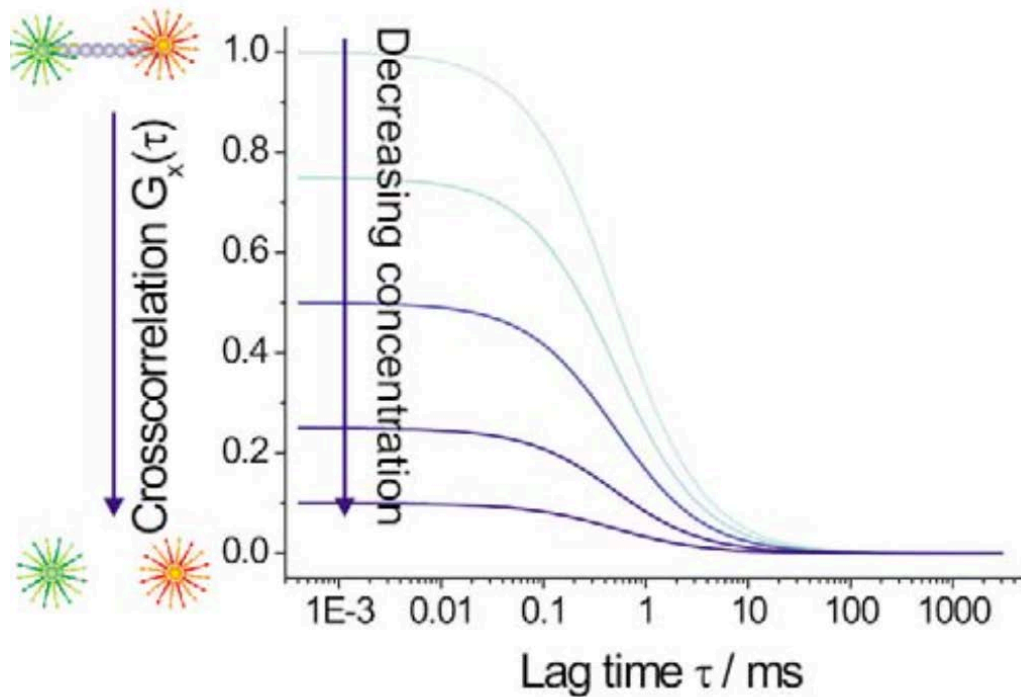


# Cross-correlation

(d)

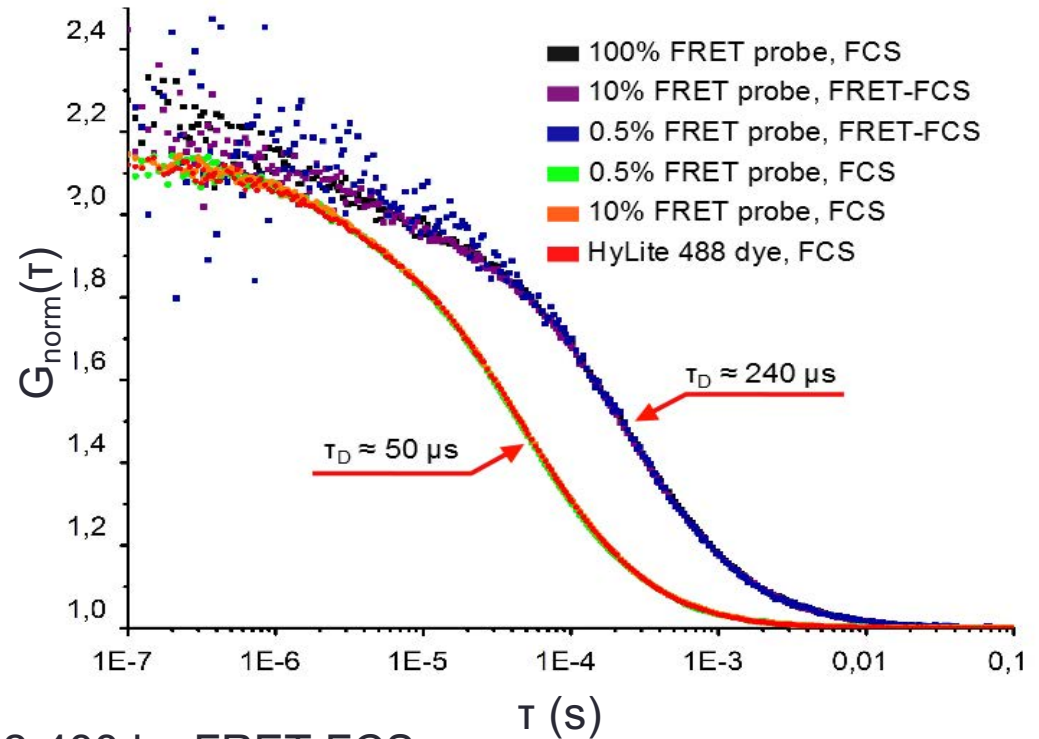
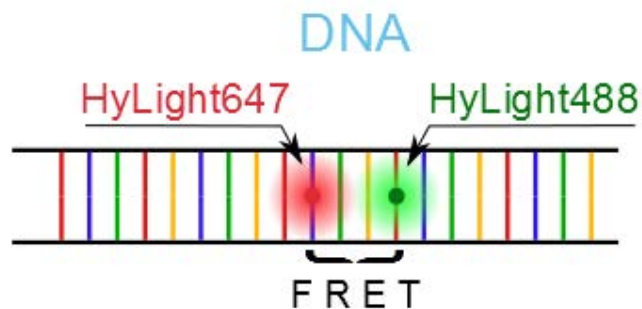
$$G_x(\tau) = \frac{\langle F_{\text{green}}(t) F_{\text{red}}(t+\tau) \rangle}{\langle F_{\text{green}}(t) \rangle \langle F_{\text{red}}(t) \rangle} - 1$$

Concentration of dimers in solution

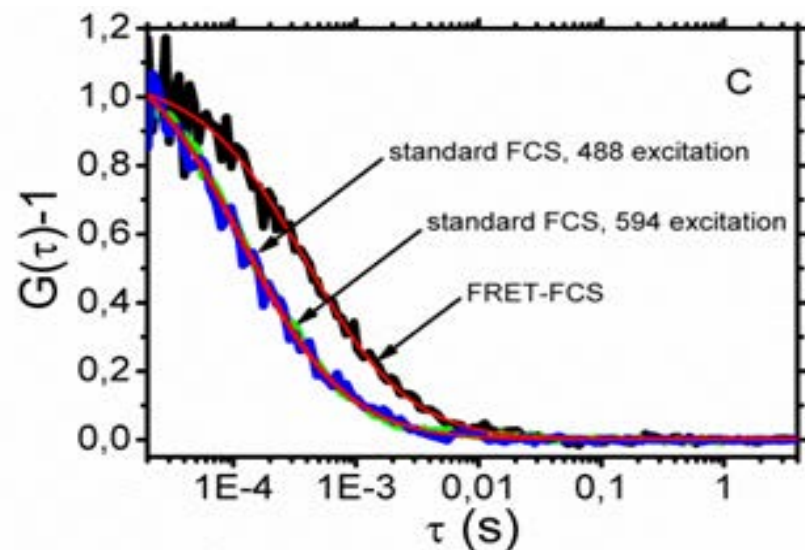


# FRET-FCS

Detection of weakly interacting molecules in solution



Detection of oligomers of A $\beta$ 42-647 and A $\beta$ 42-488 by FRET-FCS

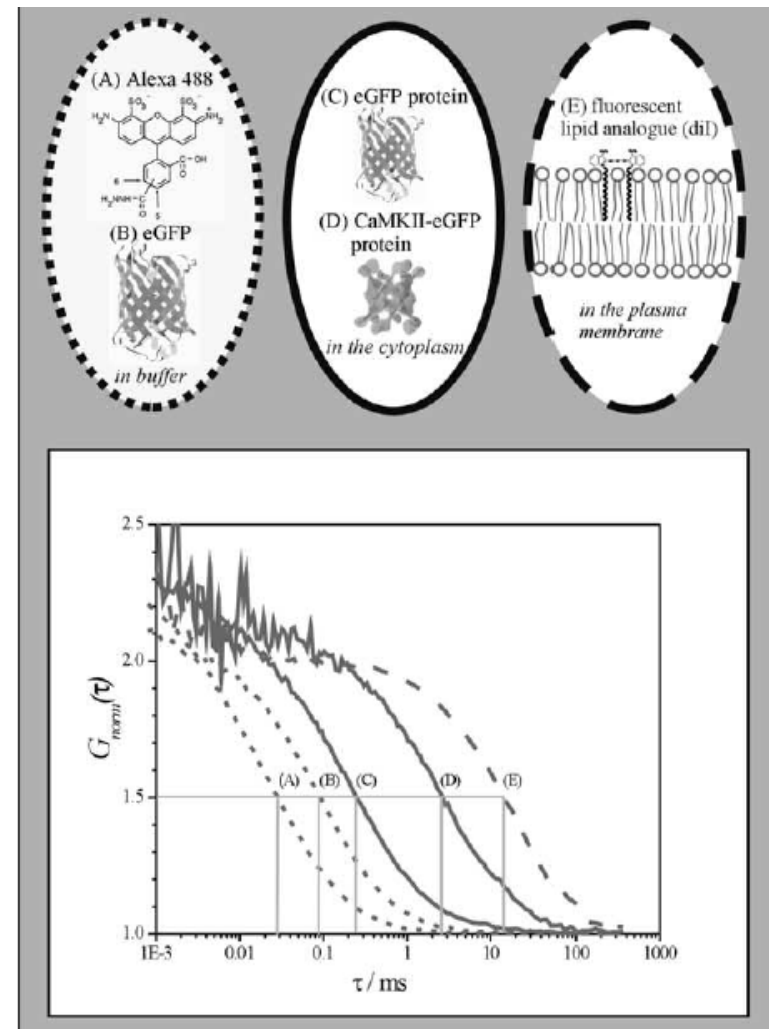
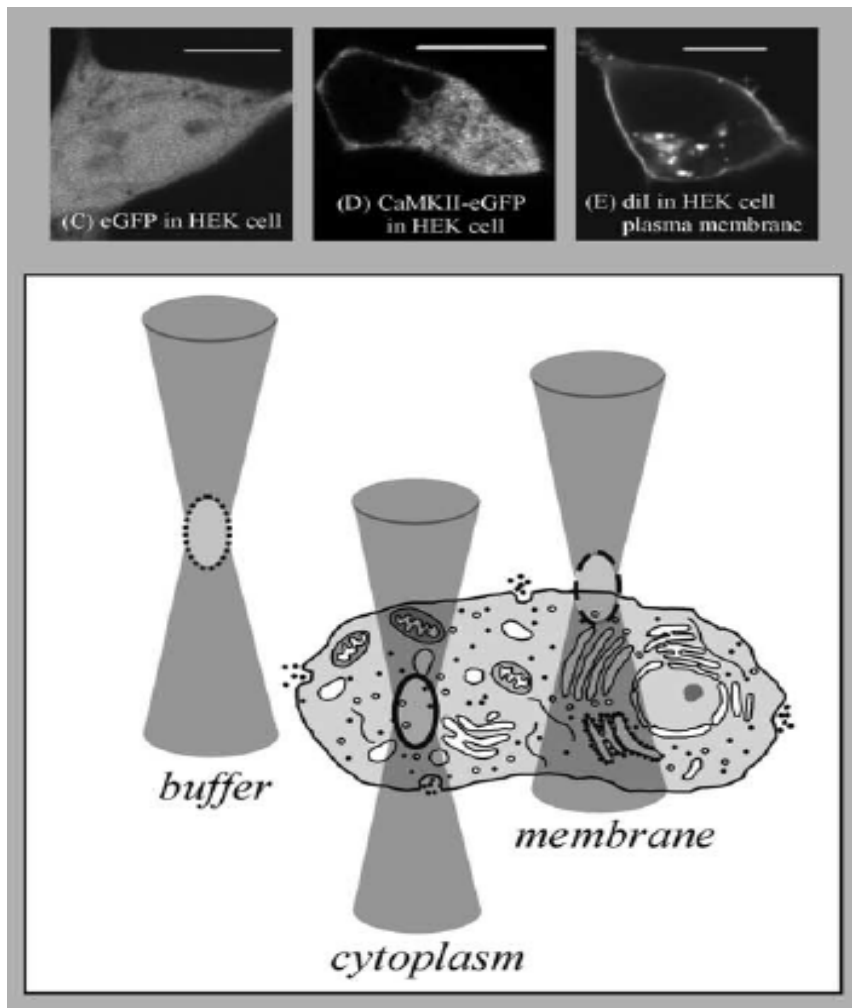


Amyloids  $\beta$  aggregation is very difficult to detect in solution:

The contrast of FRET-FCS is sufficient to detect very low aggregation



# Measurements on membranes



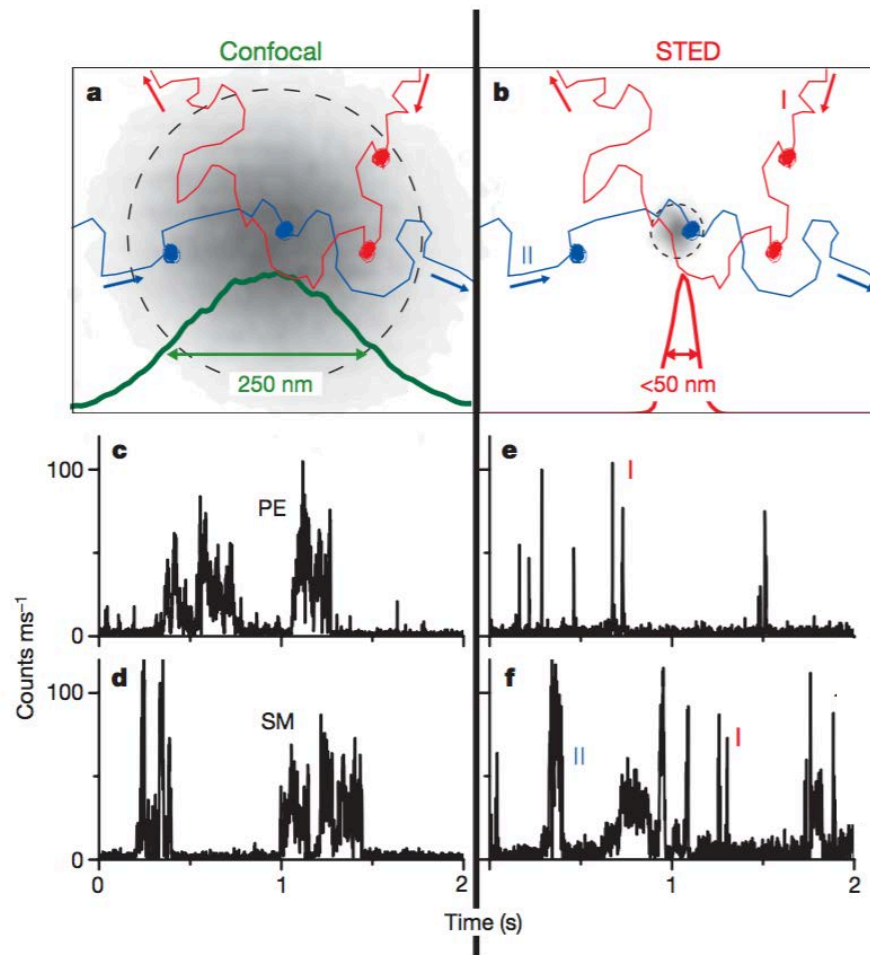
$$G(\tau) = \frac{1}{N} \cdot \frac{1}{1 + 4D\tau / \omega_1^2}$$

2D diffusion of membrane proteins is slow for conventional FCS

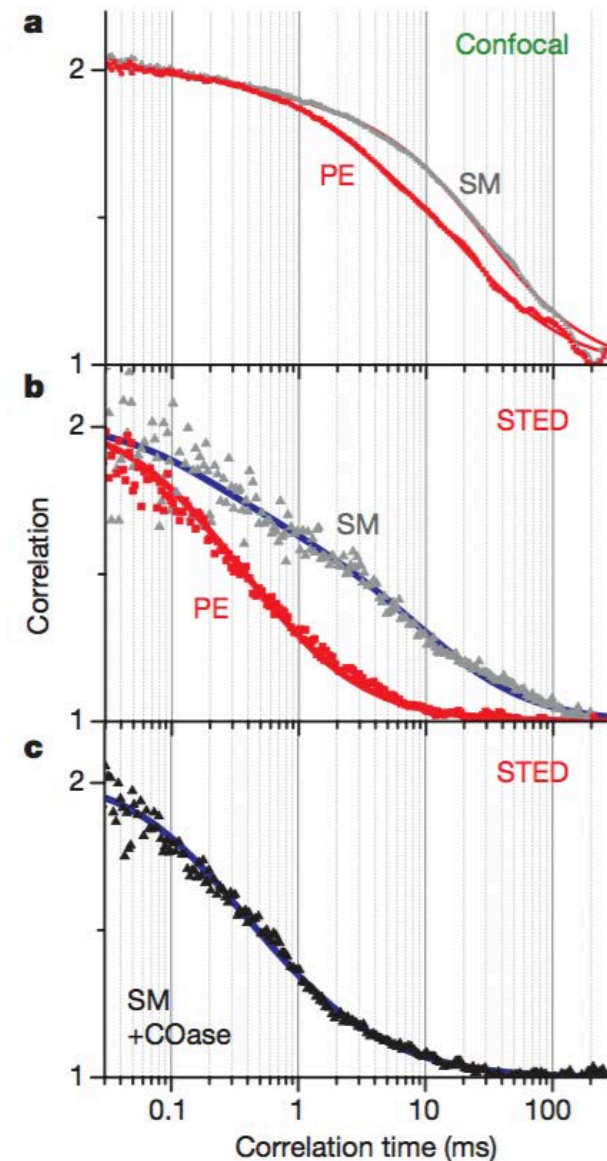
# STED FCS (2D diffusion)

Illumination volume is reduced

- Access to smaller diffusion coefficient
- Access to mesoscale structures

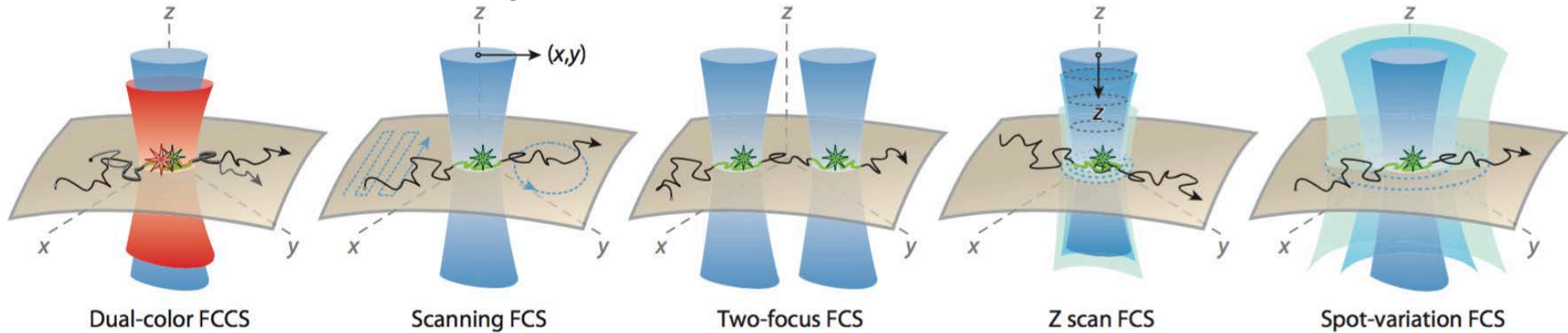


Diffusion of sphingomyelin and phosphatidylethanolamine lipids in the plasmae membrane

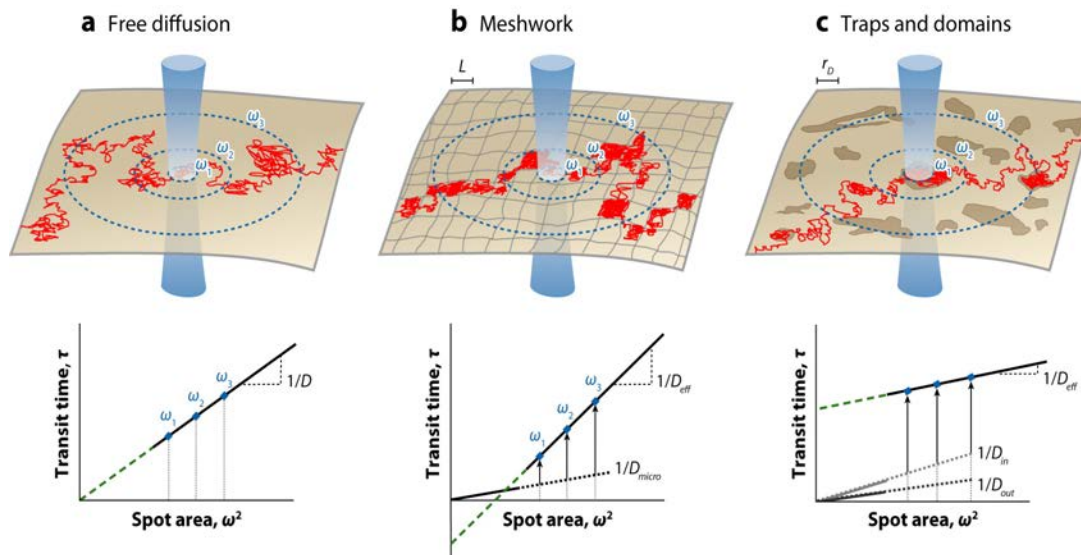


# FCS-Toolbox

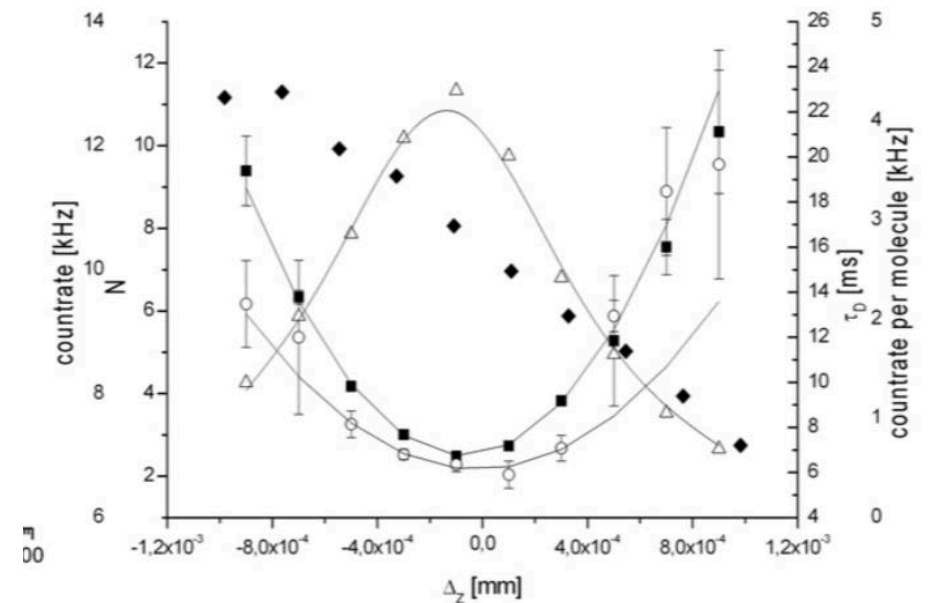
Standard FCS is not ideal for the detection of immobile molecule, domains or anomalous diffusion. Several methods gives more information about the studied molecule



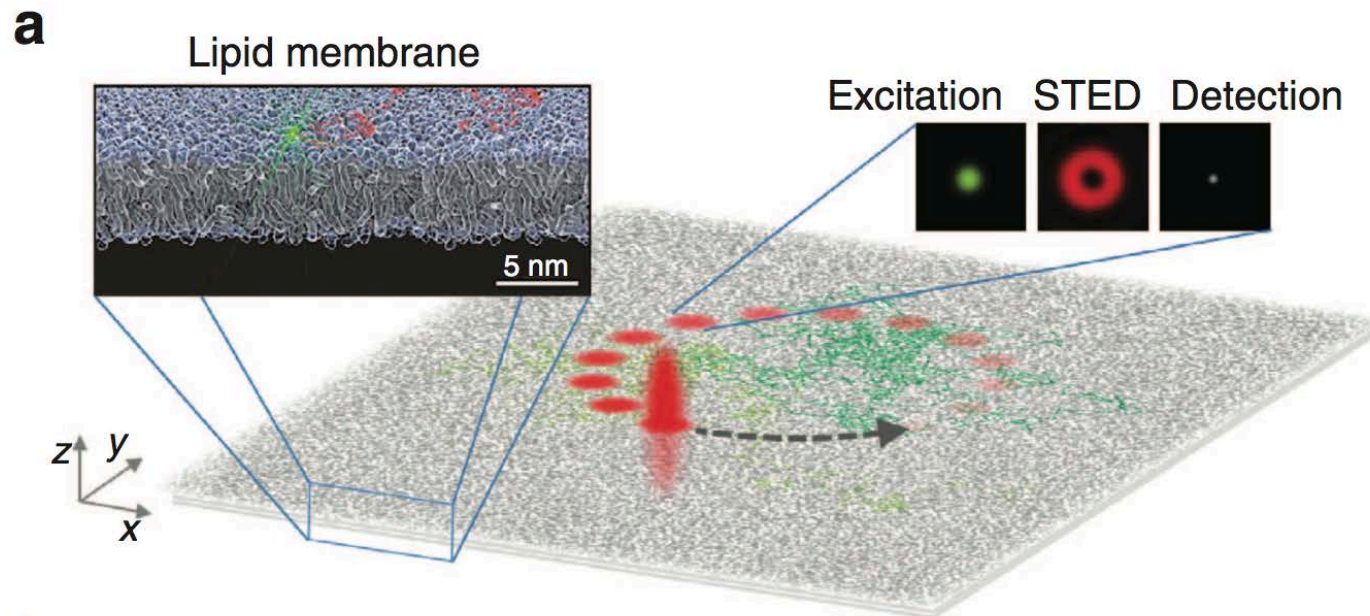
## Spot variation FCS



## Z-Scan FCS



## Scanning STED FCS (2D diffusion)



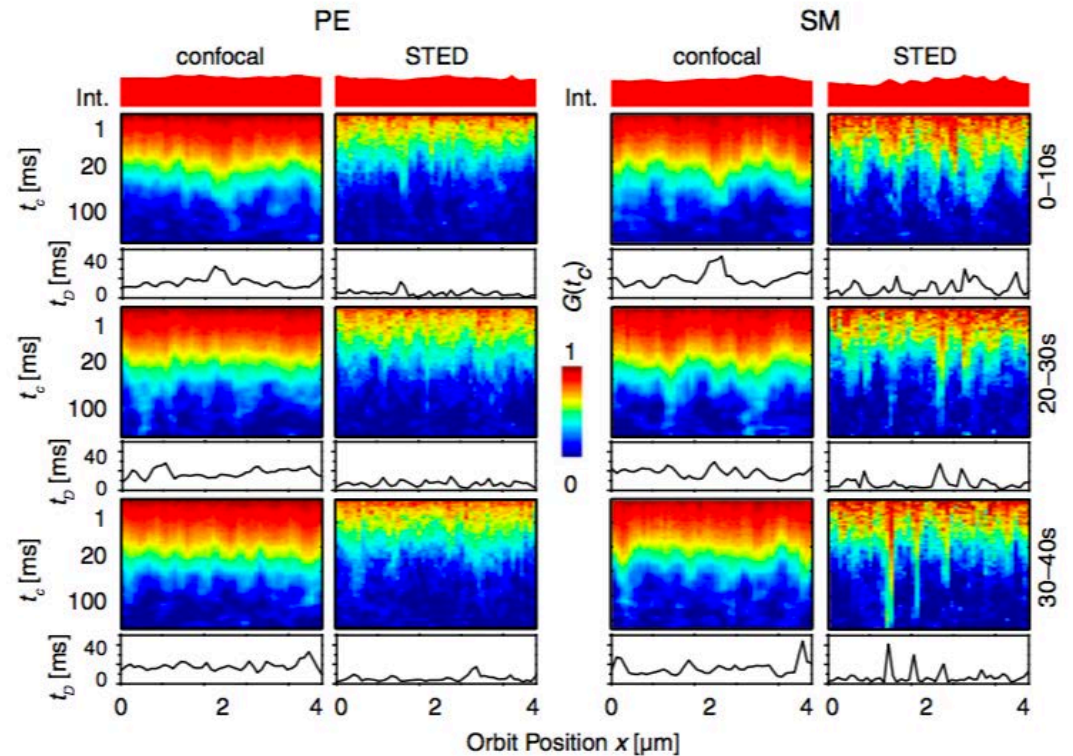
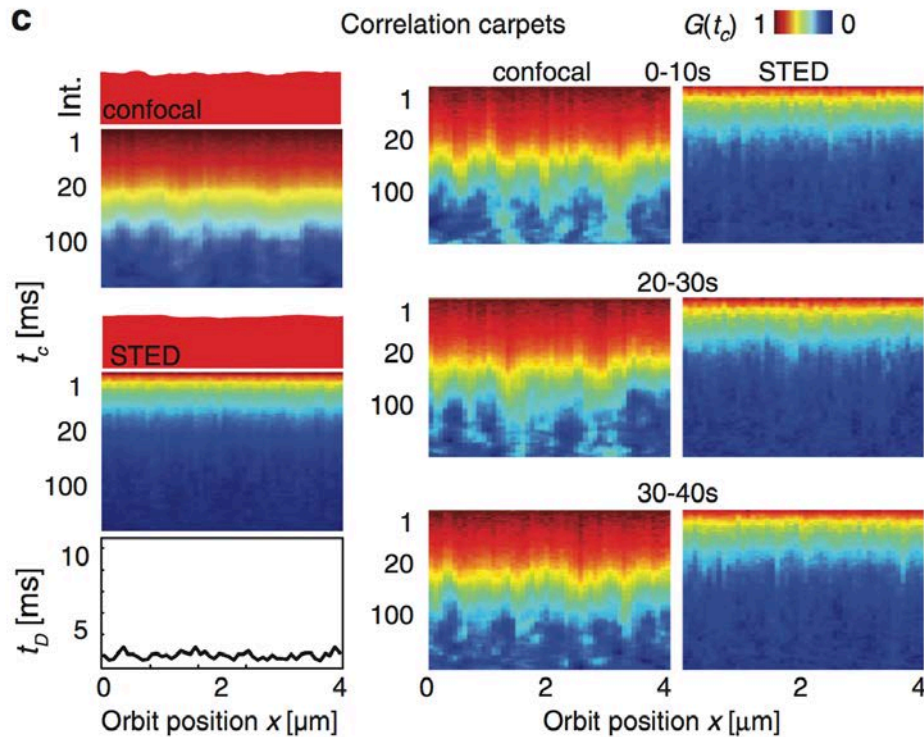
The STED beam is circularly moved in the plane of the cell membrane:

- 1-4 kHz rotating frequency
- Radius in the  $\mu\text{m}$  range
- 60 nm resolution (width of the STED volume)
- 1 pixel every 15 nm



# Scanning STED FCS (2D diffusion)

Correlation carpet of simulated brownian diffusing particles



Correlation carpet of PE and SM in the plasma membrane of living cells

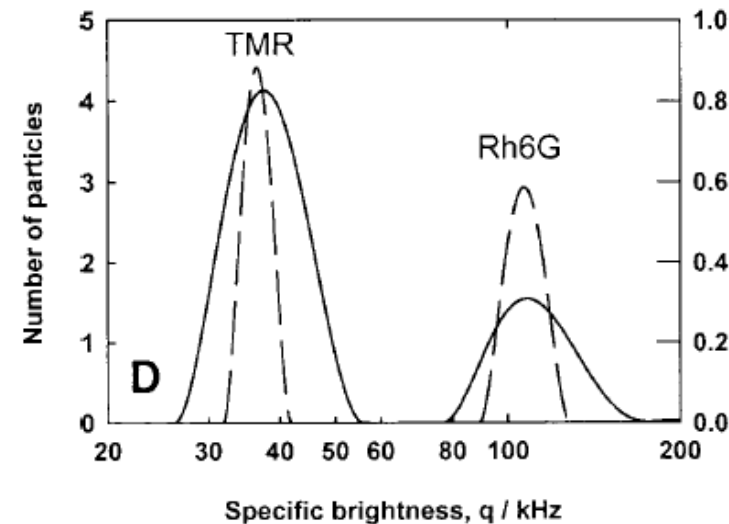
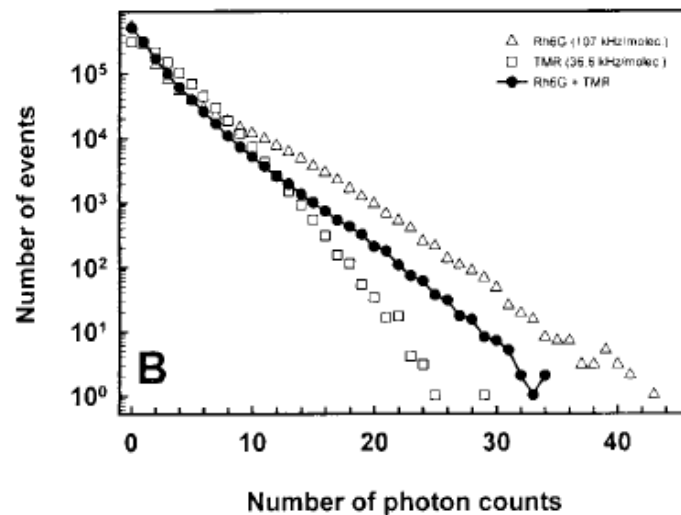
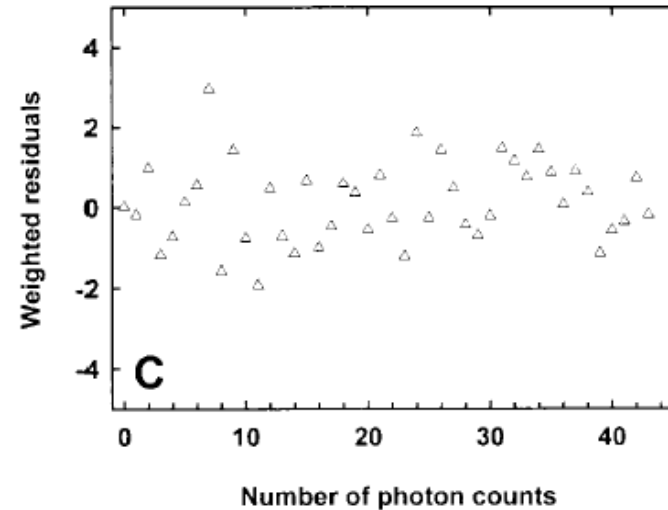
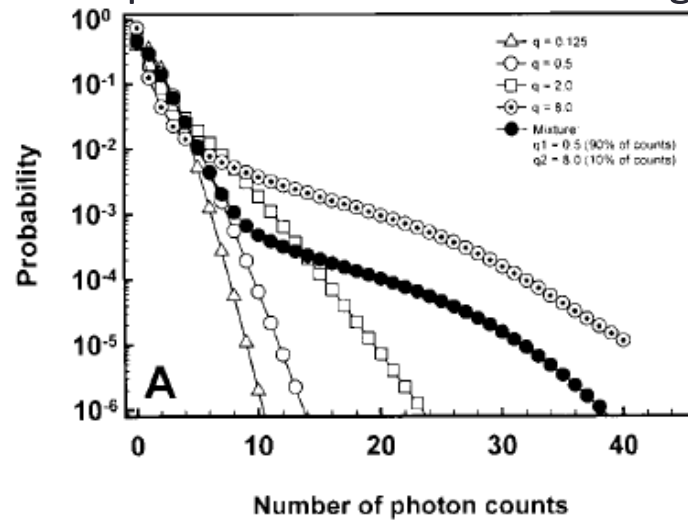
Mueller V et al. (2014) Nat Commun 5:1–12.

- ✓ Direct access to the heterogeneity of the cell membrane
- ✓ Possibility to extract informations about lipids domain
- ✓ Spatial correlation

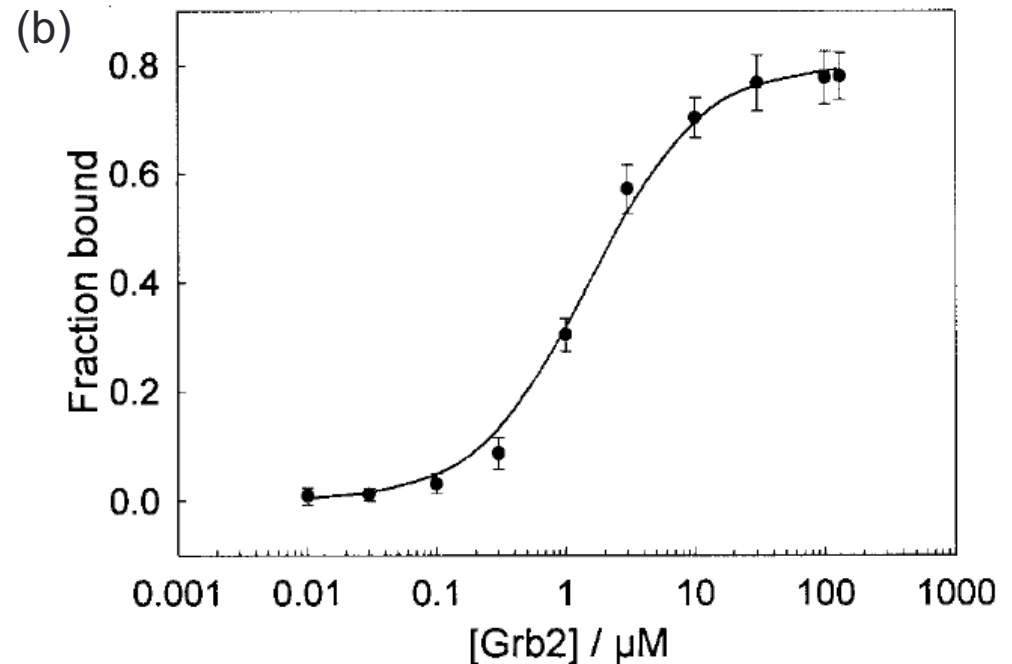
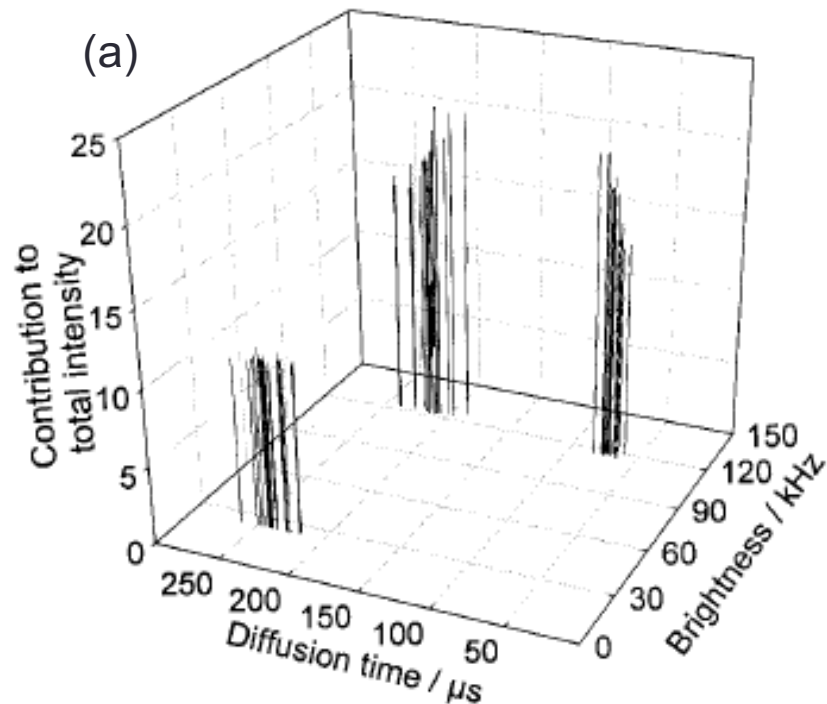


# Fluorescence intensity distribution analysis (FIDA)

- Principle: Histograms of burst intensities are measured. The intensity of the burst will depend on the brightness of the molecule; e.g. a dimer of fluorophores will be twice as bright as a monomer.



# Combining FCS and FIDA: FIMDA. High-throughput-screening at the single-molecule level

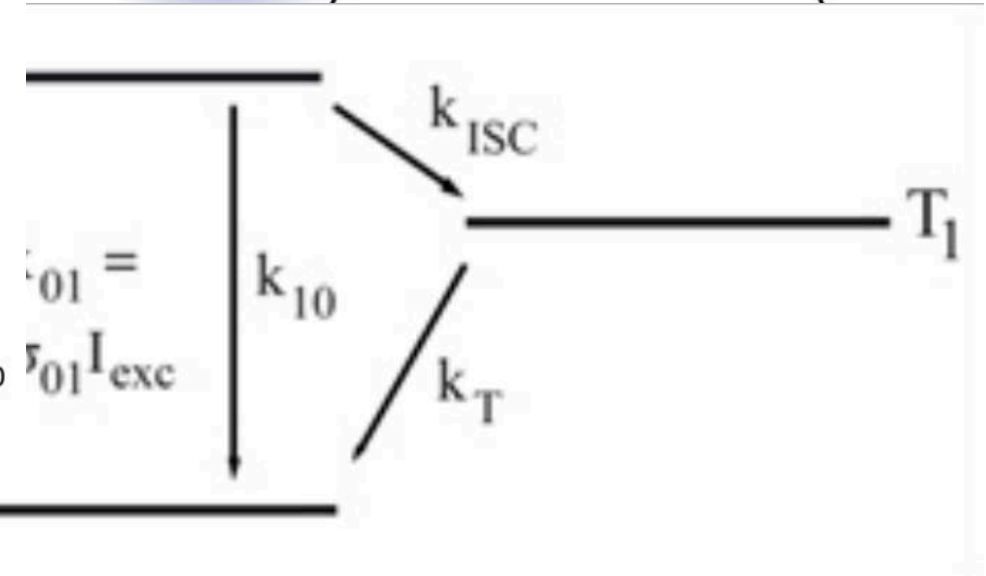
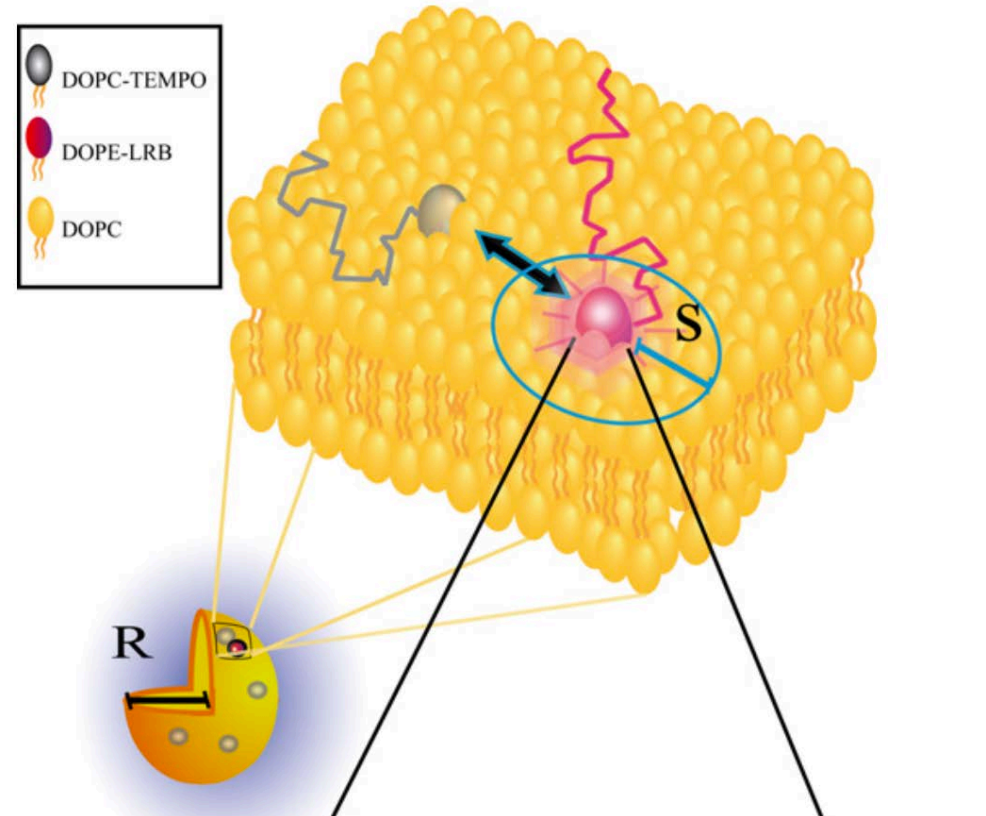
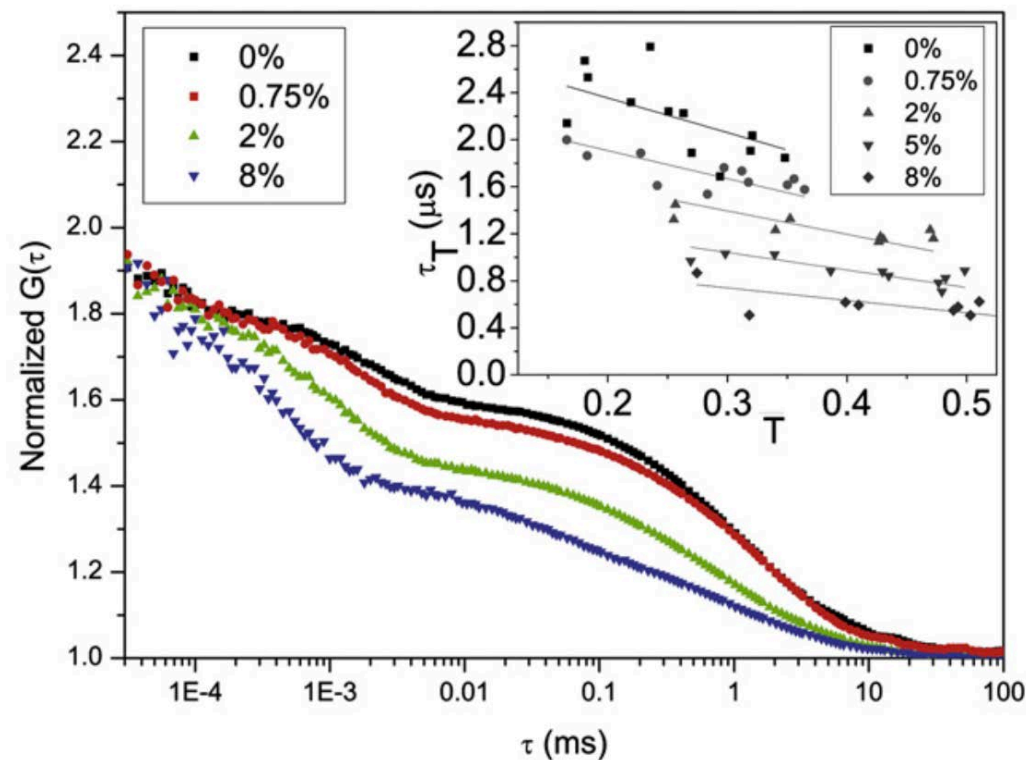


- (a): example with three components. (b) titration curve of a peptide binding to an SH2 group.
- Even more information can be obtained by combining with measurements of the fluorescence lifetime, of the anisotropy or using two colours.
- K. Palo, U. Mets, S. Jäger, P. Kask, K. Gall, *Biophys. J.* **79**, 2858 (2000)

# Quenching of Triplet State

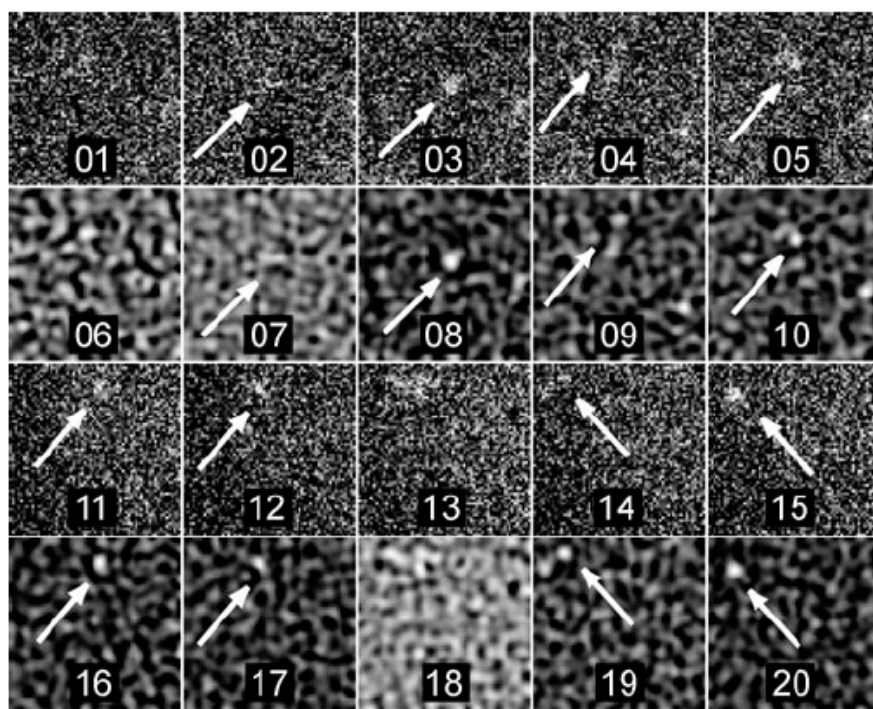
FRET timescale is too short to measure interactions between diffusing particles

Triplet lifetime (up to  $\mu\text{s}$ ) is long enough for the diffusing molecule to interact



# The two worlds are merging: FCS with a CCD detector

CCD and sCMOS cameras allow very rapid data acquisition ( $\sim 1$  kHz). This enables direct observation of diffusing molecules in solution (SMI, e.g. D. Grünwald et al., *Chemphyschem* **7**, 812 (2006)) and the recording of FCS autocorrelation curves using cameras with possibility of multiplexing (e.g. B. Kannan et al., *Anal. Chem.* **78**, 3444 (2006))



01 – 10: Streptavidin-Cy5 (SAv-Cy5)

11 – 20: mAb-Alexa 635

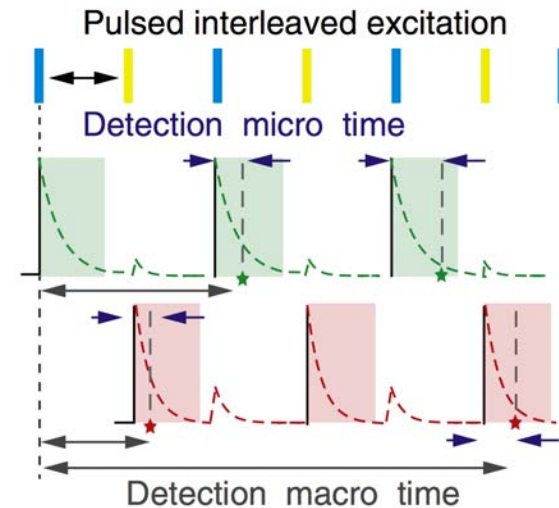
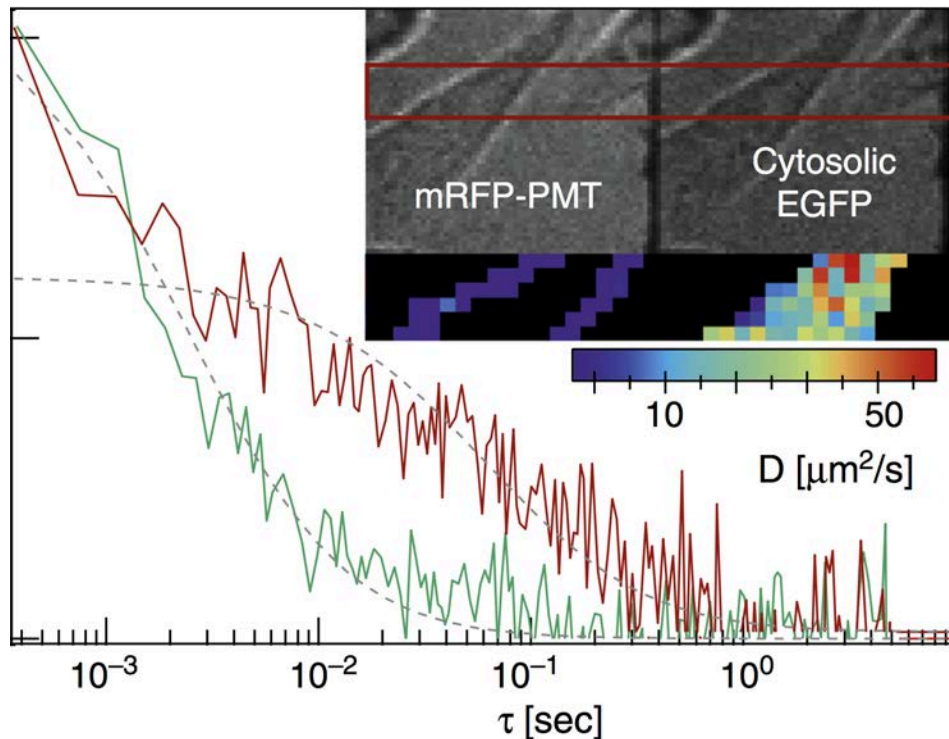
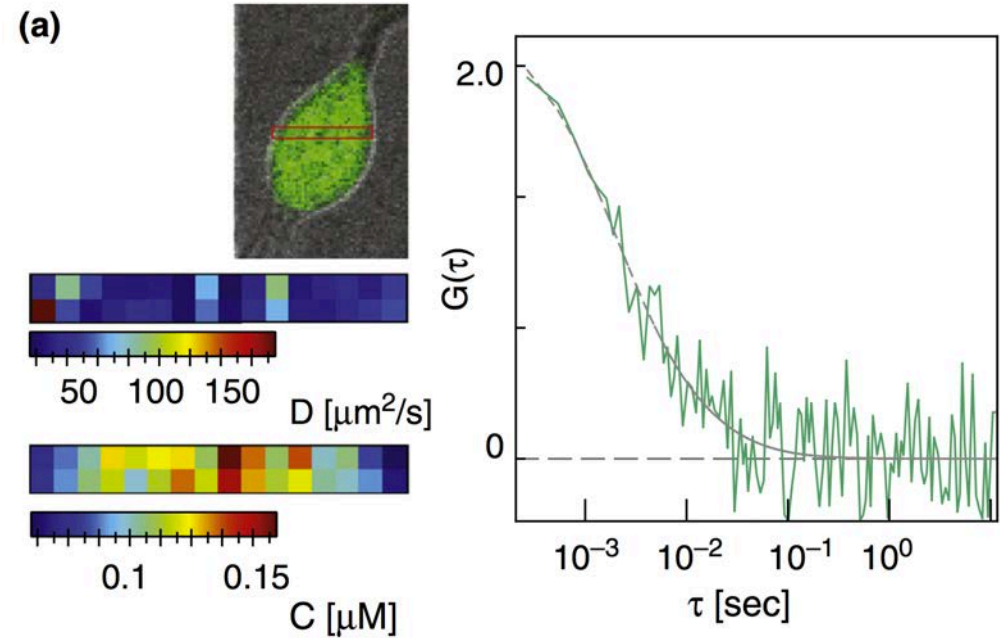
	$D_{\text{SMT}} [\mu\text{m}^2\text{s}^{-1}]$	$D_{\text{FCS}} [\mu\text{m}^2\text{s}^{-1}]$	$D_{\text{theory}} [\mu\text{m}^2\text{s}^{-1}]$
SAv-Cy5	$80 \pm 5$	$87 \pm 10$	81
mAb-Alexa635	$42 \pm 5$	$40 \pm 10$	57.4



# Imaging FCS

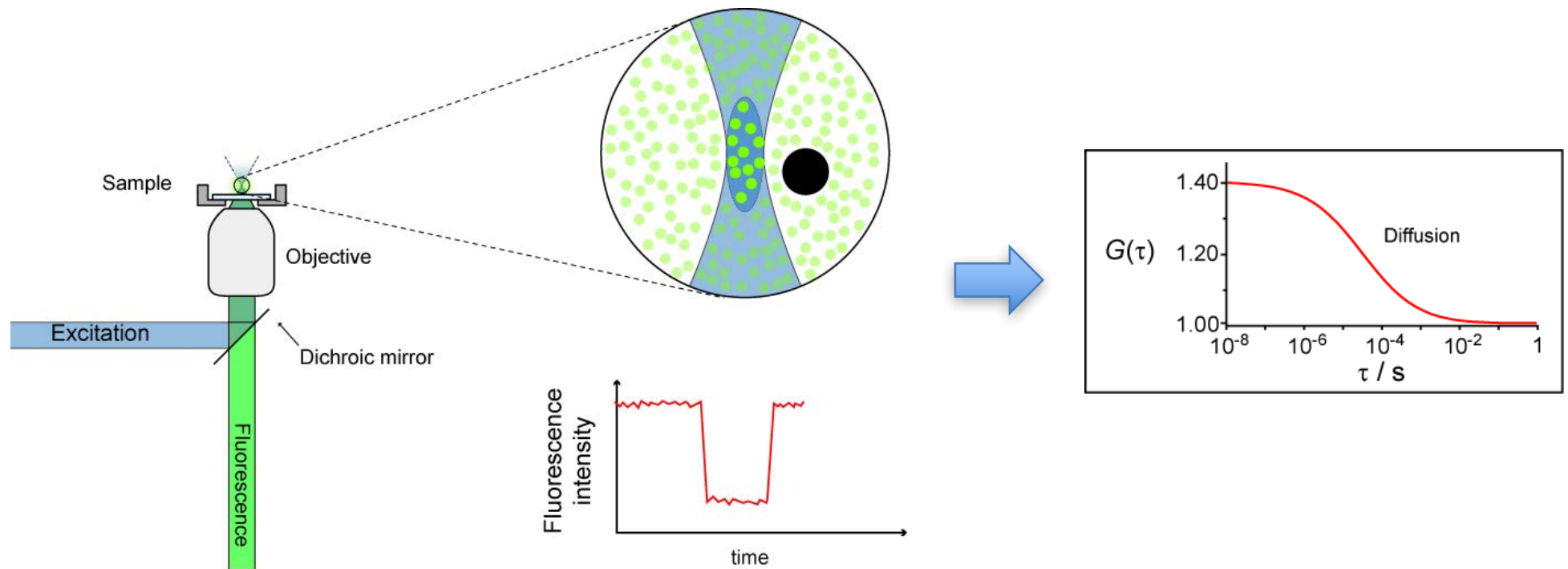
Two observables:

- Diffusion coefficient
- Number of molecules





# Single-molecule detection without labeling: Inverse FCS



$$G(0) = \frac{N}{\frac{1}{V_q} N^2}$$

$$V_q = \frac{V_{particle}}{V_{detection}}$$

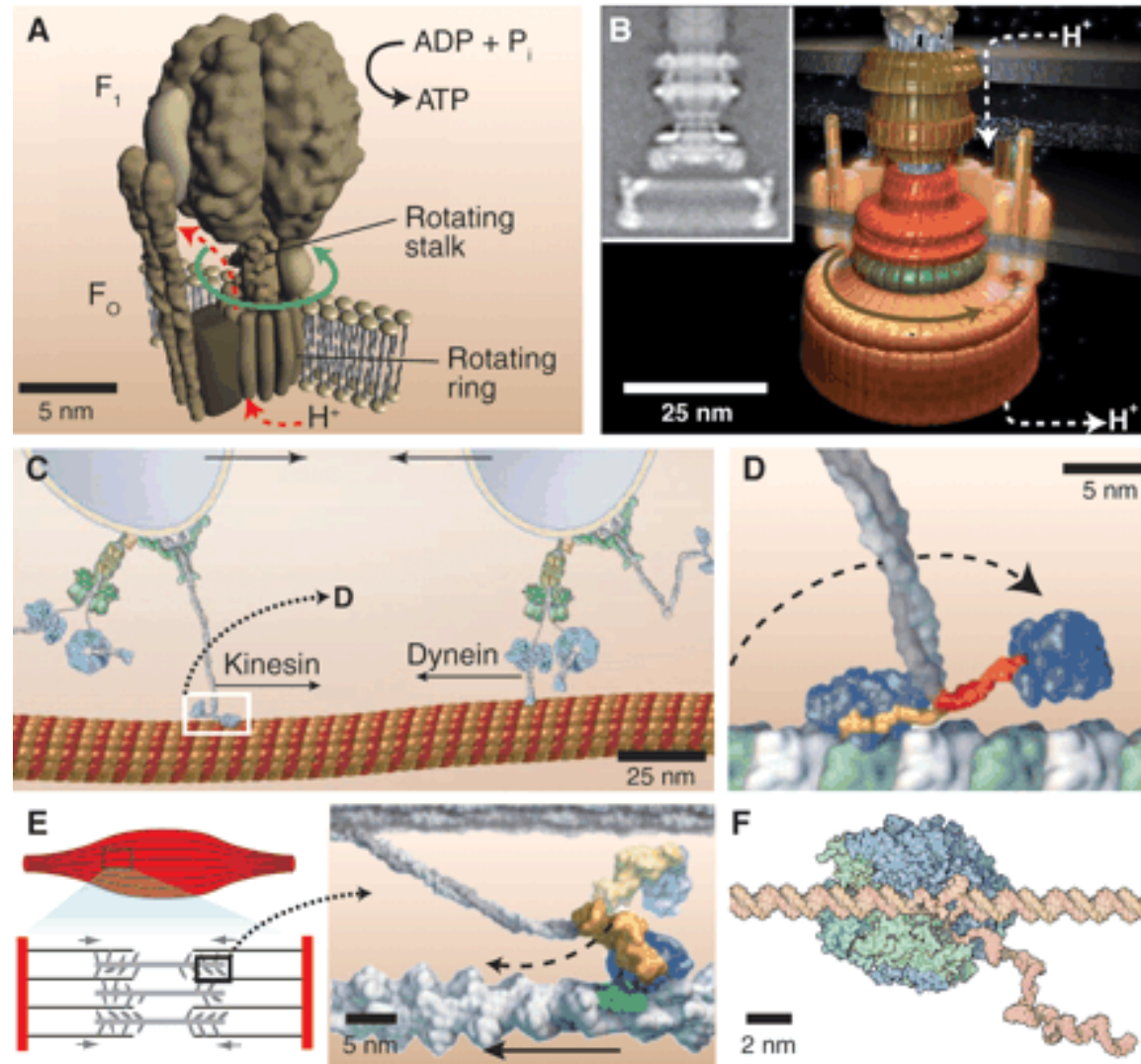
- Photon noise
- Molecular noise

Functional devices based on single-molecule

## Outlook: How can one integrate nano-machines into functional devices?

- Molecular motors
- Nano-bioanalytics, nano-containers: Reducing the sample volumes
- Nano-sensors: Combination with electrophysiology
- Nano-sequencer: DNA, RNA and peptide sequencing

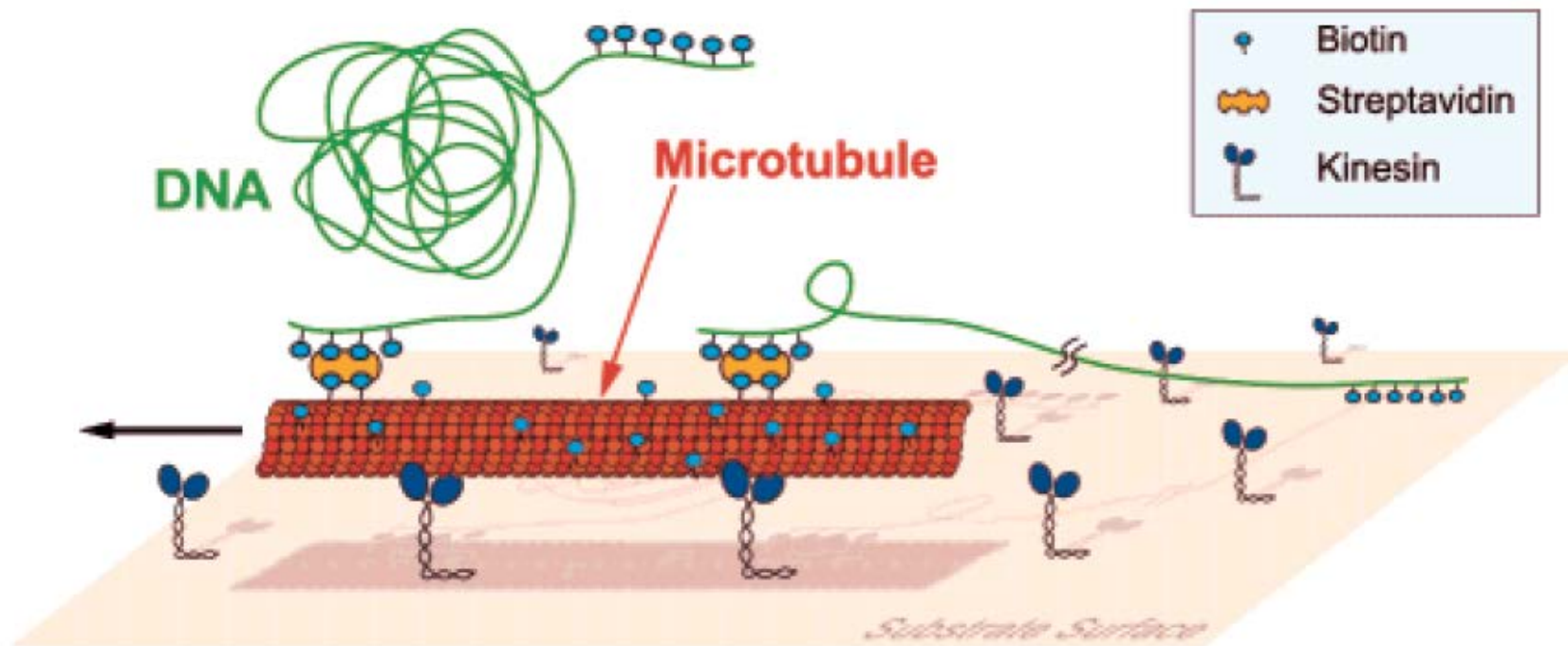
# Molecular Motors



M. G. L. van den Heuvel, C. Dekker, *Science* **317**, 5836, (2007) 333 – 336

## Processing motors: Moving cargos

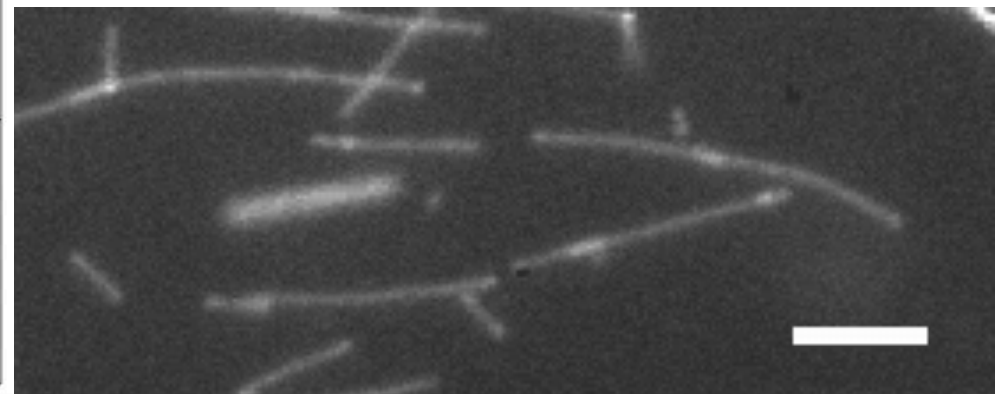
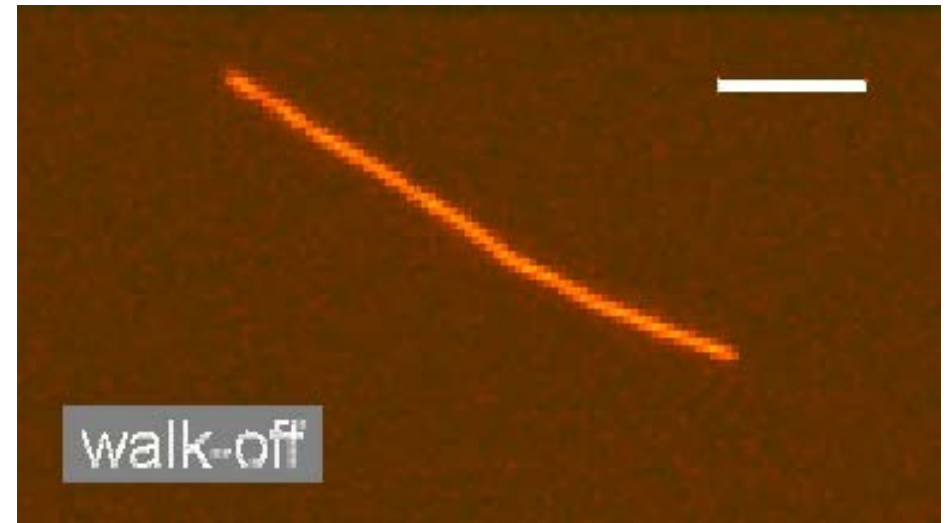
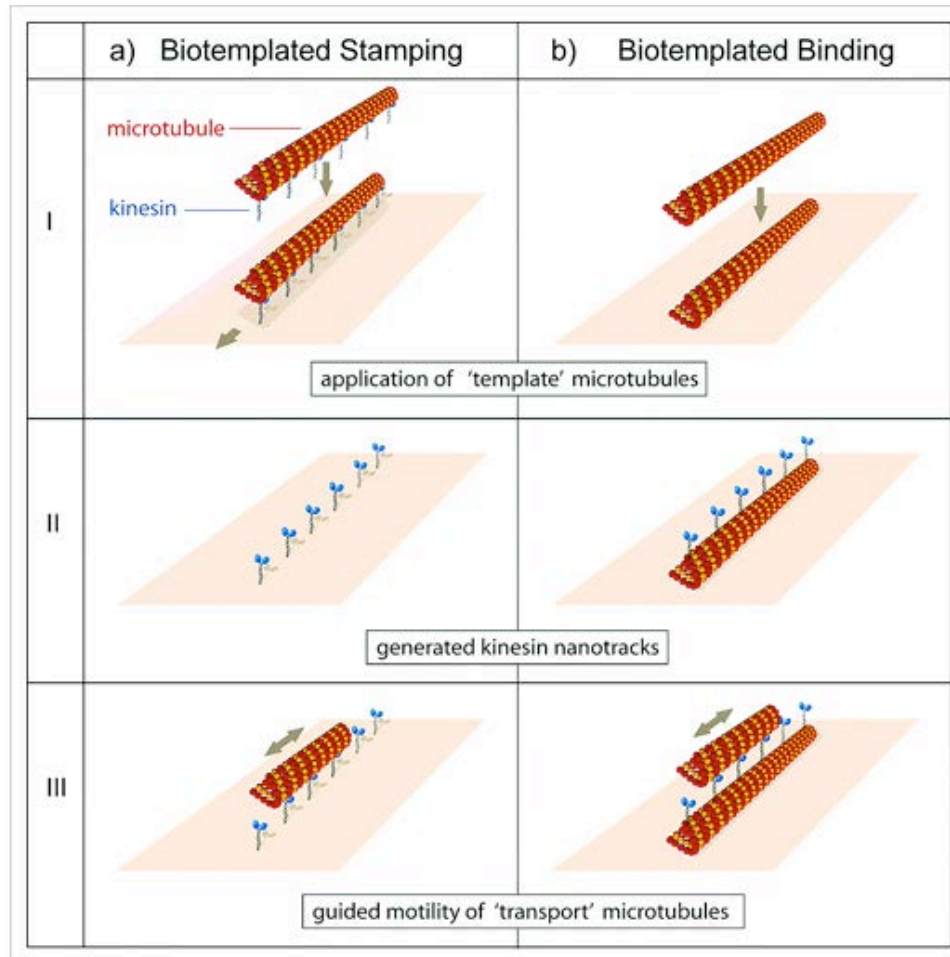
Motor: kinesin. Cargos: DNA attached to microtubules



S. Diez, C. Reuther, C. Dinu, R. Seidel, M. Mertig, W. Pompe, J. Howard, *Nano Lett.* **3**, 1251 (2003)



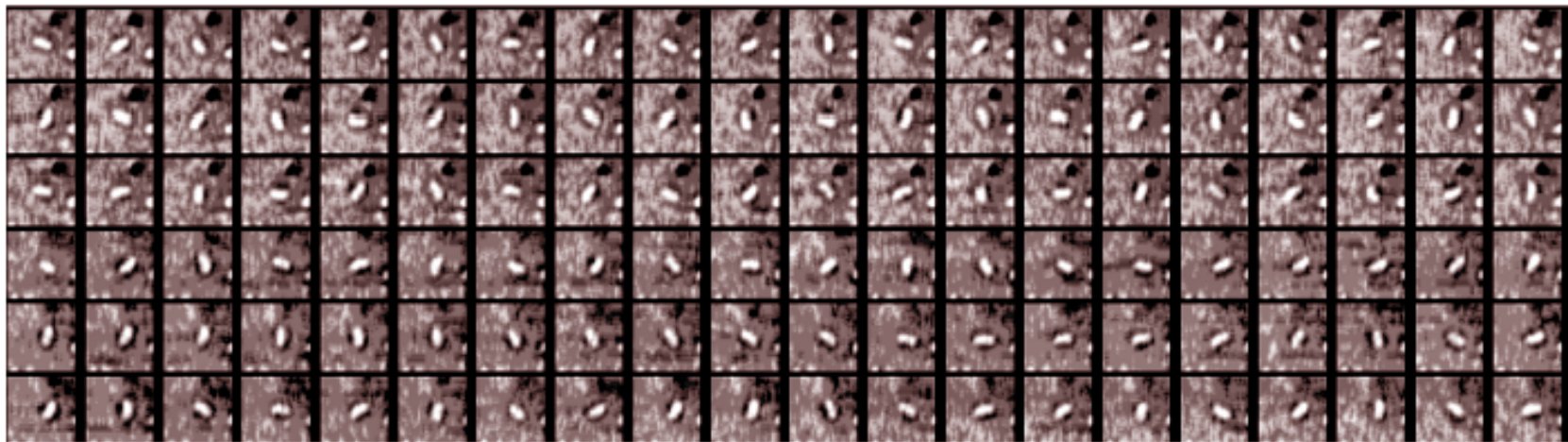
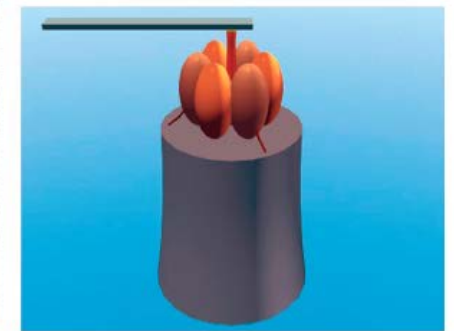
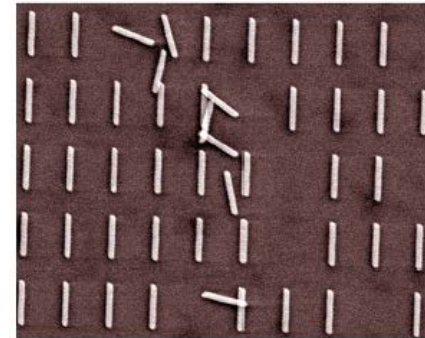
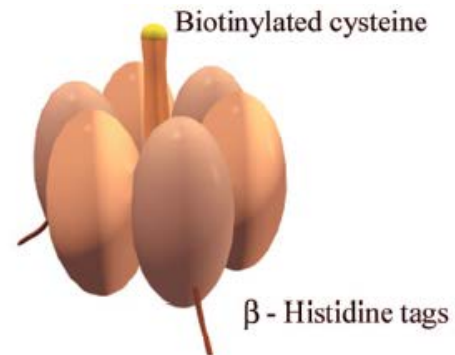
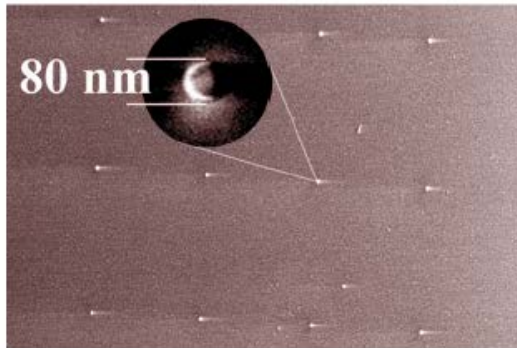
# Kinesin nanotracks



C. Reuther,<sup>†</sup> L. Hajdo,<sup>‡</sup> R. Tucker,<sup>§</sup> A. A. Kasprzak,<sup>‡</sup> S. Diez<sup>\*†</sup> *Nano Lett.*, 2006, 6 (10), 2177–2183

# Rotary motors: F1 ATPase

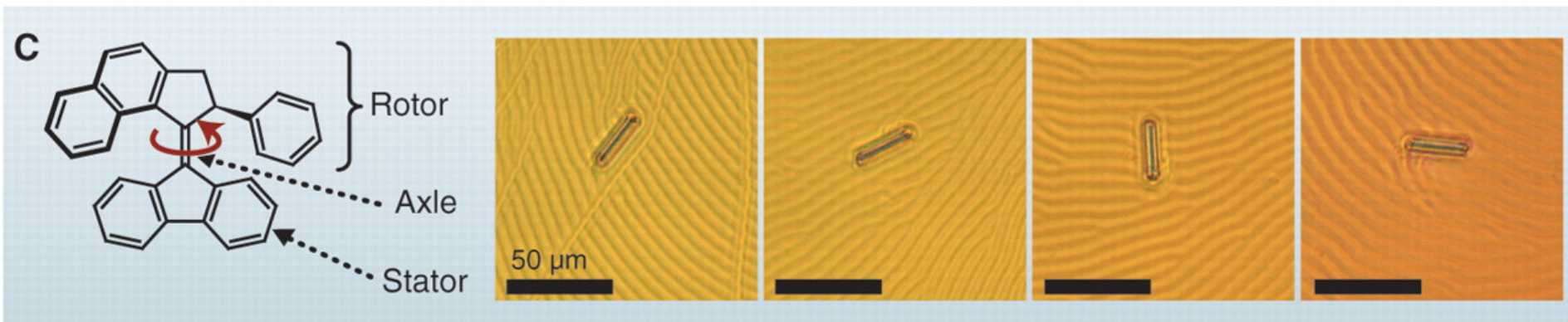
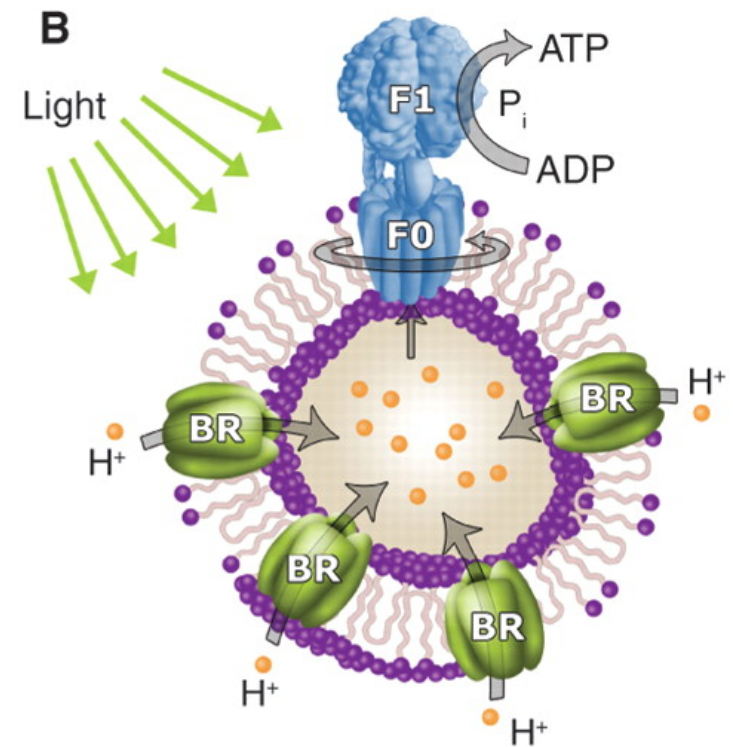
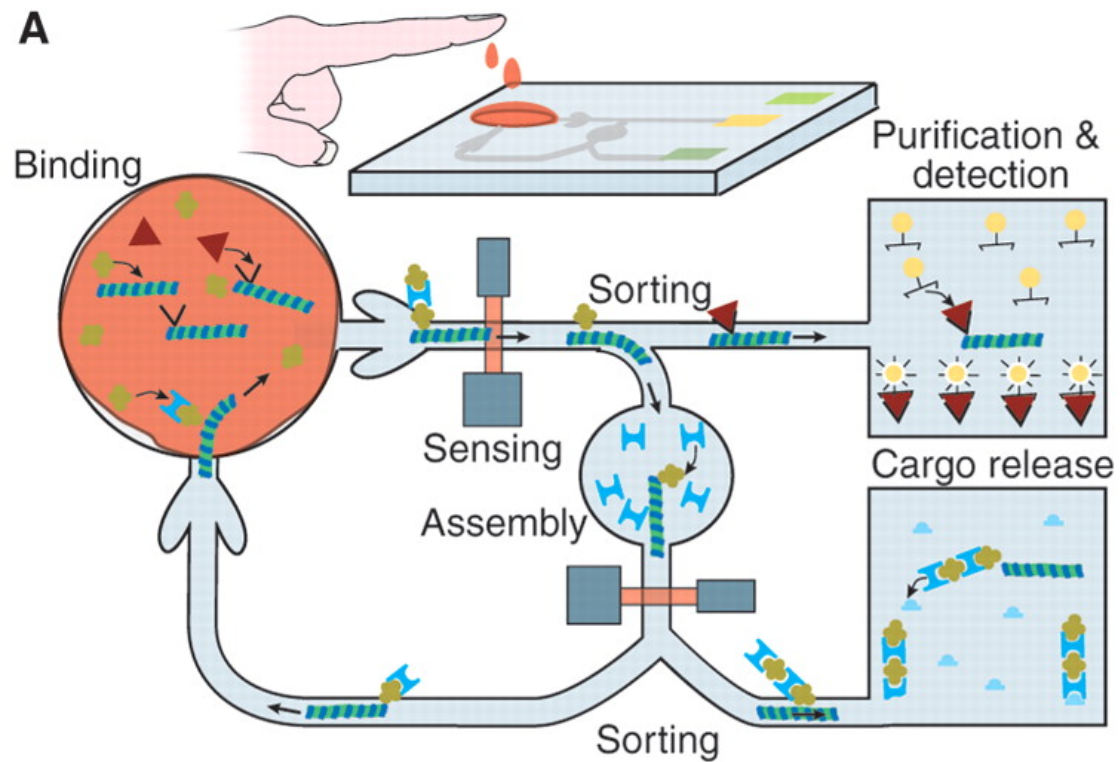
F1 ATPase attached to Ni posts by His Tags is used to rotate Ni arms



R.K. Soong, G.D. Bachand, H.P. Neves, A.G. Olkhovets, H.G. Craighead, C.D. Montemagno, *Science* **290**, 1555 (2000)



# New directions with nanomotors

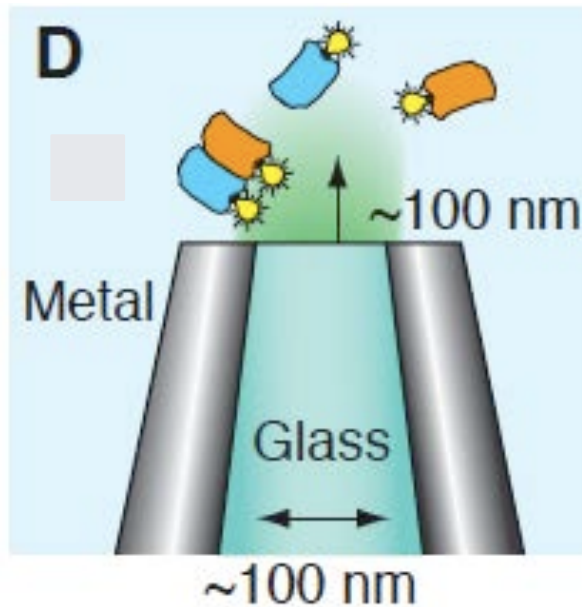


# High concentration or slow diffusion: Confining the volume

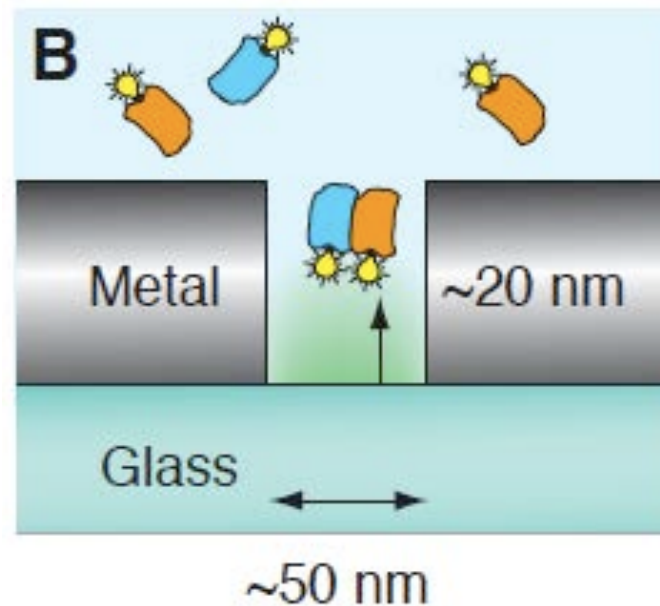
Measurement on living systems often involve high concentration on molecule or very slow diffusion coefficient, which are not compatible with conventional FCS

Working with small volume can overcome these drawbacks

Metallic Tapered Fiber tip

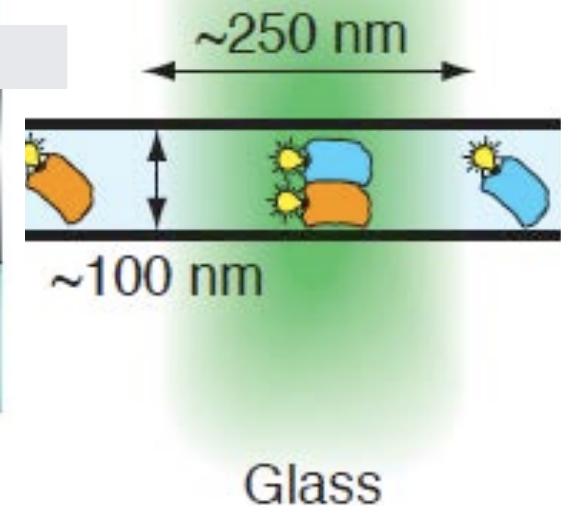


Subwavelength metal nanopores

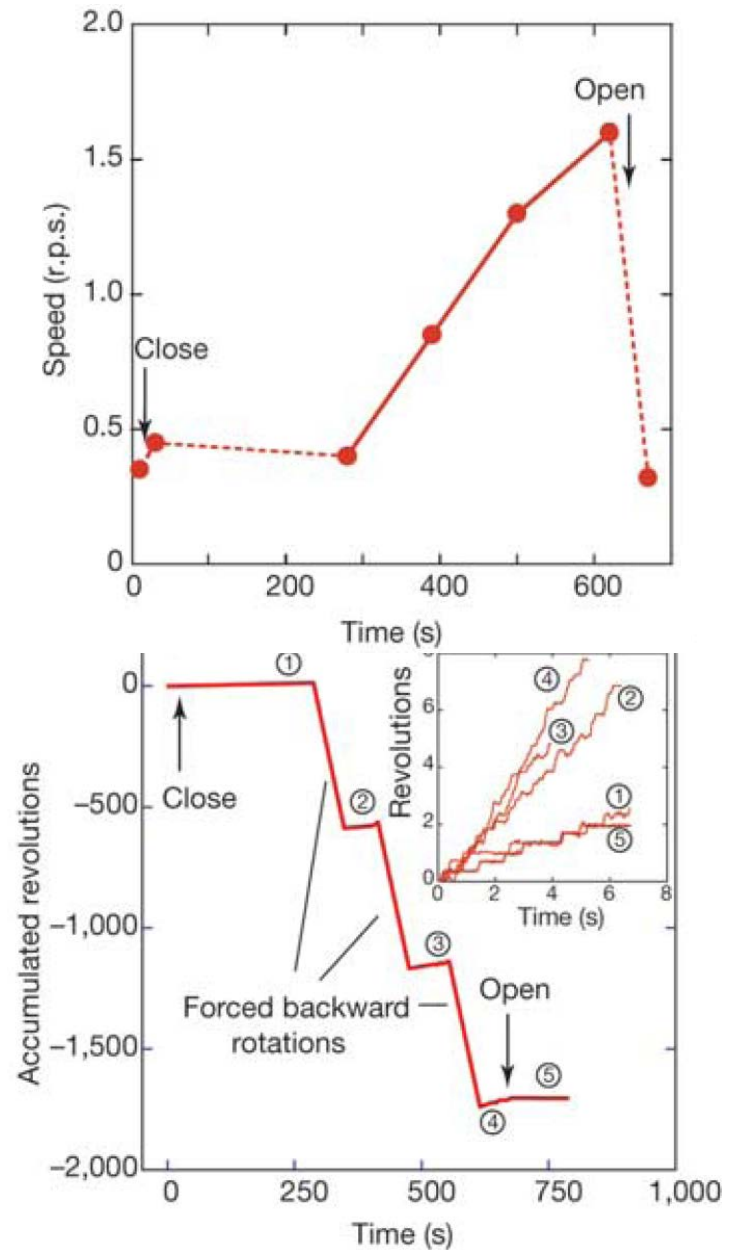
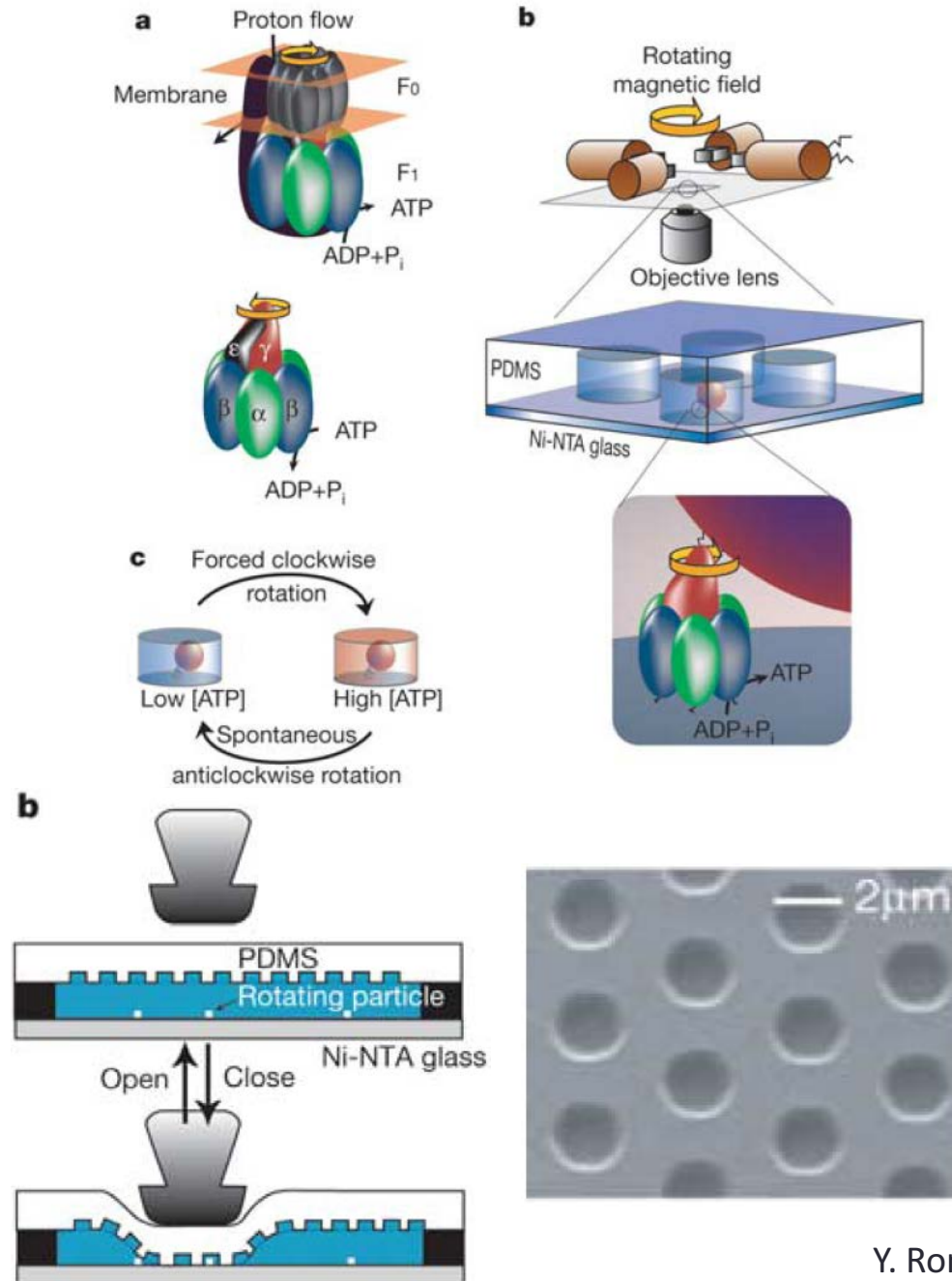


Nanofluidic

Glass



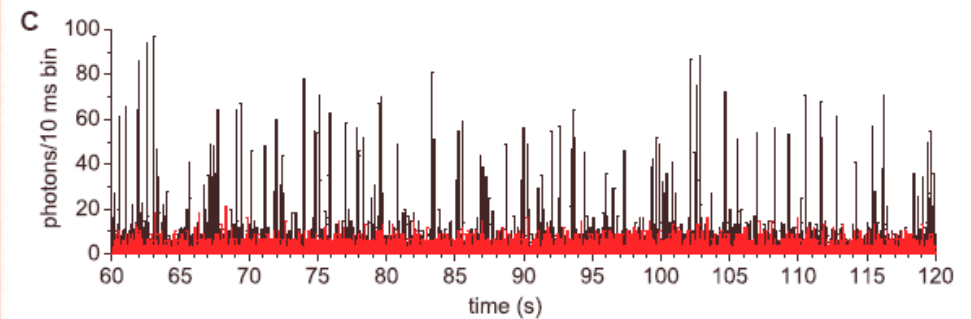
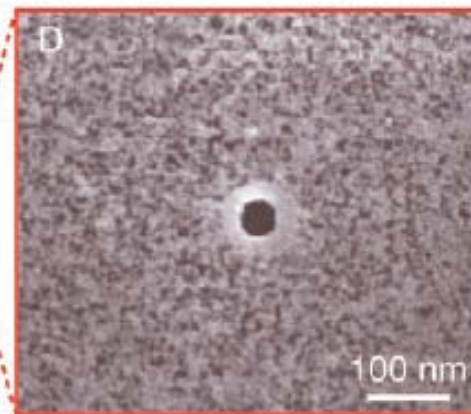
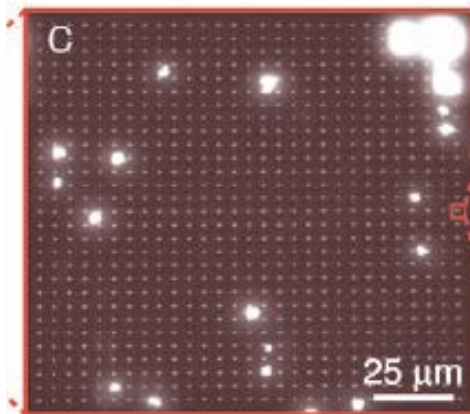
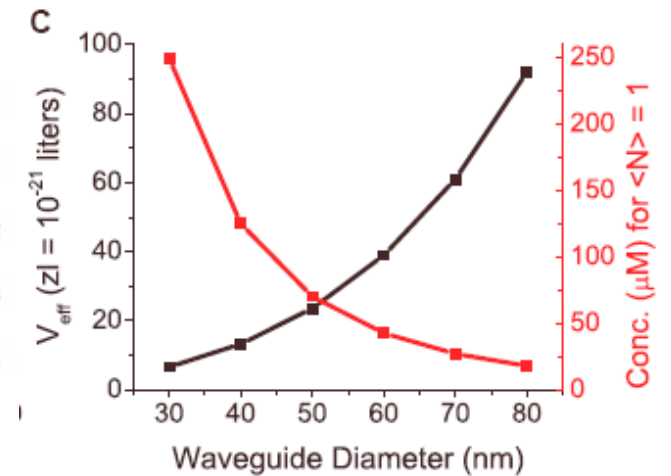
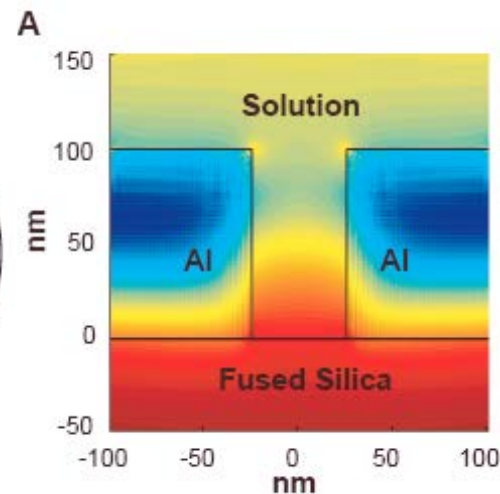
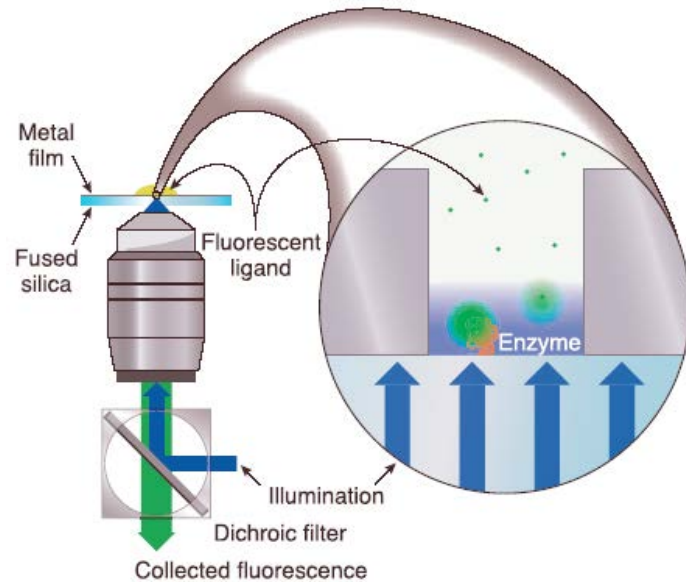
# Reducing the volumes: Femtoliter chambers



Y. Rondelez, et al., *Nature* **433**, 773 (2005)



# Reducing the volumes for nano-bioanalytics: Nanowells



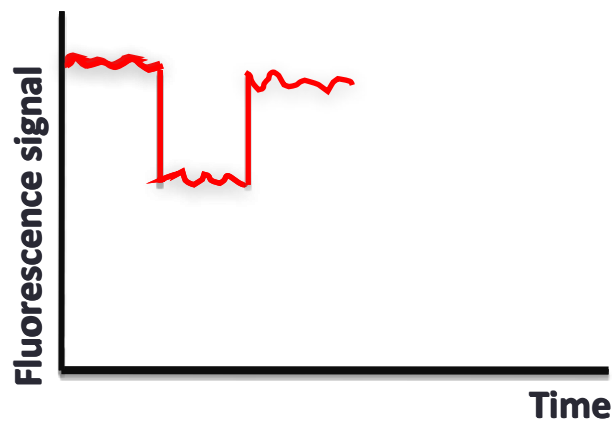
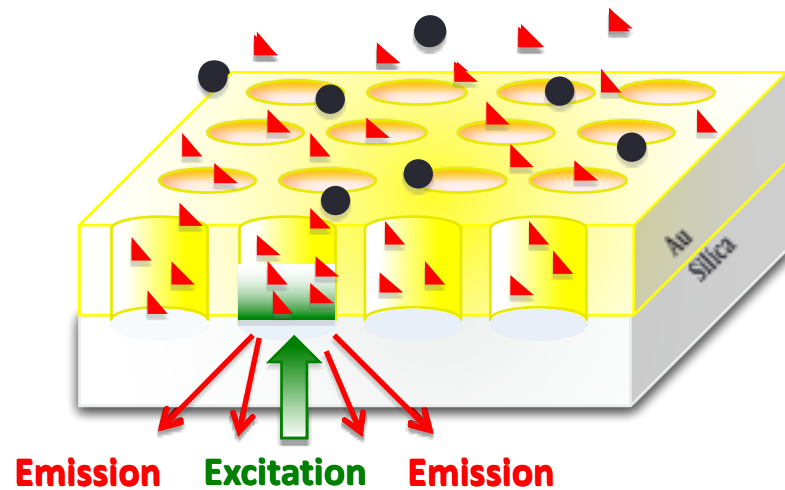
$$I(z) = \exp(-z / \Lambda)$$

$$\frac{1}{\Lambda} = \sqrt{2 \frac{1}{\lambda_c^2} - \frac{1}{\lambda_m^2}}$$

Principle: Small wells in Al with a diameter smaller than the wavelength of light. The light penetrates only up to a small depth in  $z$ .

M.J. Levene, J. Korlach, S.W. Turner, M. Foquet, H.G. Craighead, W.W. Webb, *Science* **299**, 682 (2003)

# Inverse FCS in nanoholes



Small detection volume

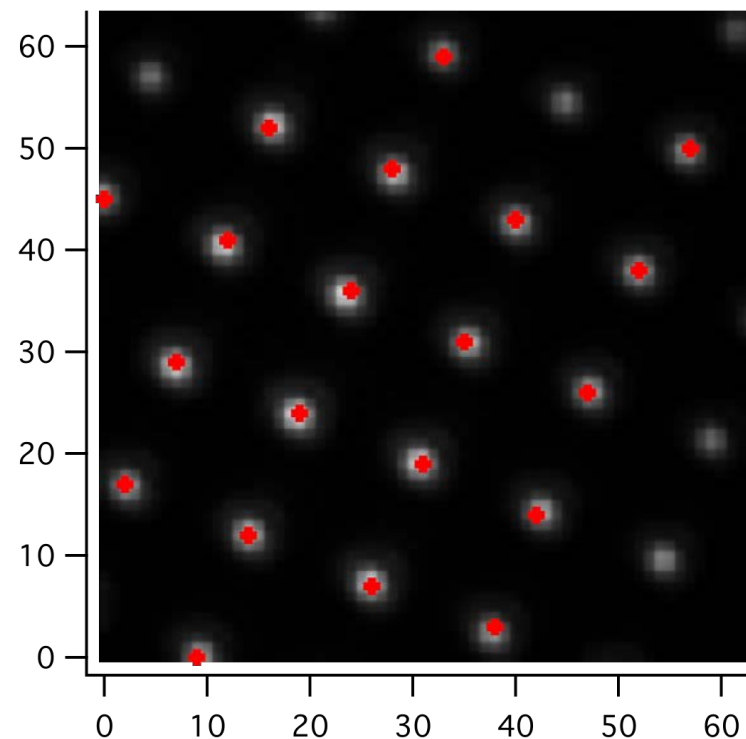
Measurements at  $\mu\text{M}$  concentrations, potentially mM

Label-free analysis of nano-sized particles or even proteins

Monitoring binding reactions

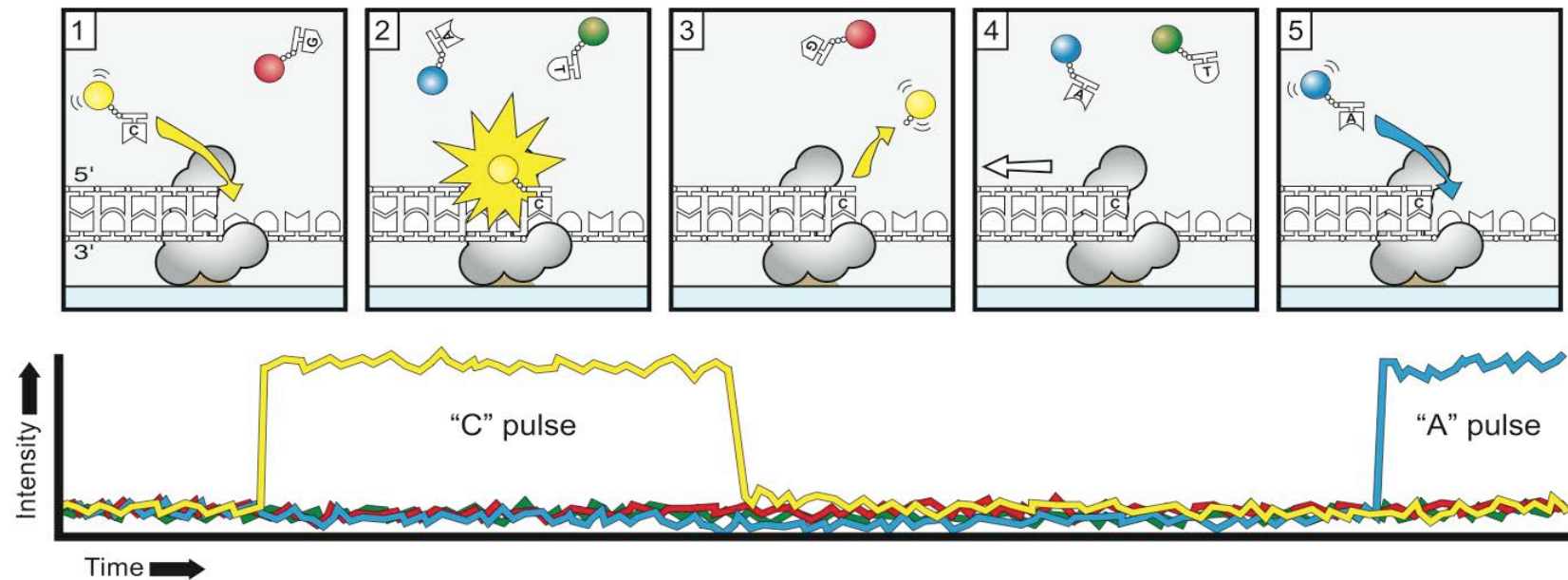
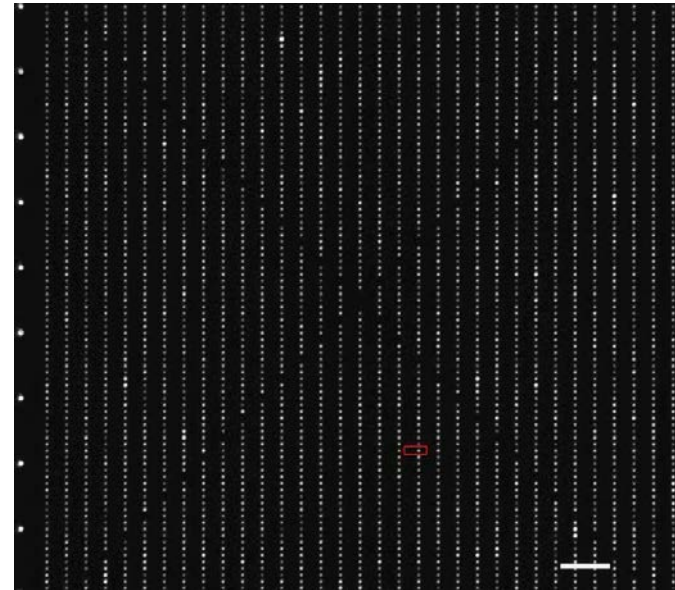
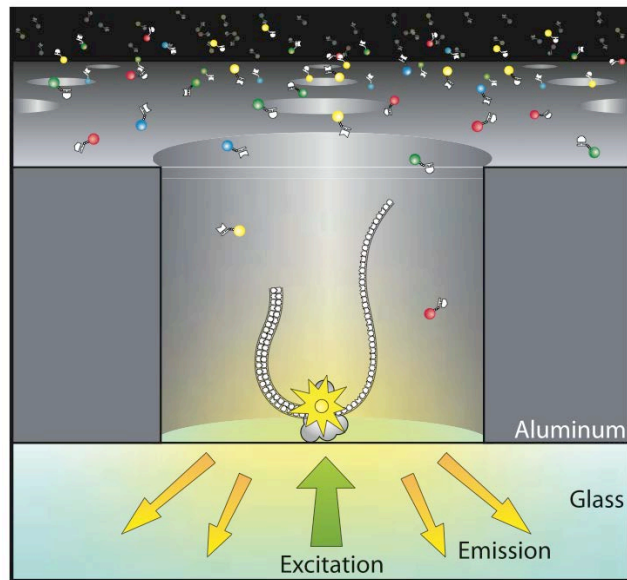
Low power – no photodamage

1 mM Alexa647



20 holes of 200 nm

# Nanowells: DNA sequencing



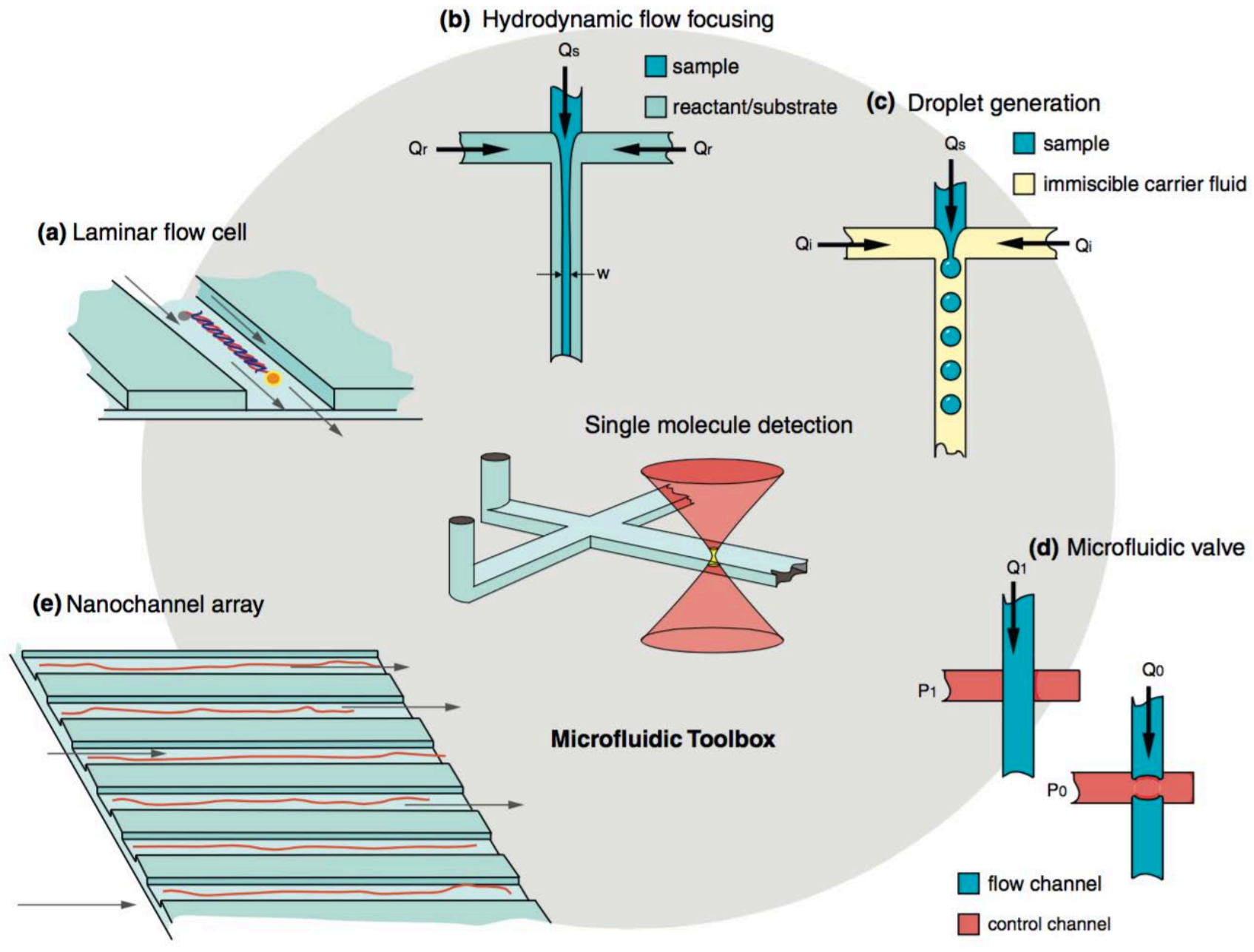
Nanowells: DNA sequencing

## Pacific Biosciences RSII



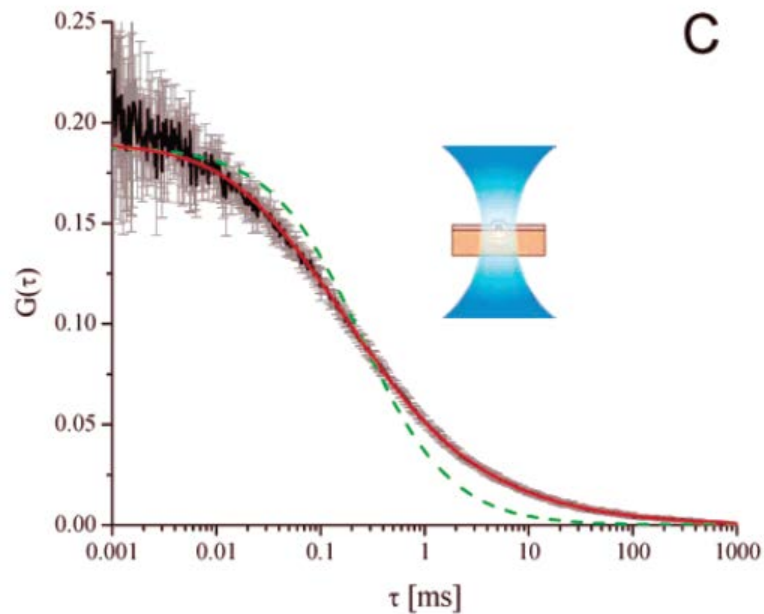
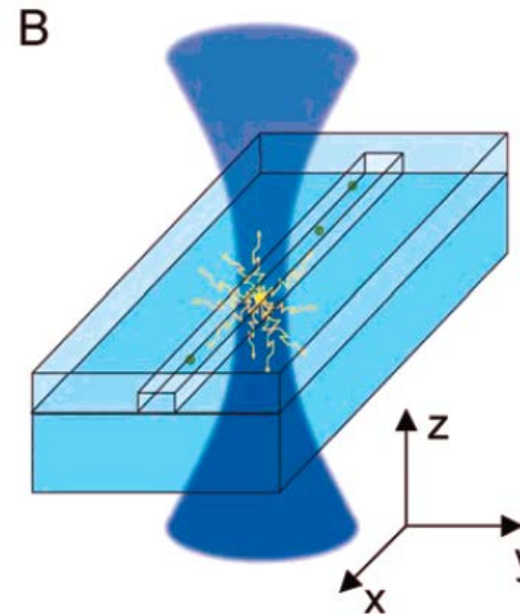
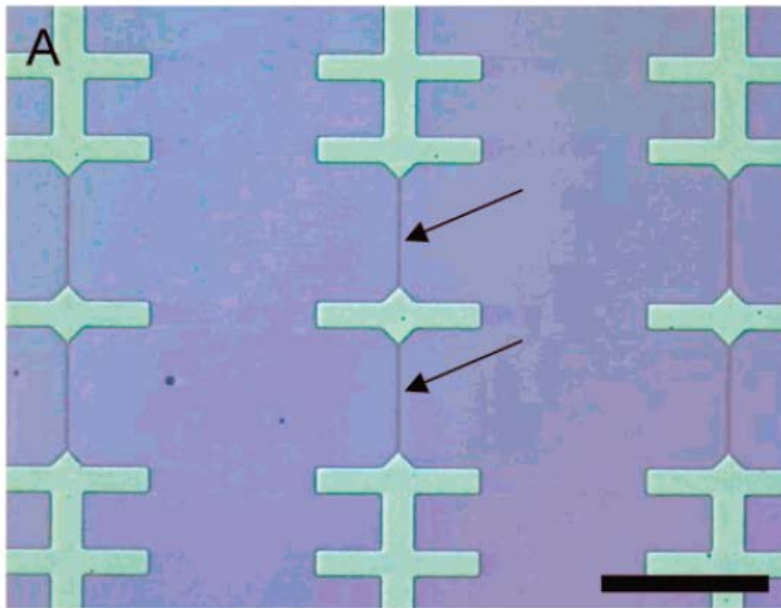


# Reducing the volumes for nano-bioanalytics: Nanofluidics





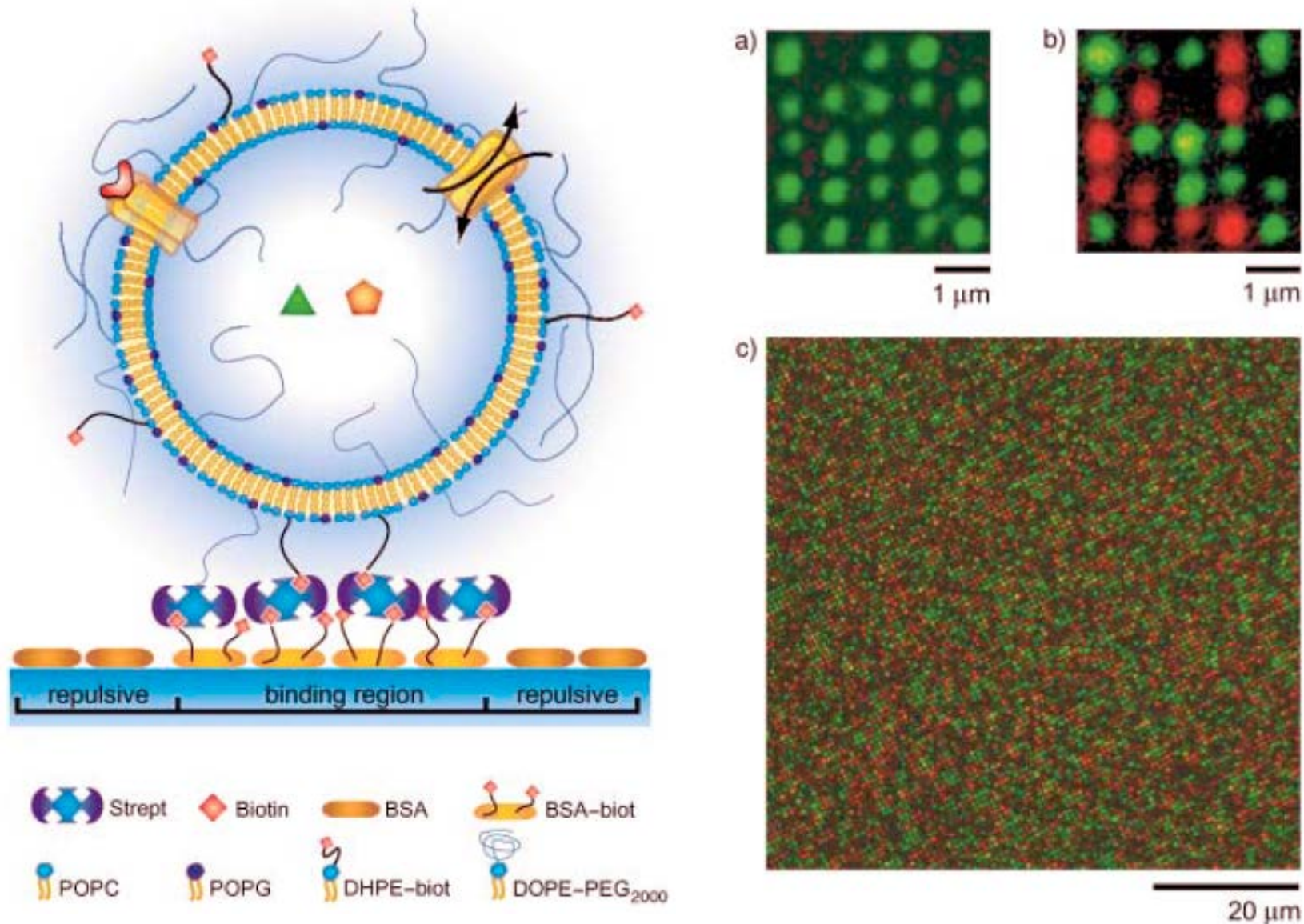
# Reducing the volumes for nano-bioanalytics: Nanofluidics



Channel height:  $\sim 250$  nm  
Wide channel diameter: 10  $\mu$ m  
Narrow channel diameter:  $\sim 350$  nm  
 $V_{\text{eff}} \sim 1$  fL usually  
 $V_{\text{eff}} = 0.033$  fL for the wide channel  
 $V_{\text{eff}} = 0.011$  fL for the narrow channel

M. Foquet, J. Korlach, W.R. Zipfel, W.W. Webb, H.G. Craighead  
*Anal. Chem.* **76**, 1618 (2004)

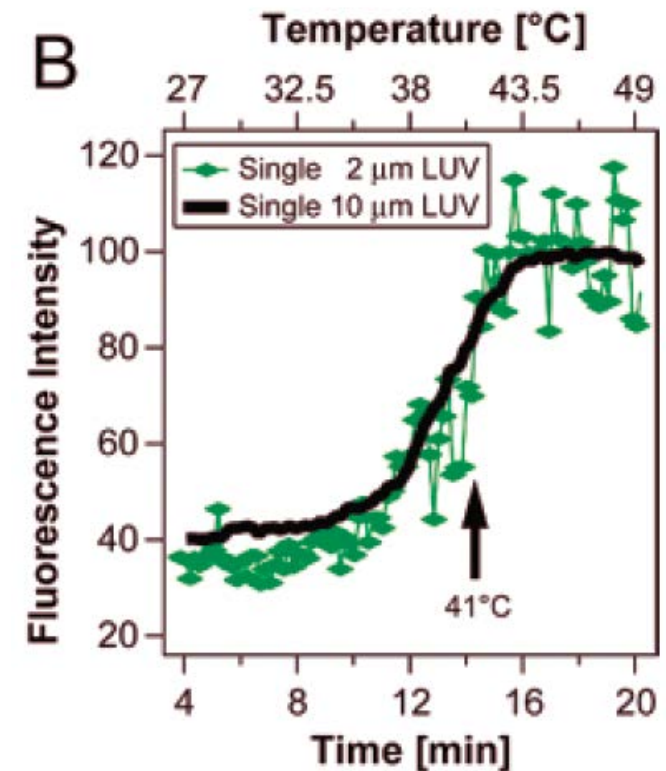
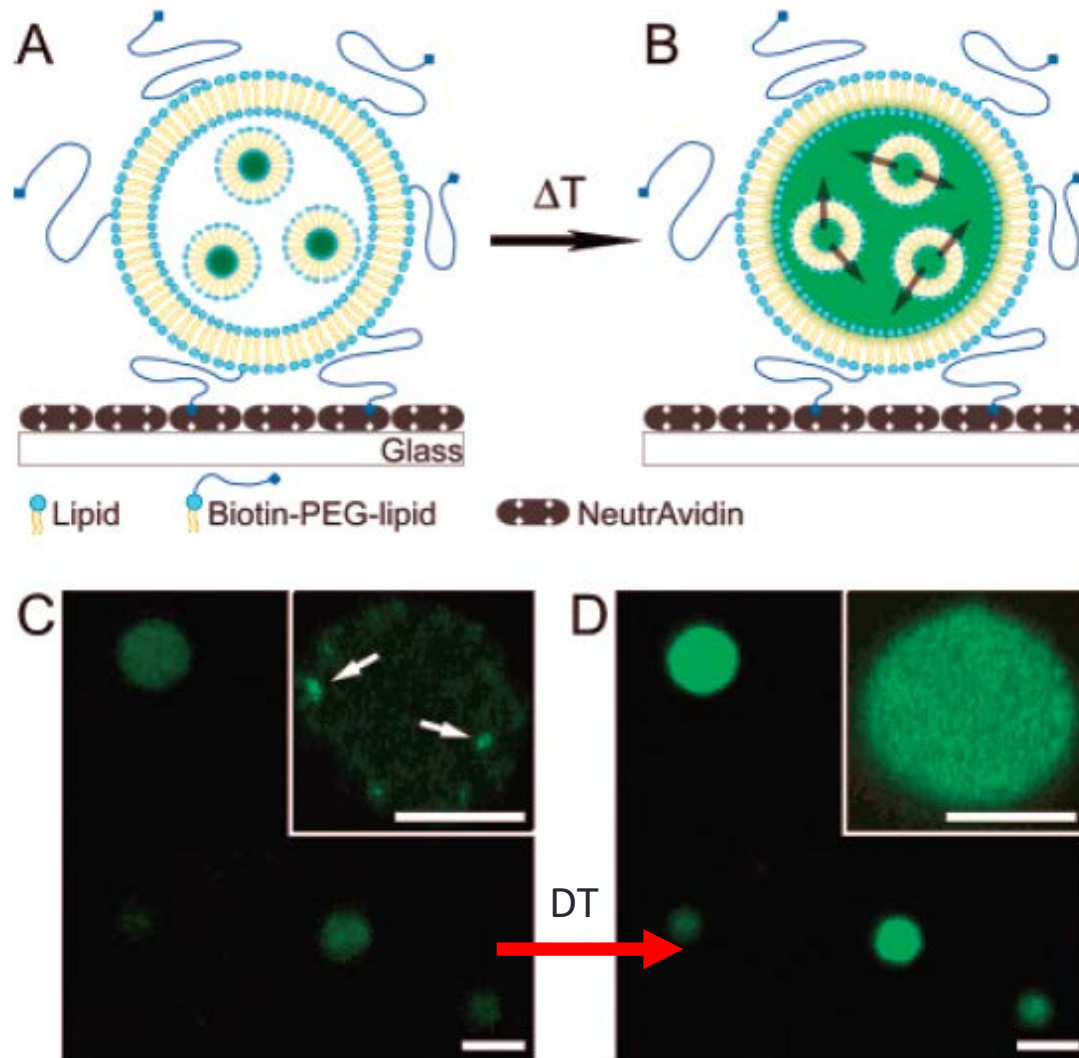
# Reducing the volumes for nano-bioanalytics: Nanocontainers made out of vesicles ( $V_{\text{vesicle}} = 1 \text{ aL}$ )



D. Stamou, C. Duschl, E. Delamarche, H. Vogel, *Angew. Chem. Int. Ed.* **42**, 5580 (2003)

# Nano-reactor: Nanochemistry in a vesicle

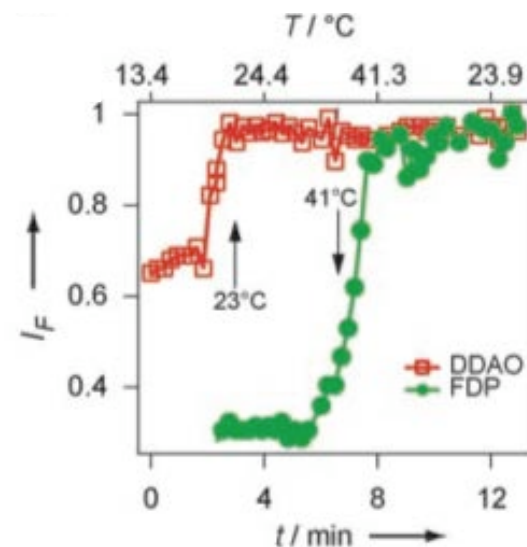
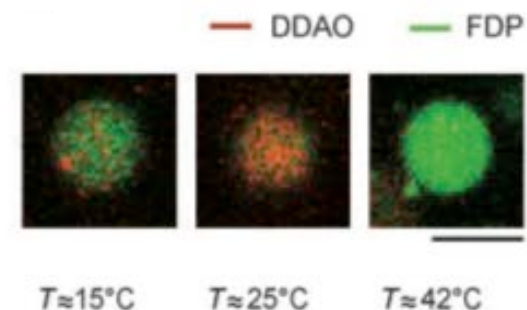
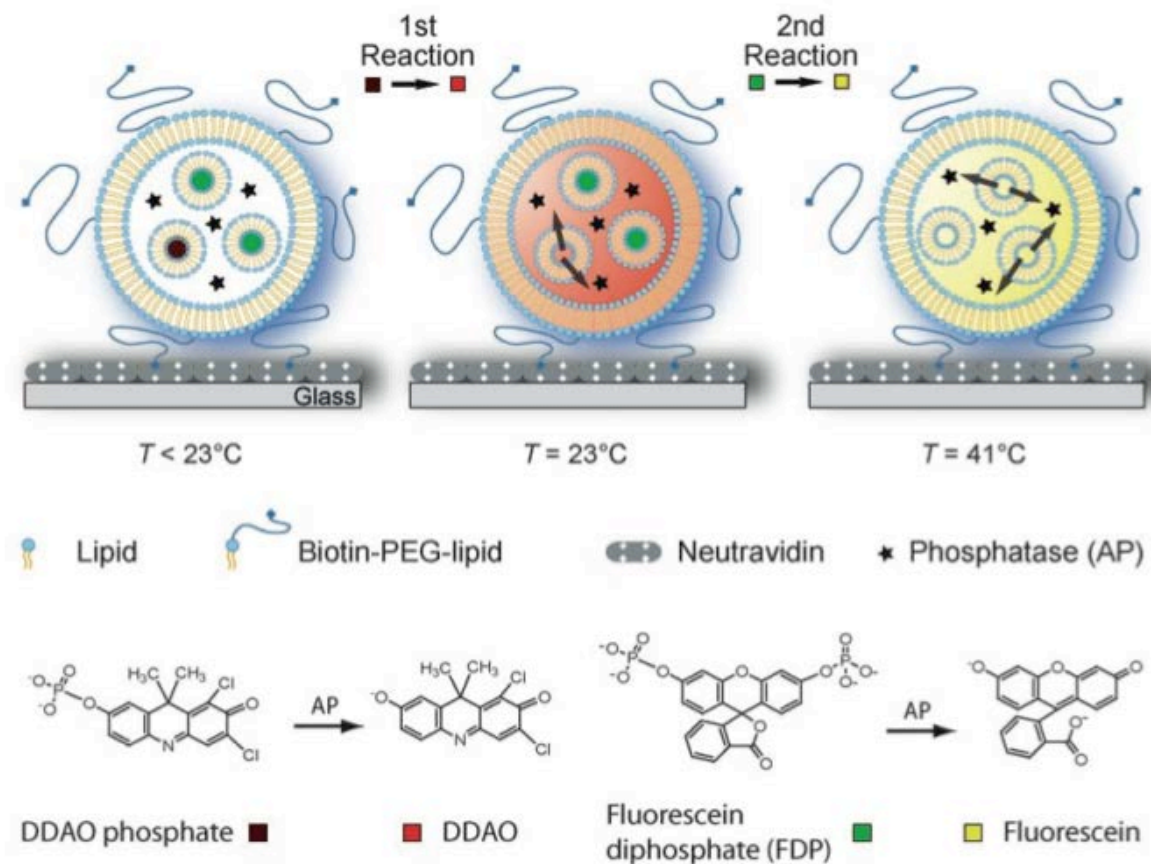
Proof of principle using fluorescein. Fluorescein is quenched in the small vesicles. After release from the small vesicles, its intensity increases.





# Nano-reactor: Nanochemistry in a vesicle

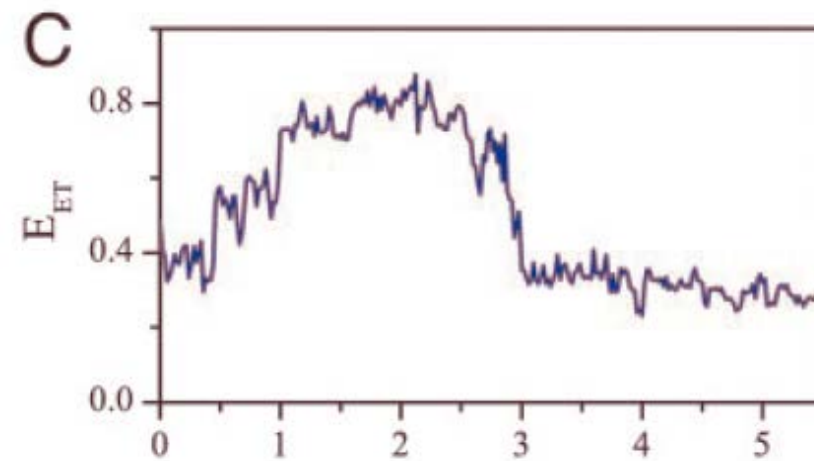
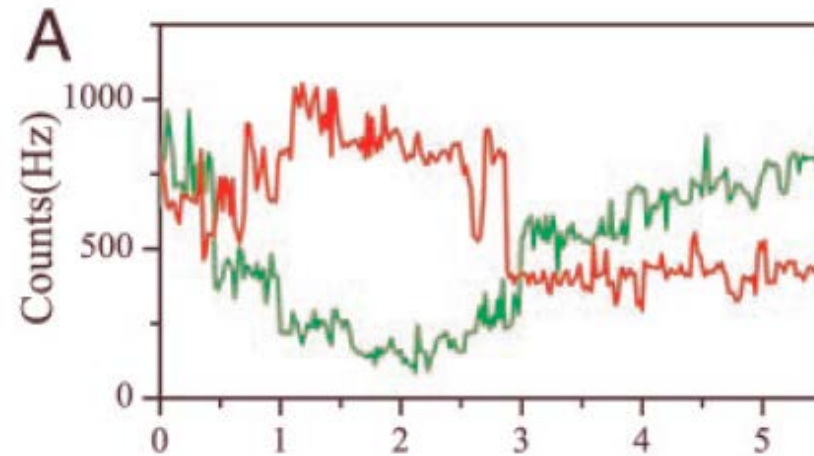
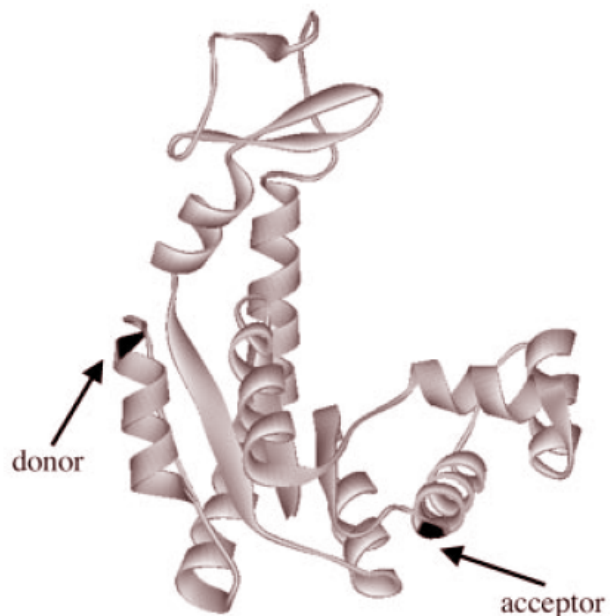
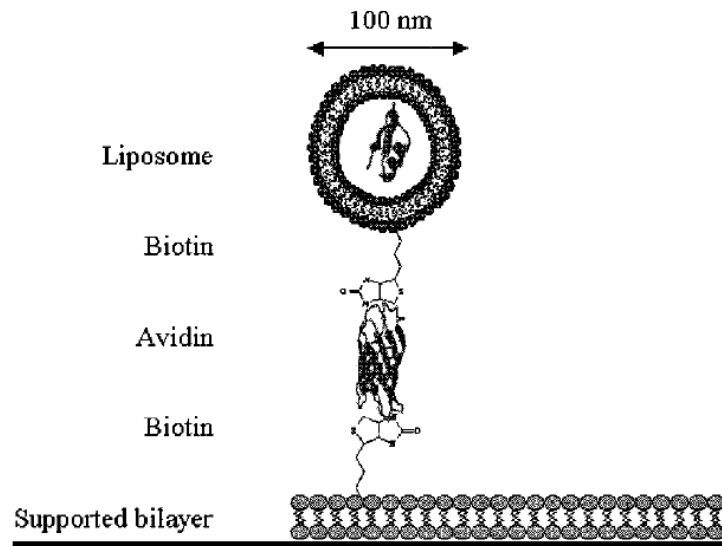
Consecutive enzymatic reactions in a single nanoreactor.



P.-Y. Bolinger, D. Stamou, H. Vogel, *Angew. Chem. Int. Ed.* **47**, 5544 (2008)

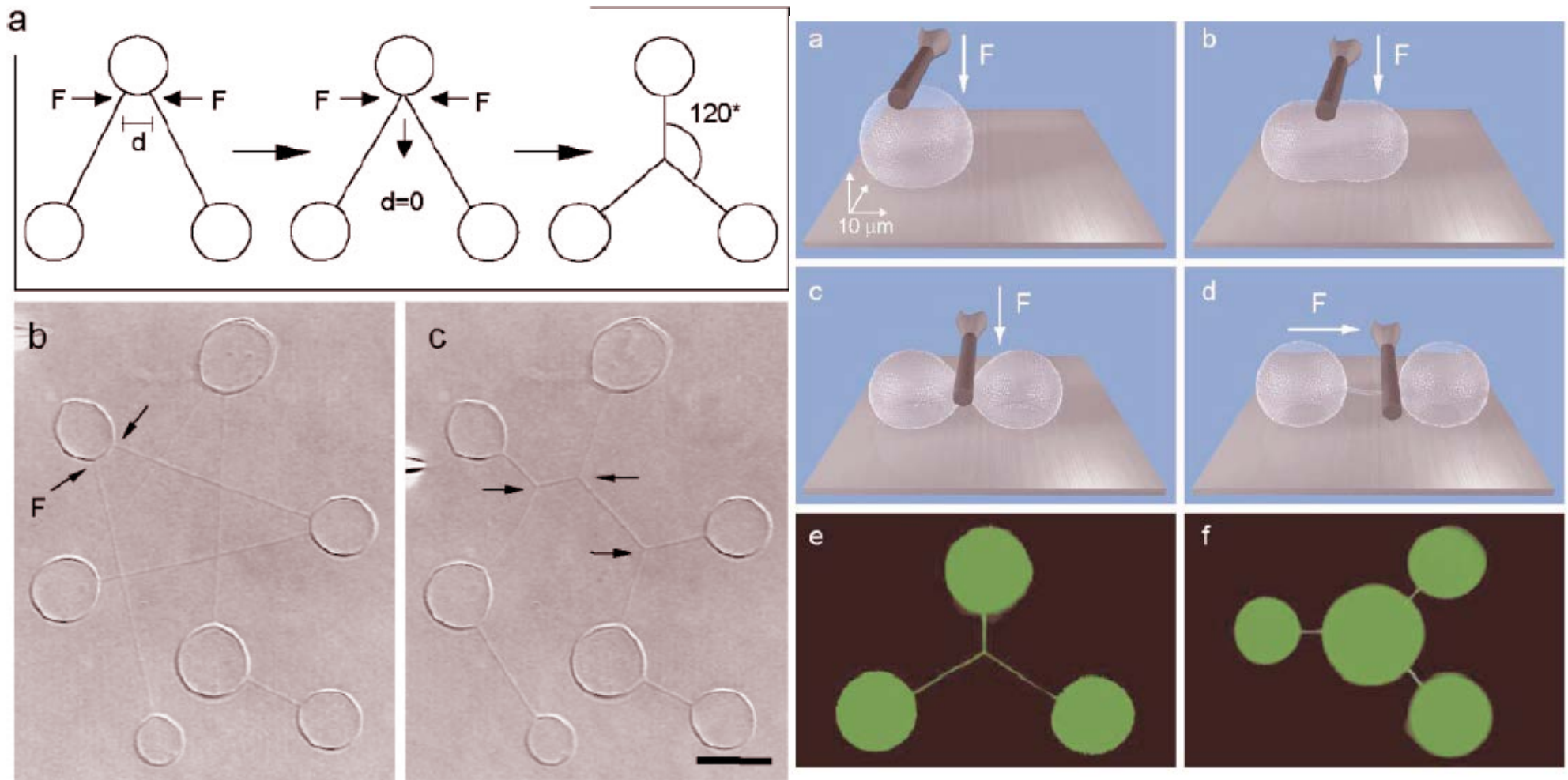
# Single-molecule investigations in nano-containers

## Protein folding of Adenylate Kinase

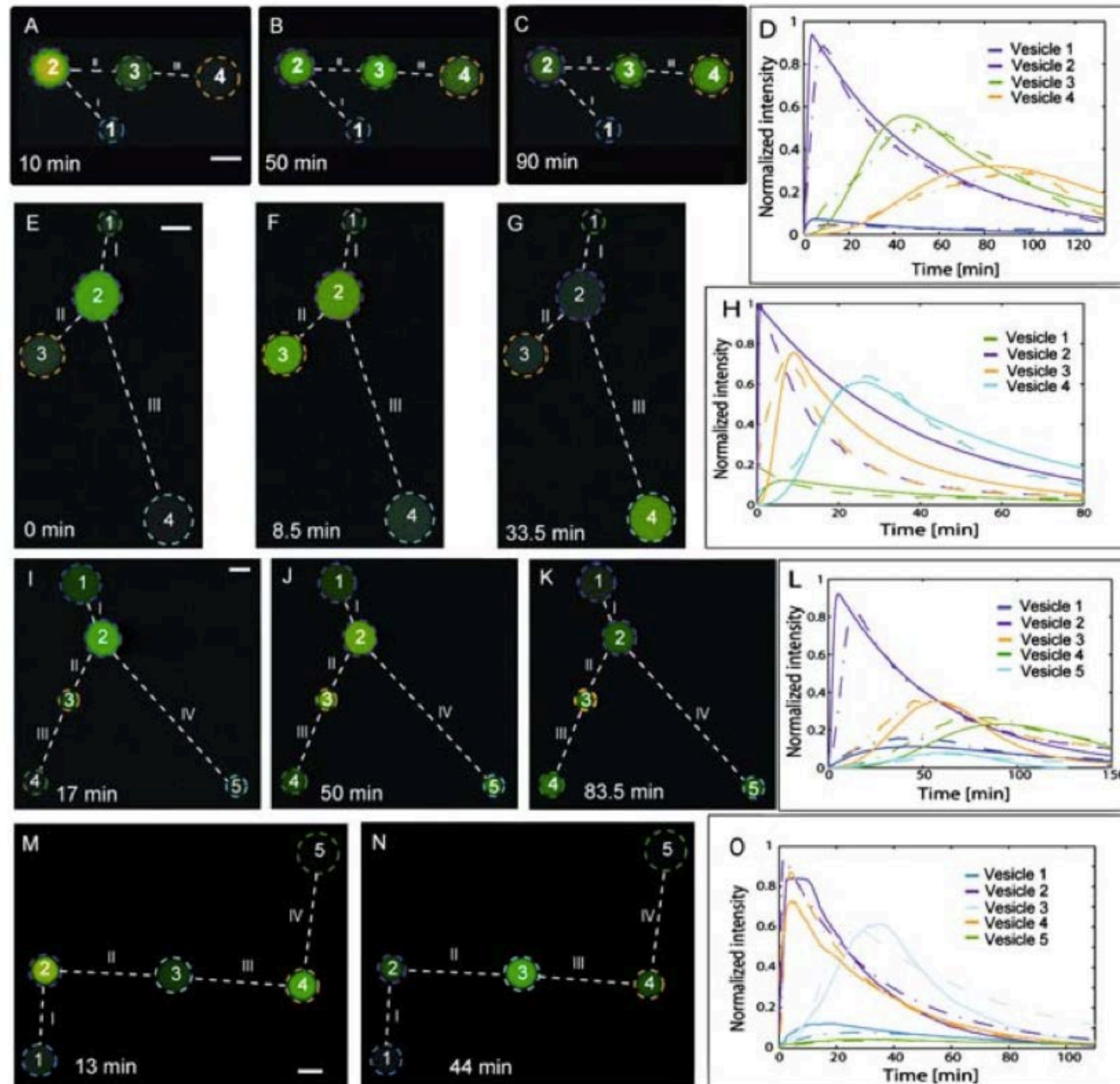




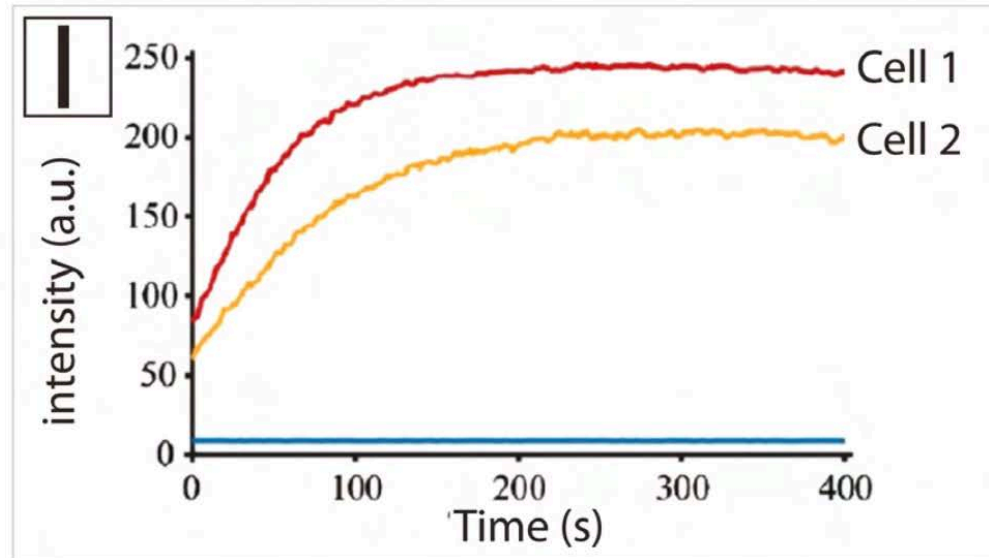
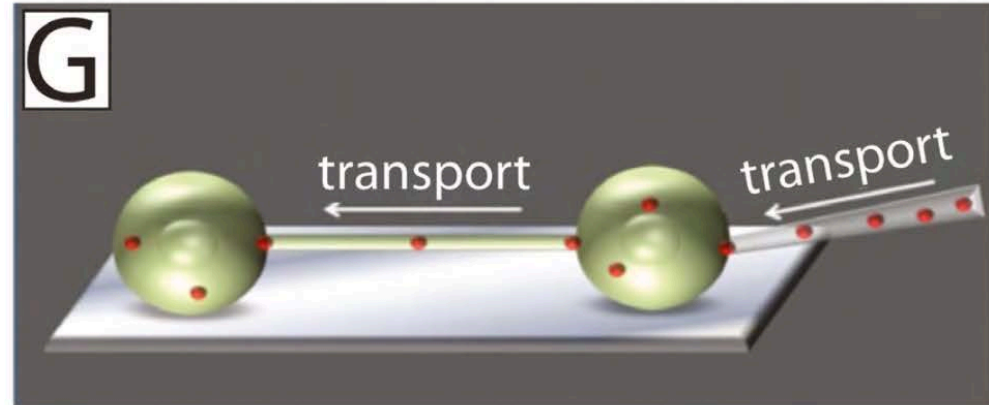
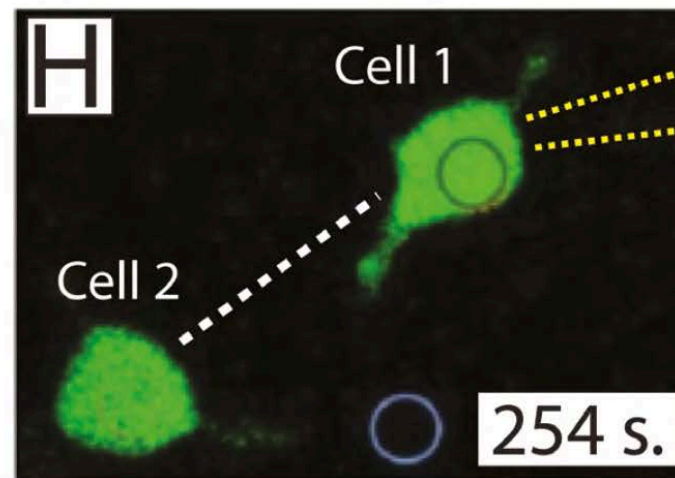
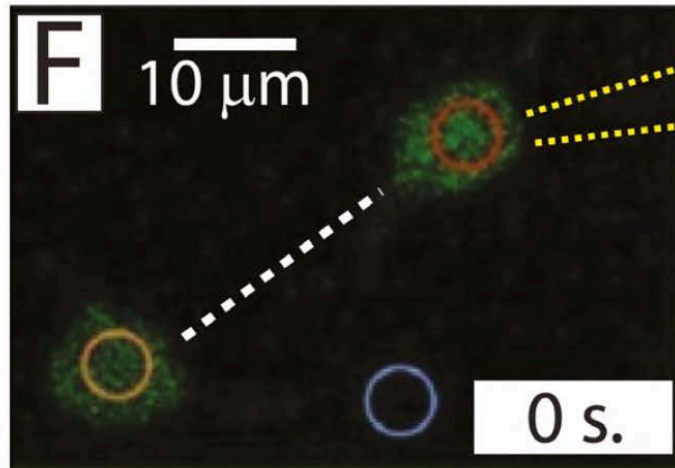
# Connecting nano-containers



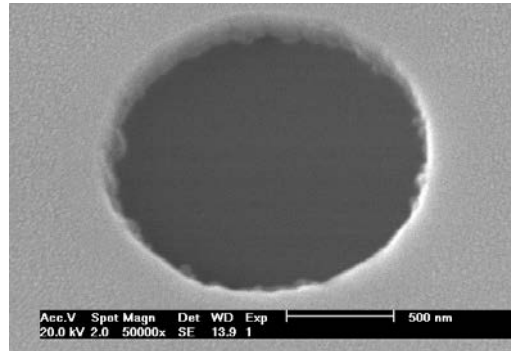
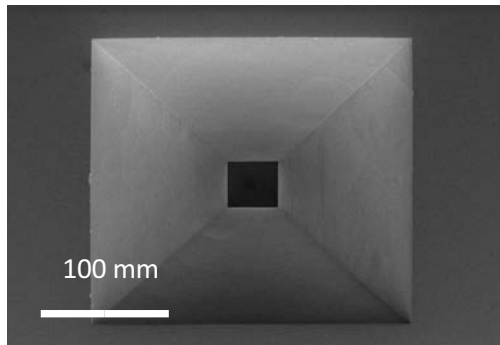
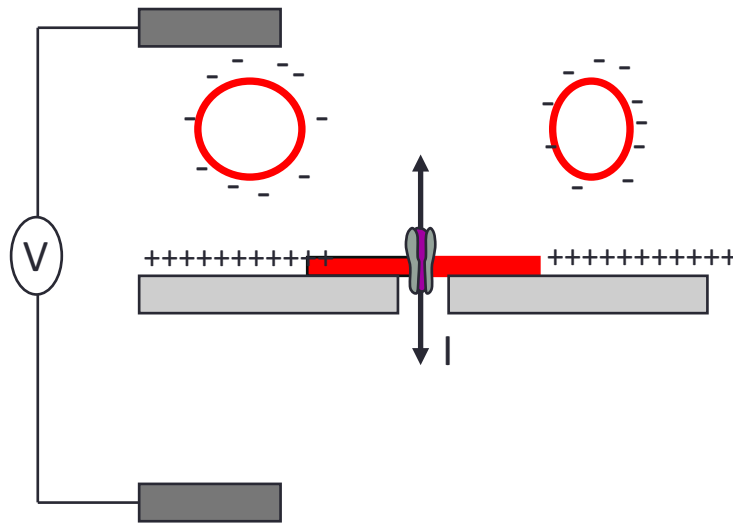
# Chemistry in network of nano-containers



## Semi-natural network of cells



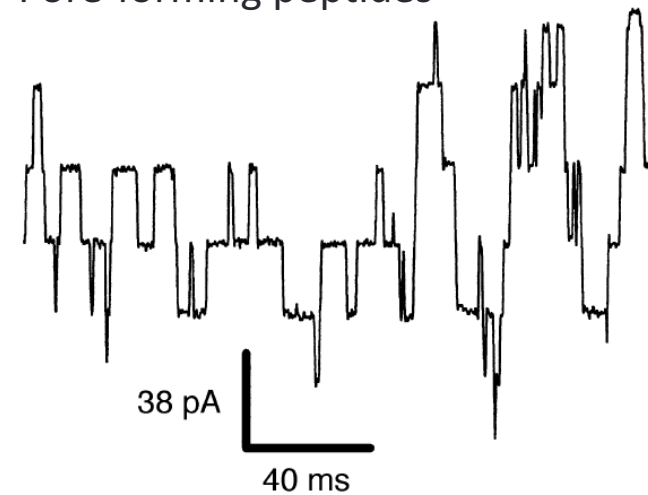
# Nano-sensors: Chips to detect signals from ion channels



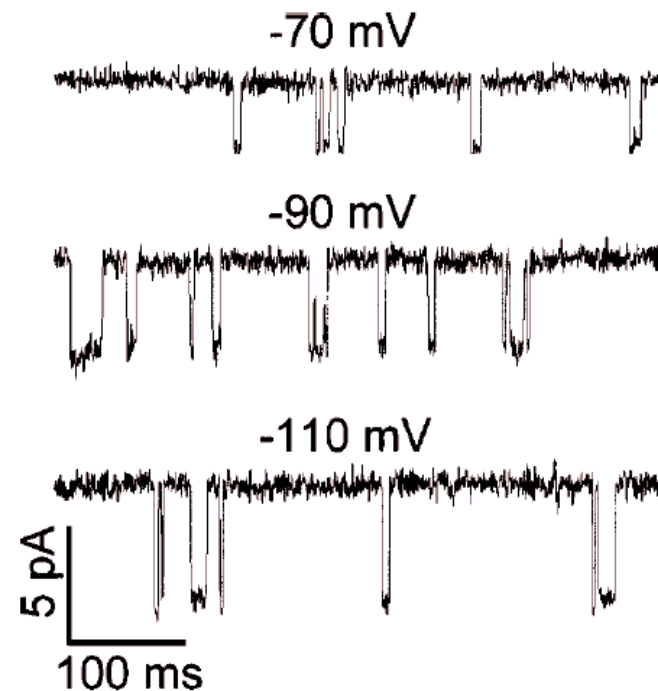
C. Schmidt, M. Mayer, H. Vogel, *Angew. Chem. Int. Ed.* **39**, 3137 (2000)

N. Fertig, M. Klau, M. George, R.H. Blick, J.C. Behrends, *Appl. Phys. Lett.* **81**, 4865 (2002)

Pore-forming peptides



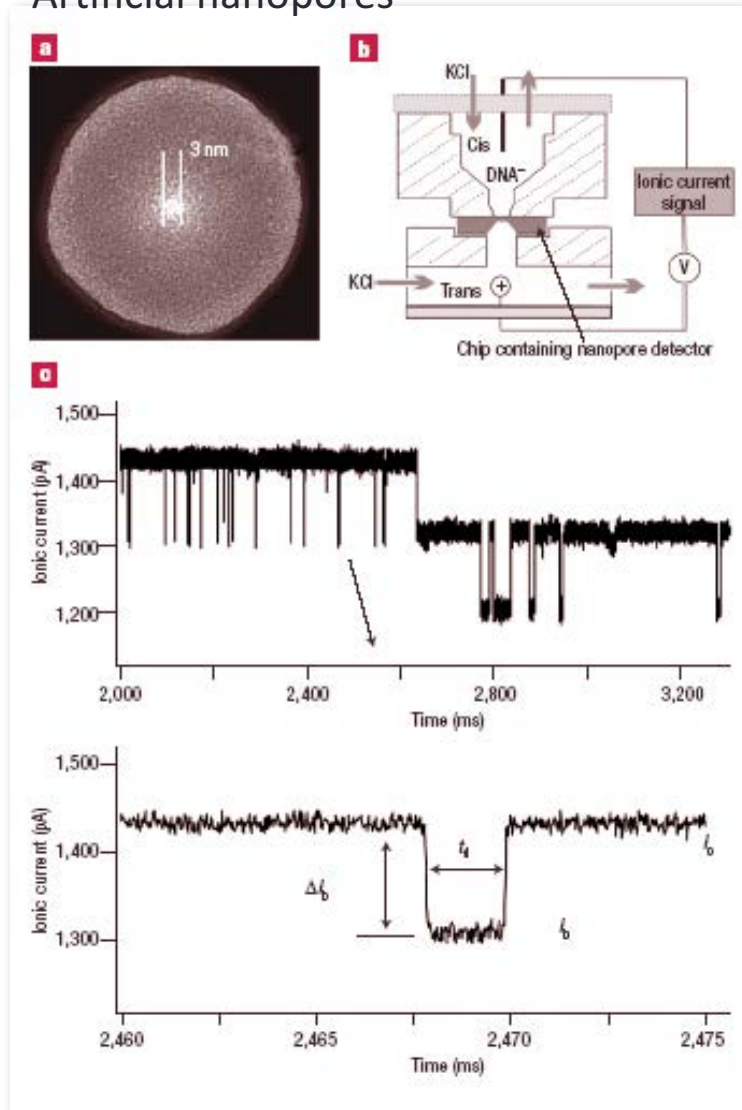
Ion channels



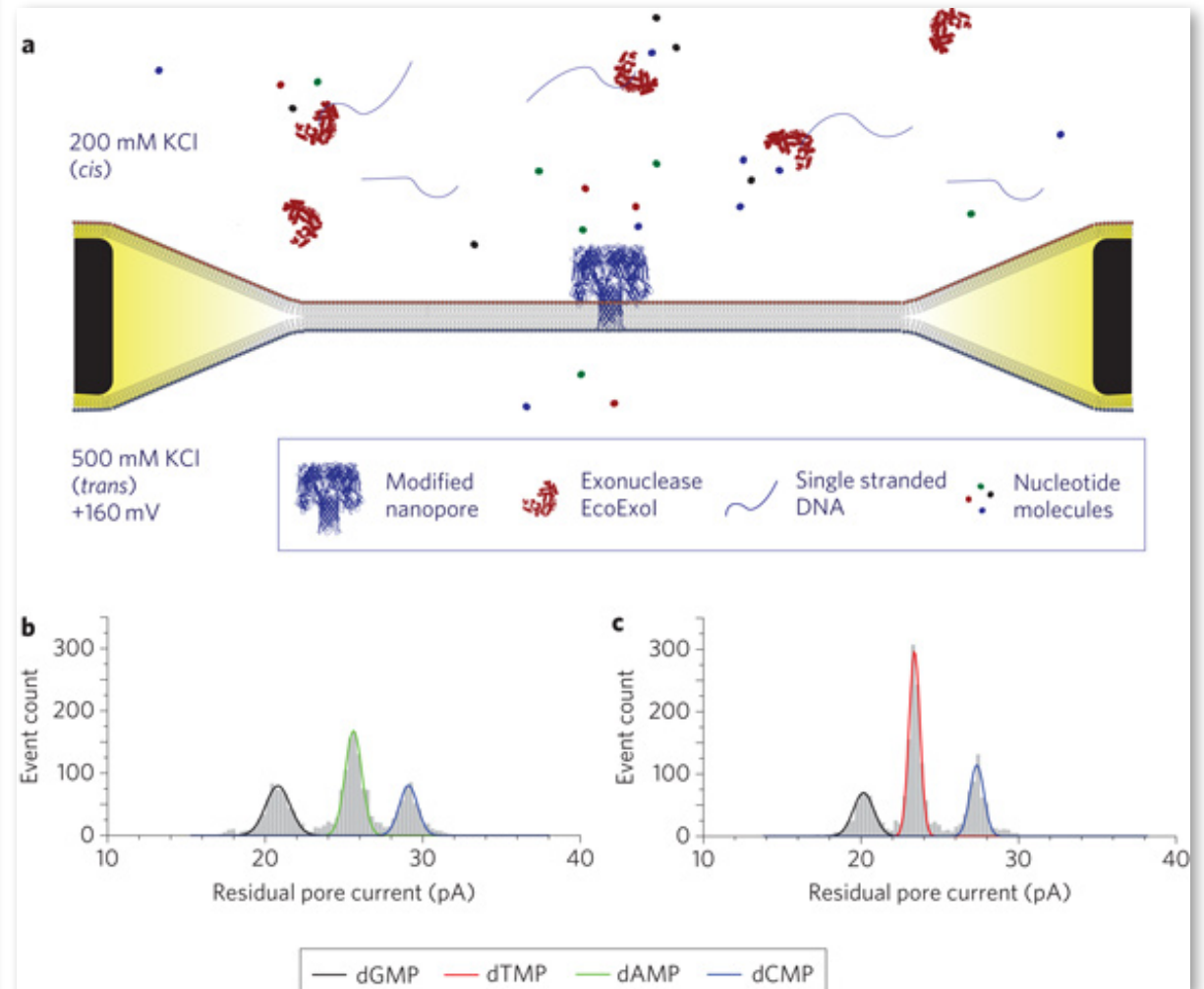


# DNA sequencing using a nano-pore

## Artificial nanopores



## Biological nanopores



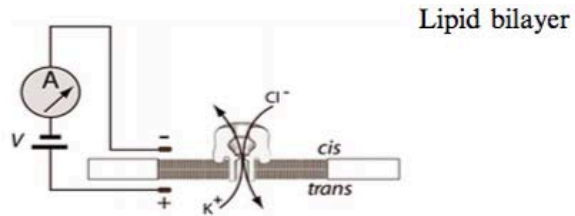
J. Li, M. Gershow, D. Stein, E. Brandin, J.A. Golovchenko, *Nature Materials* **2**, 611 (2003)

J Clarke, HC Wu, L Jayasinghe, A Patel, S Reid, H Bayley, *Nature Nanotechnology* **4**, 265 - 270 (2009)

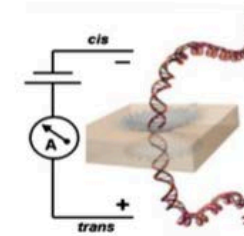


# DNA sequencing using a nano-pore

$\alpha$ -hemolysin

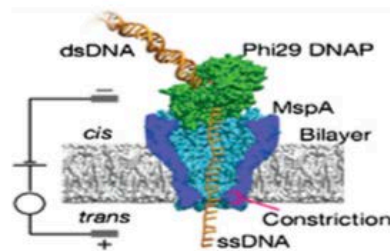


$\text{Al}_2\text{O}_3$  nanopore

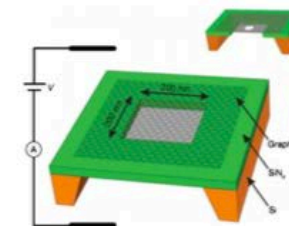


$\text{Al}_2\text{O}_3$

MspA



Single-layer membranes

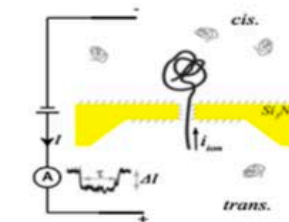


Graphene  
BN  
 $\text{MoS}_2$

Phi 29

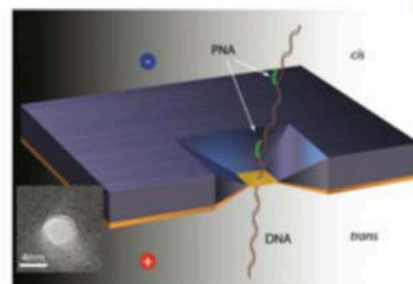


Hybrid biological/solid-state nanopores



$\text{Si}_3\text{N}_4$   
 $\text{Al}_2\text{O}_3$

Silicon-based nanopore



$\text{Si}_3\text{N}_4/\text{SiO}_2$  membrane



Feng, Y., Zhang, Y., Ying, C., Wang, D., & Du, C. (2015). *Genomics, Proteomics & Bioinformatics*, 13(1), 4–16.  
<http://doi.org/10.1016/j.gpb.2015.01.009>

Eisenstein, M. (2012, April). *Nature Biotechnology*, pp. 295–296.  
<http://doi.org/10.1038/nbt0412-295>

## Literature

J. R. Lakowicz, *Principles of fluorescence spectroscopy* (Plenum, New-York, 1999)

R. Loudon, *The Quantum Theory of Light Sec. Ed.* (Oxford University Press, 1983)

S. Weiss, "Fluorescence spectroscopy of single biomolecules", *Science* **283**, 1676 (1999)

A. Gräslund, R. Rigler, and J. Widengren *Single Molecule Spectroscopy in Chemistry, Physics and Biology Nobel Symposium* (Springer, 2010)

P. Tinnefeld and M. Sauer, "Branching Out of Single-Molecule Fluorescence Spectroscopy: Challenges for Chemistry and Influence on Biology", *Angew. Chem. Int. Ed.* **44**, 2642 (2005)

X. Michalet, Sh. Weiss, and M. Jäger, "Single-Molecule Fluorescence Studies of Protein Folding and Conformational Dynamics", *Chem. Rev.* **106**, 1785 (2006)

P. Schwille, "Fluorescence correlation spectroscopy and its potential for intracellular applications", *Cell biochem biophys* **34**, 383 (2001)

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P. Tinnefeld, C. Eggeling & S. W. Hell, *Far-Field Optical Nanoscopy*. (Springer, 2015)

<http://www.microscopyu.com/references/single-molecule-localization>